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The new Canadian Regional Analysis & Forecasting System: REG-LAM3D

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Collaborators:

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Internal Seminar, Friday, 19 June 2009, Dorval

1 Meteorological Research Division

2 Canadian Meteorological Center (Development)

3 Météo-France

4 Saskatchewan University

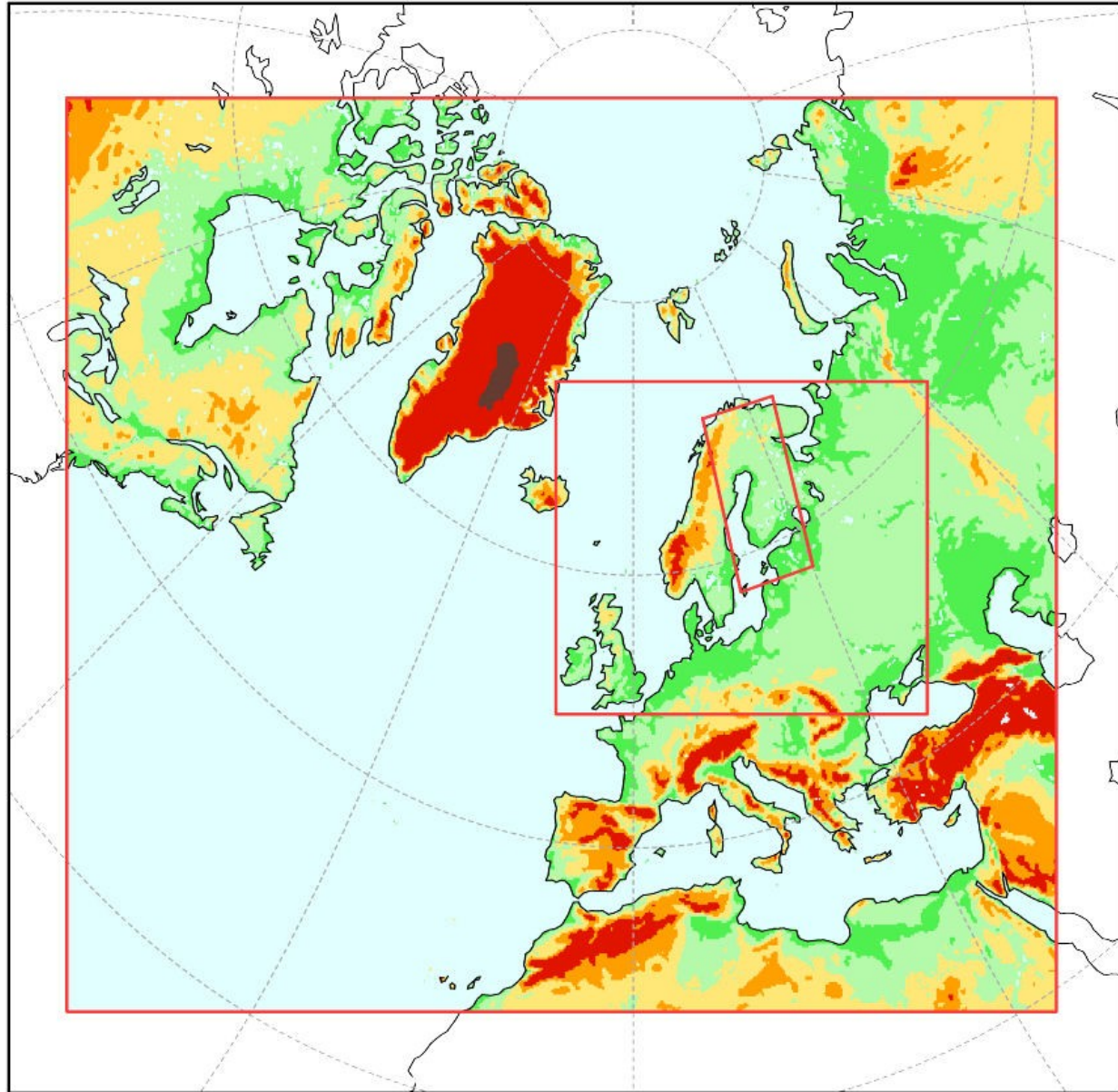
5 Canadian Meteorological Center (Operations)



Overview of the talk

- Current LAM data assimilation/forecasting systems in operational centers
- REG-LAM3D DA/Forecasting strategy
- Spectral approaches. New operators, options and configurations supported in 3D-VAR unified code
- Removing obstacles on our way to a robust REG-LAM3D system
- Evaluations of REG-LAM3D against Regional-Strato (Ervig Lapalme).
- Where we are going now: CMC Transfer & 2009-2010 Schedule
- REG-LAM-4D-Var
- VO-LAM3D-15km analysis. Special aspects of the problem + Results with full obs.
- Introduction to QC-LAM3D-1km : Radar data assimilation with McGill.

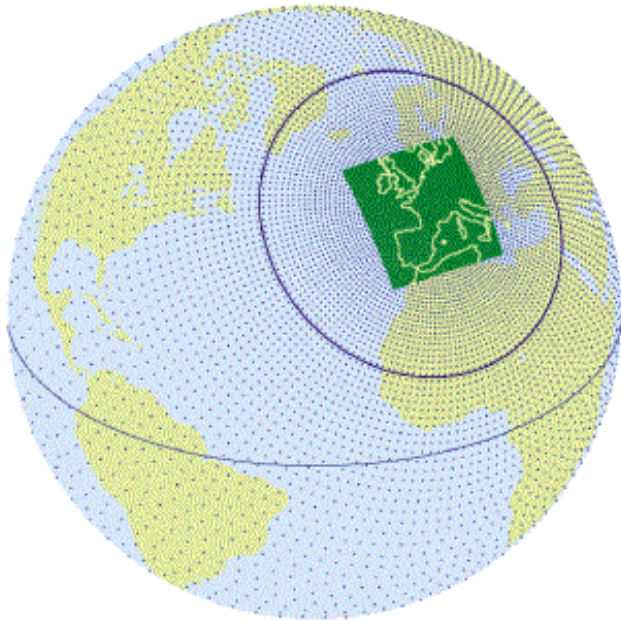
HIRLAM RCR -> HIRLAM MB71 -> AROME



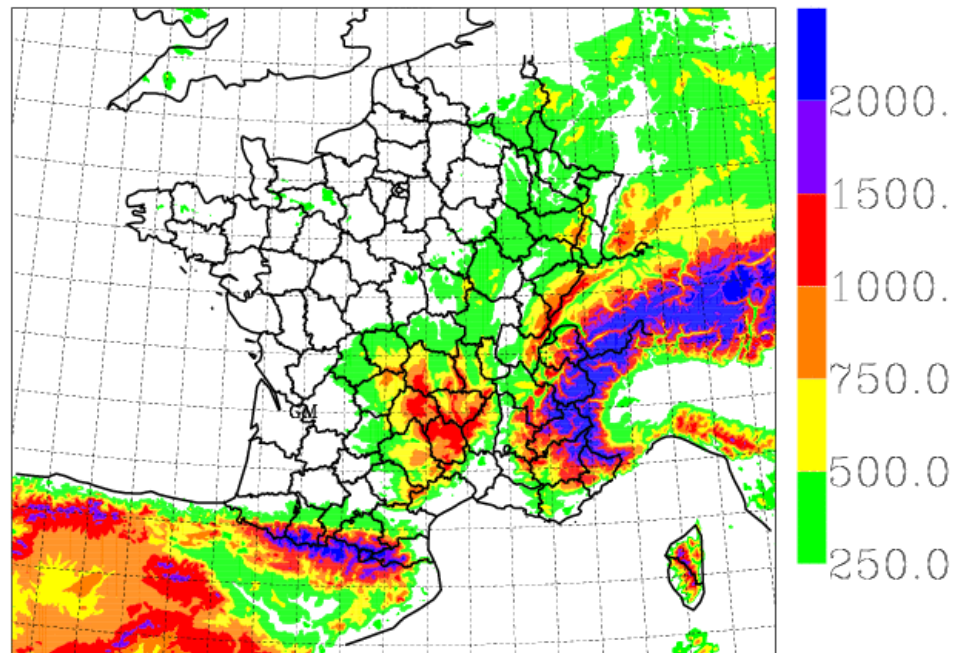
NWP at Météo-France

- NWP systems :
 - ARPEGE : global model (15 km over Europe), 4D-Var, increment at 90 km
 - ALADIN-France : regional model (9.5km), 3D-Var, increment at 9.5 km
 - AROME : meso scale model (2.5km), 3D-Var, increment at 2.5 km

ARPEGE stretched grid
and ALADIN-FRANCE domain



AROME France domain



Unified Model Operational Configurations

Global 40 km
N320L50

640x481x50 63 km top
150 million numbers

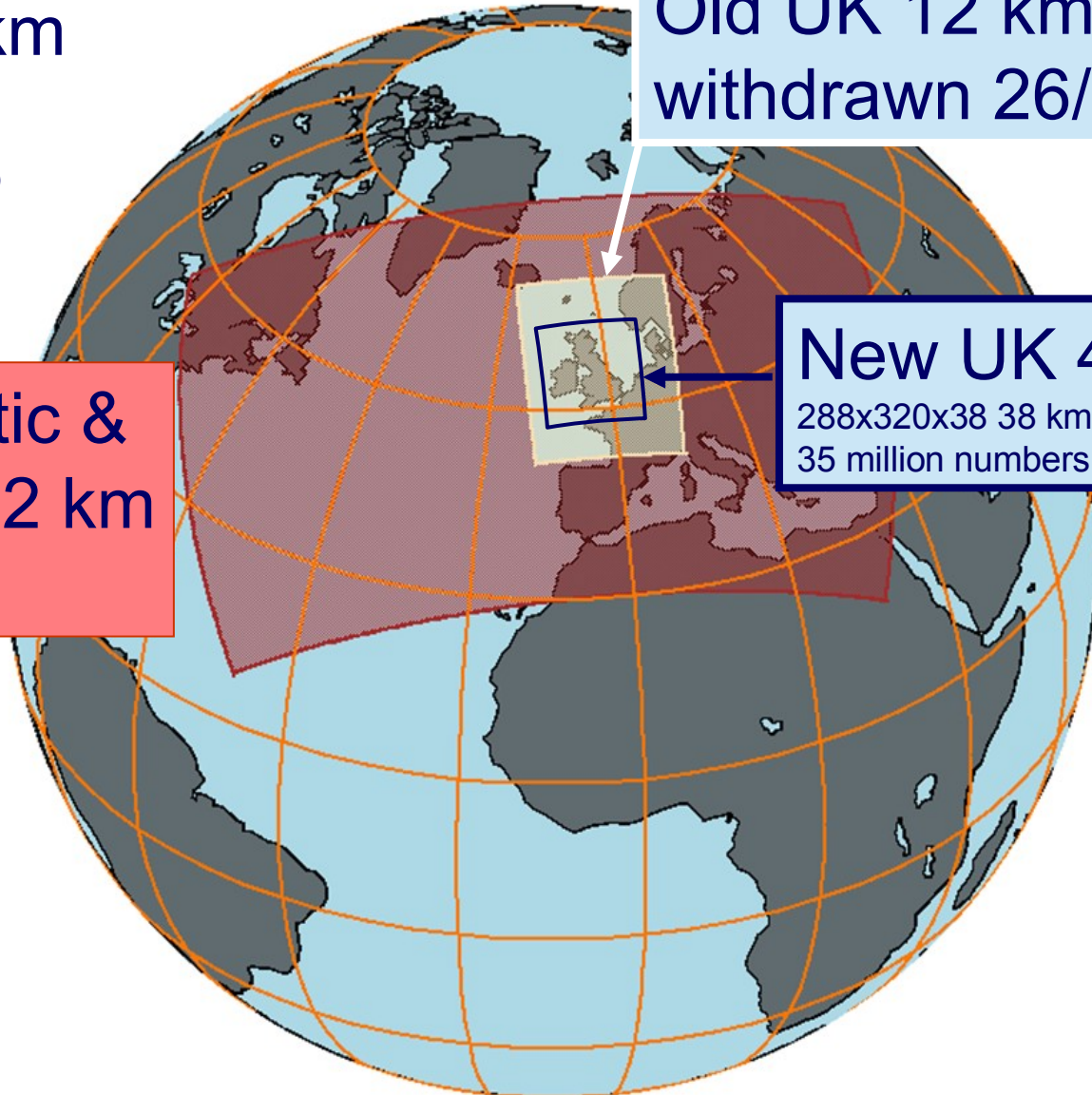
North Atlantic &
European 12 km

720x432x38 38 km top
120 million numbers

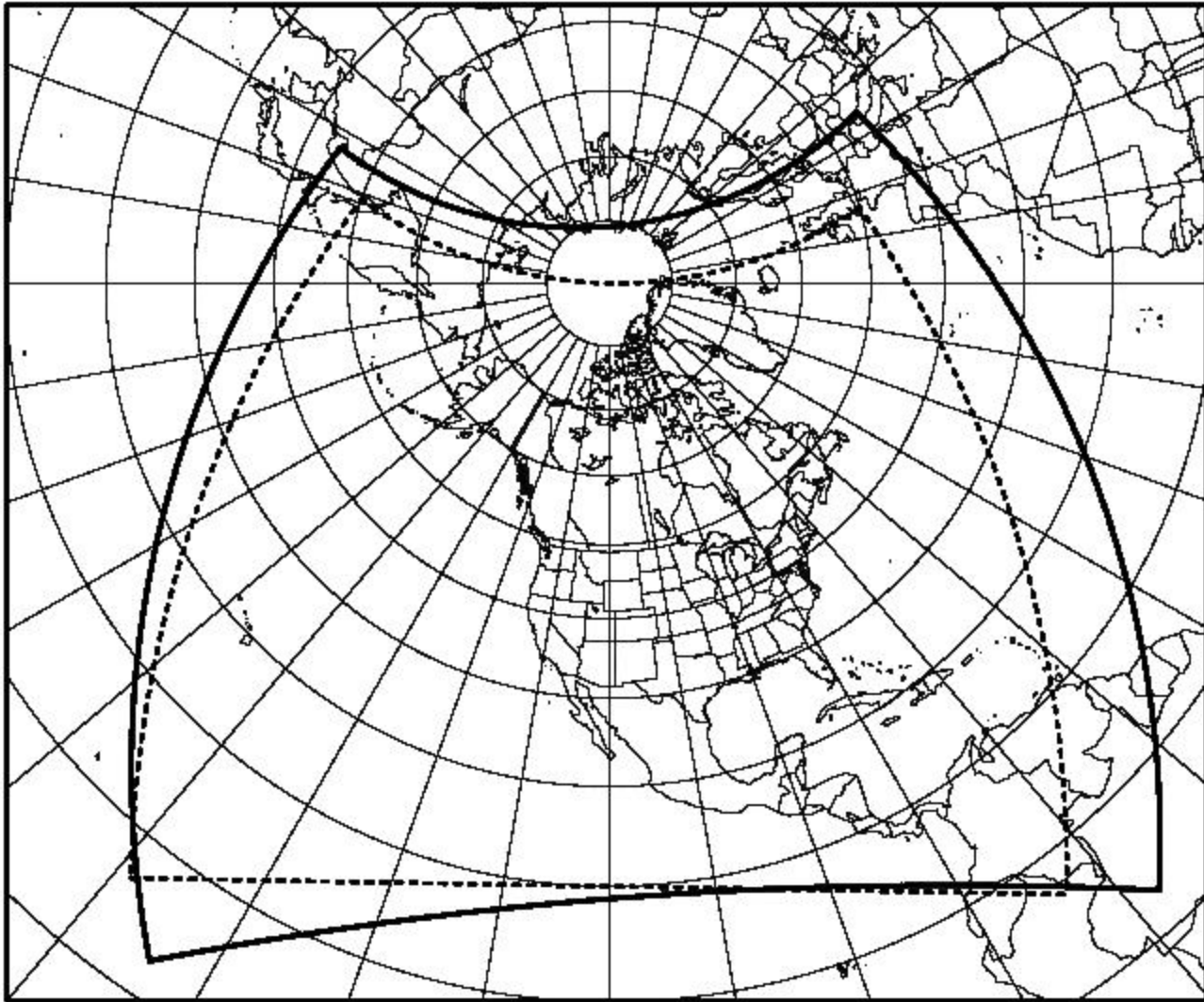
Old UK 12 km,
withdrawn 26/09/06

New UK 4 km

288x320x38 38 km top
35 million numbers



SOLID = EXPANDED NAM ; DASHED = OPS NAM

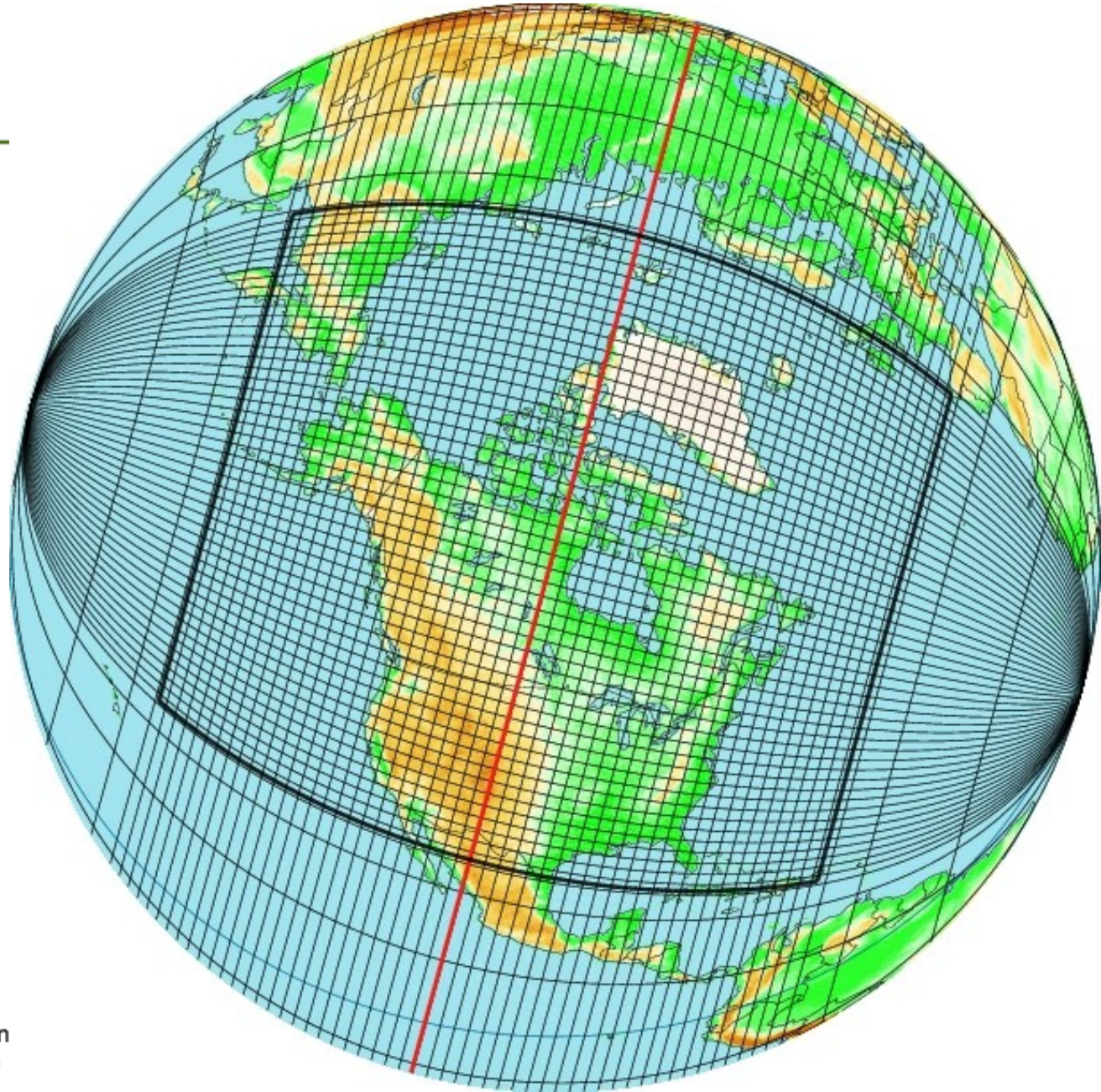


**Regional
Model
00, 06, 12, 18 UTC**

671 X 641 grid
(66% in 15-km
uniform
area), 58 levels
(soon 80 with
Strato)

Assimilation is 3D-
Var done with
global system at
T108 (~180 km)

Every 10th grid point shown



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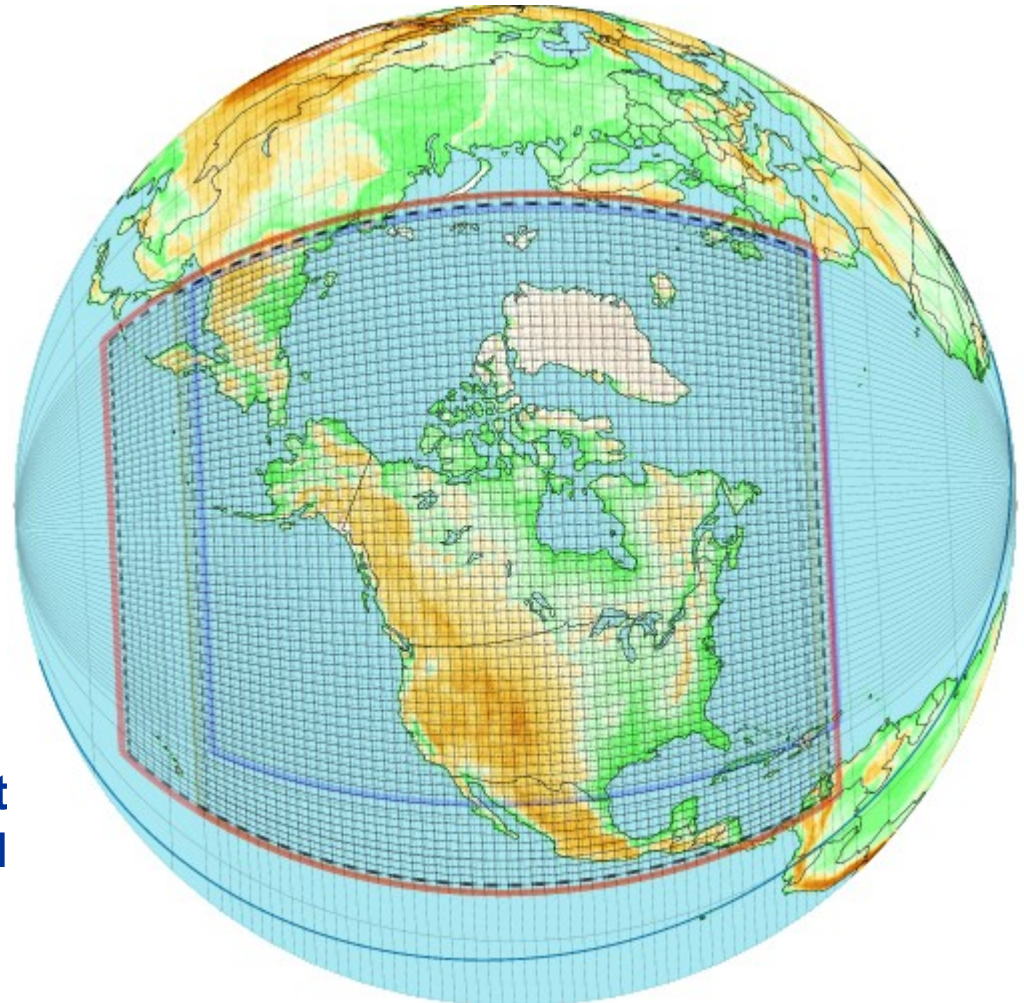
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Next regional system: Continental LAM-3DVar REG-LAM3D

Blue: Current constant resolution portion of GEM regional grid

Red: Proposed GRID of continental LAM, 15-km (649x672) with 3D-Var assimilation at 55 km on LAM-core domain (176x176)

Boundary conditions provided by GEM global at 50 km, run during the LAM data assimilation step



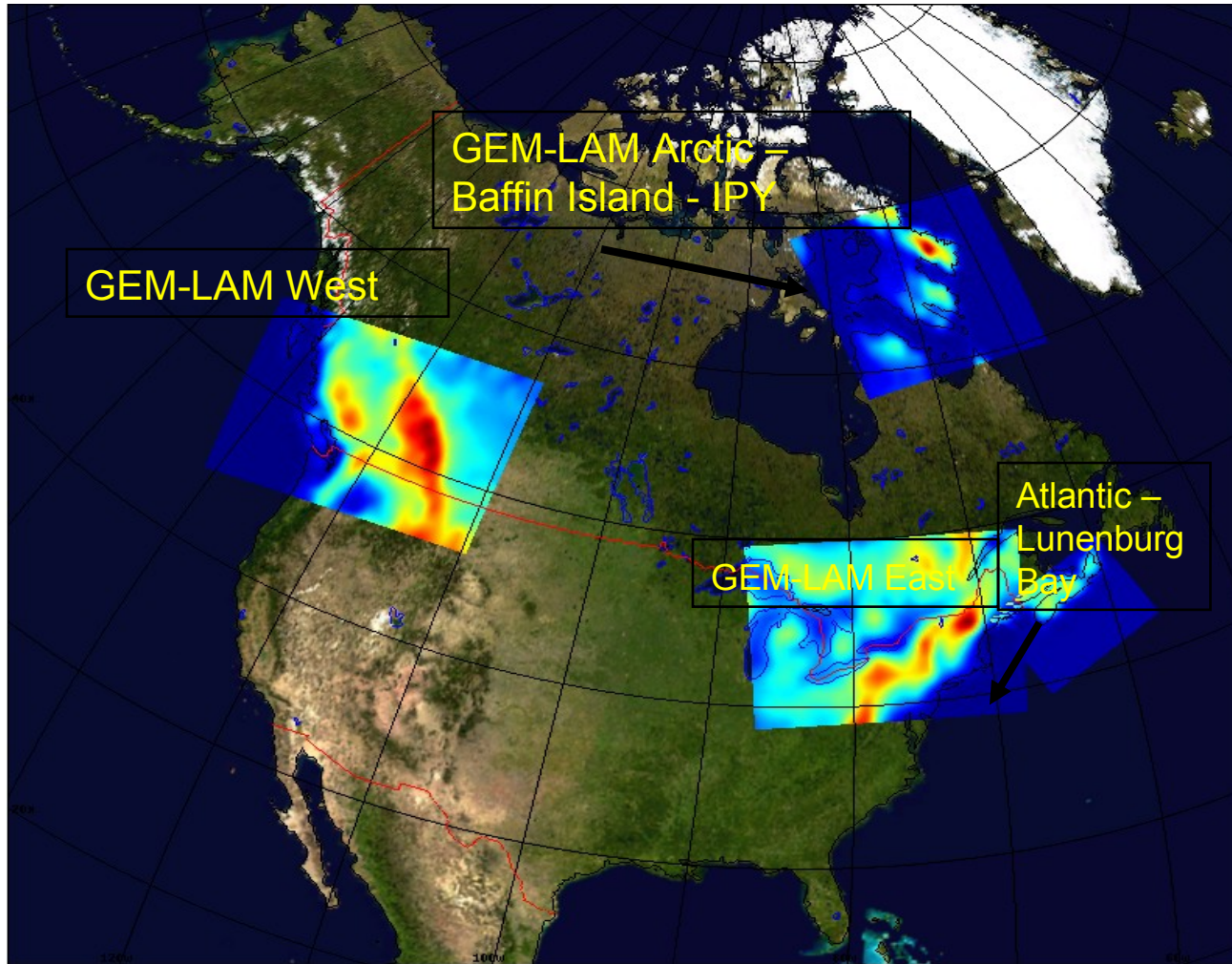


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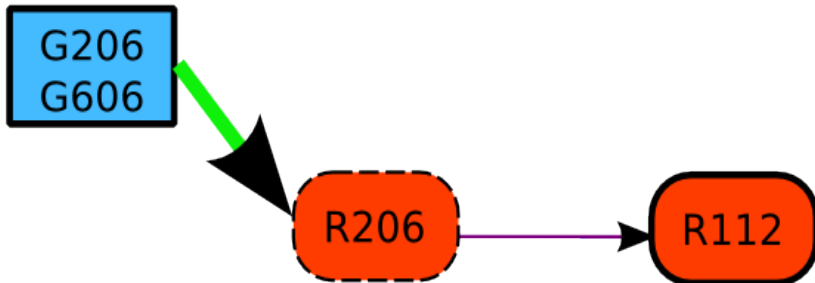
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Current local very high resolution windows Also 1-km window for 2010 winter Olympics



Spin-up Régional



Modèle Global 33 km



Modèle Régional 15 km



Pilote



Champ d'essai



Analyse globale



Analyse non produite

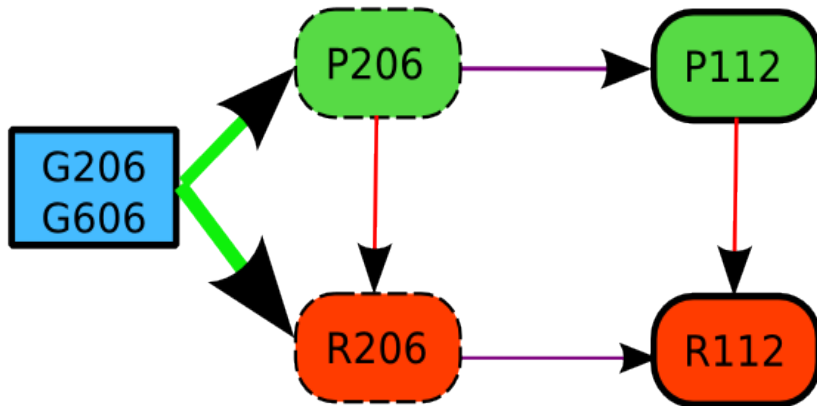


Analyse 3D-VAR FGAT



Analyse 4D-VAR

Spin-up REG-LAM3D



Modèle Global 33 km



Modèle Global 55 km



Modèle LAM 15 km



Pilote



Champ d'essai



Analyse globale



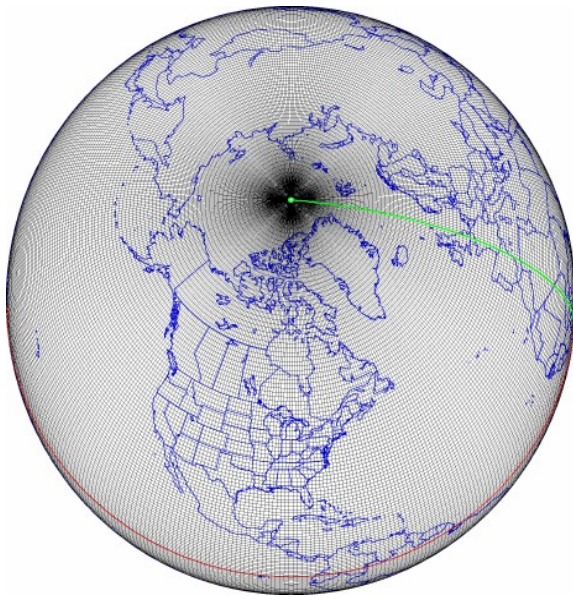
Analyse non produite



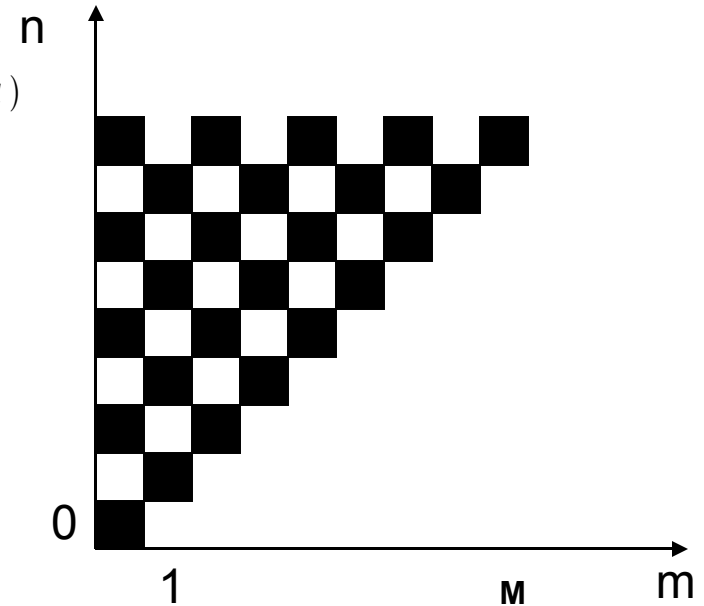
Analyse 3D-VAR FGAT



Analyse 4D-VAR



$$\zeta(\lambda, \mu) = \sum_{m=-M}^M \sum_{n=|M|}^M \zeta_n^m Y_n^m(\lambda, \mu)$$



► **Forward Two-Dimensional DFT**

$$F_{jk} = \frac{1}{MN} \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} f_{mn} \omega_M^{-mj} \omega_N^{-nk} \quad j=0:M-1; k=0:N-1$$

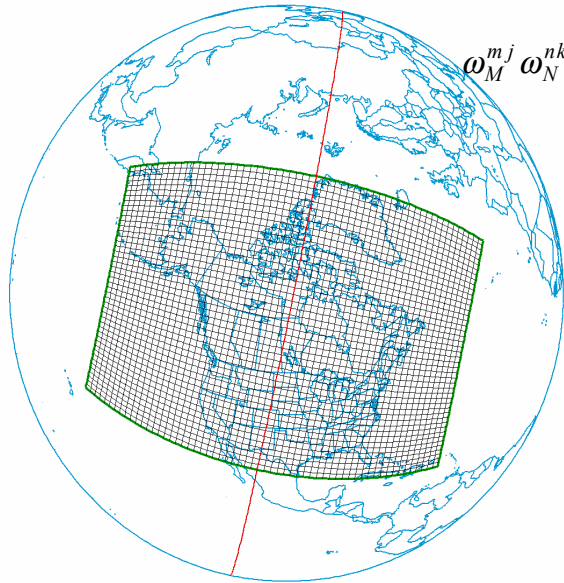
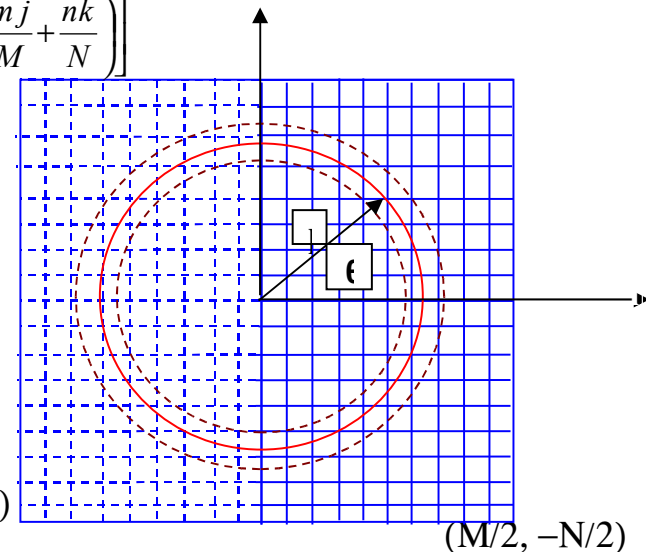
► **Inverse Two-Dimensional DFT**

$$f_{mn} = \sum_{j=0}^{M-1} \sum_{k=0}^{N-1} F_{jk} \omega_M^{mj} \omega_N^{nk} \quad m=0:M-1; n=0:N-1$$

$$\omega_M^{mj} \omega_N^{nk} = e^{i2\pi\left(\frac{mj}{M} + \frac{nk}{N}\right)} = \cos\left[2\pi\left(\frac{mj}{M} + \frac{nk}{N}\right)\right] + i \sin\left[2\pi\left(\frac{mj}{M} + \frac{nk}{N}\right)\right]$$

The integer N must be factorizable in the form:

$$N = 2^p 3^q 5^r$$



Specific aspects of the LAM analysis

In 'LU' mode: (Kilometric-scale configuration for transfer to CMC)

- Uses bi-fourier representation (DFT-2D)
- Arakawa-C grid. Analysis increments are bi-periodic on the *extended* computational grid.
- Uses a Rotated analysis grid (following same approach as in GEM).
- A fast wind-rotation operator (& adjoint) is used at the end of the process of constructing the analysis increment before computing departures with innovation vector at each simulation of 3D-VAR

In 'GU' & lcva_hemis = .true. mode: (Regional-continental configuration for tranfer to CMC)

- Uses Hemispheric-spectral representation
- Based on symmetrized NH/SH background-error fields and associated statistic file.
- mbal_order = 0 enforced !

New features in 3D-Var

&NAMDIM

`nj = 250,`
`njinc = 250,`
`njsur = 2,`
`ni = 250,`
`niinc = 250,`
`nisur = 2,`
`nflev = 80,`
`nvgaux=0,`
`ntrunc=100,`
`ntruncinc=100,`
`nsaux=0.,`
`nlatbin=1,`

&NAMGRD

`multi_grd=0,`
`grd_typ='LU', (grd_typ='GU')`
`nila=250,`
`njla=250,`
`grd_dx = 0.4832,`
`grd_dy = 0.4832,`
`grd_iref = 101,`
`grd_jref = 71,`
`grd_latr = 0.0,`
`grd_lonr= 180.06875,`
`grd_xlon1=-97.,`
`grd_xlat1=64.,`
`grd_xlon2=-85.,`
`grd_xlat2=75.,`
`mextendx=74,`
`mextendy=74,`
`Glb_pil_n=7,`
`Glb_pil_s=7,`
`Glb_pil_e=7,`
`Glb_pil_o=7,`

&NAMCVA

`...`
`lcva_hemis = .false.,`
`lcva_helm = .true.,`
`lcva_euclid = .false.,`
`lsw= .false.,`
`l simulcor=.false.,`
`l1obs= .false.,`
`cptot= 'SP',`
`mbal_order = 0,`
`...`



Spectral manipulations

grd_typ = 'GU'

```
do jn = 0, ntrunc  
  ila = nind(jm) + jn - jm  
  do jk = 1, nkdim  
    sp(ila,1,jk) = ...  
    sp(ila,2,jk) = ...  
  enddo  
enddo
```

grd_typ = 'LU'

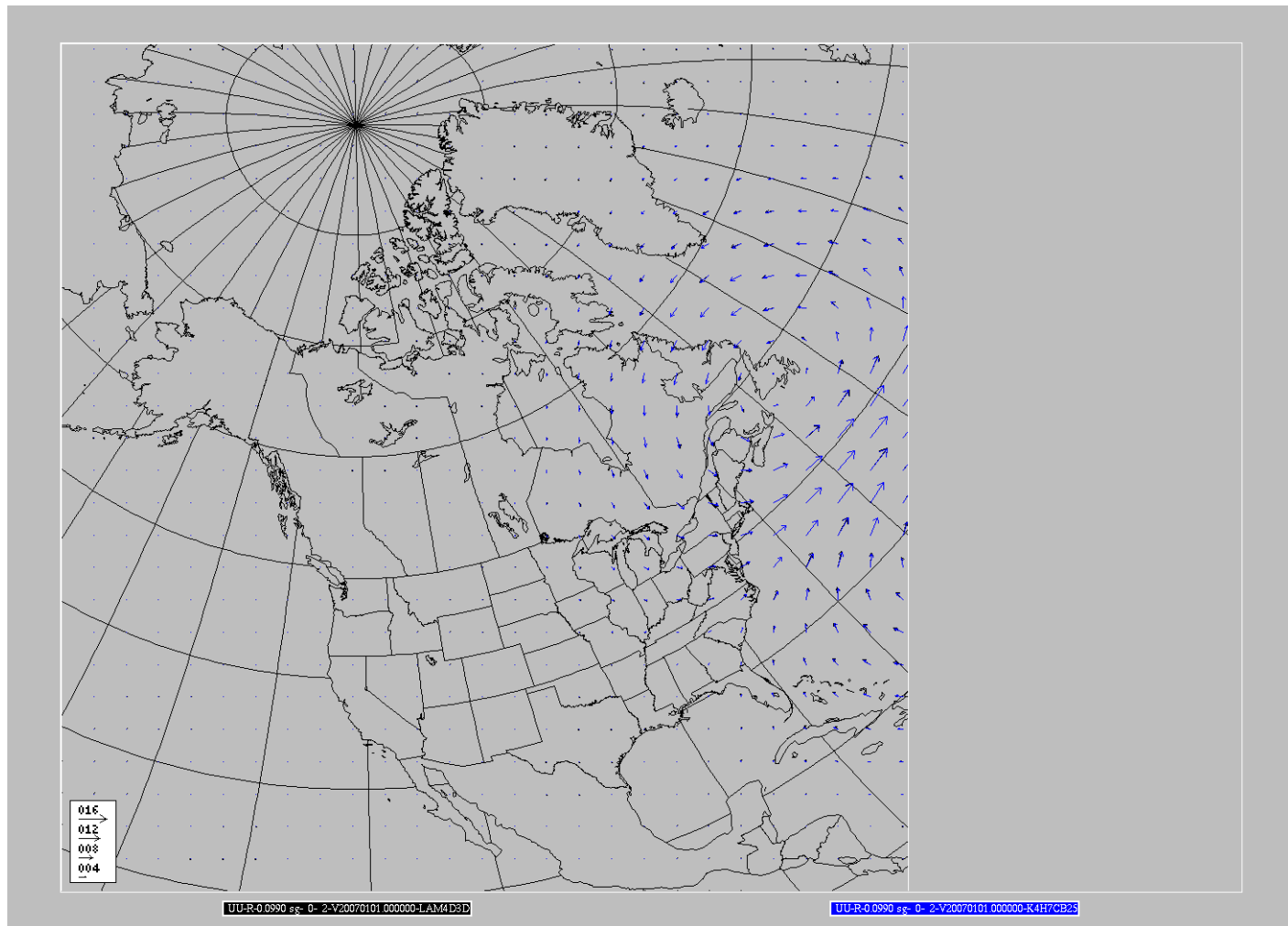
```
do jband = 1, nband  
  do jm = 1, mbandsp(jband)  
    ila = mila(jm,jband)  
    do jk = 1, nkdim  
      sp(ila,1,jk) = ...  
      sp(ila,2,jk) = ...  
    enddo  
  enddo  
enddo
```

58 Lev; GU versus LU:

1obs_UU = 1.0 ms⁻¹ at 10 hPa (Level 12),

Isimulcor, cptot = 'GD', Isdevsim

Validation + Extension test



The Standard NMC approach for control variables: Initial implementation in REG-LAM3D/4D.

$$\mathbf{\Delta x} \equiv \overbrace{(\Delta\psi, \mathbf{\Delta}\chi_b, \mathbf{\Delta}T_b, 0, \mathbf{\Delta}p_{sb})^T}^{\text{Balanced}} + \overbrace{(0, \mathbf{\Delta}\chi_u, \mathbf{\Delta}T_u, \mathbf{\Delta}q, \mathbf{\Delta}p_{su})^T}^{\text{Unbalanced}}$$

- Construction of P_b from ψ using Local Balance Equation:

$$\nabla^2 \Delta P_b = - \nabla \cdot (f k \times \Delta v_\psi)$$

- Spectral form of Regression matrix to derive T_b and p_{sb} :

$$\begin{bmatrix} \Delta \tilde{T}_b \\ \Delta \tilde{p}_{sb} \end{bmatrix} = \tilde{V} \Delta \tilde{P}_b$$

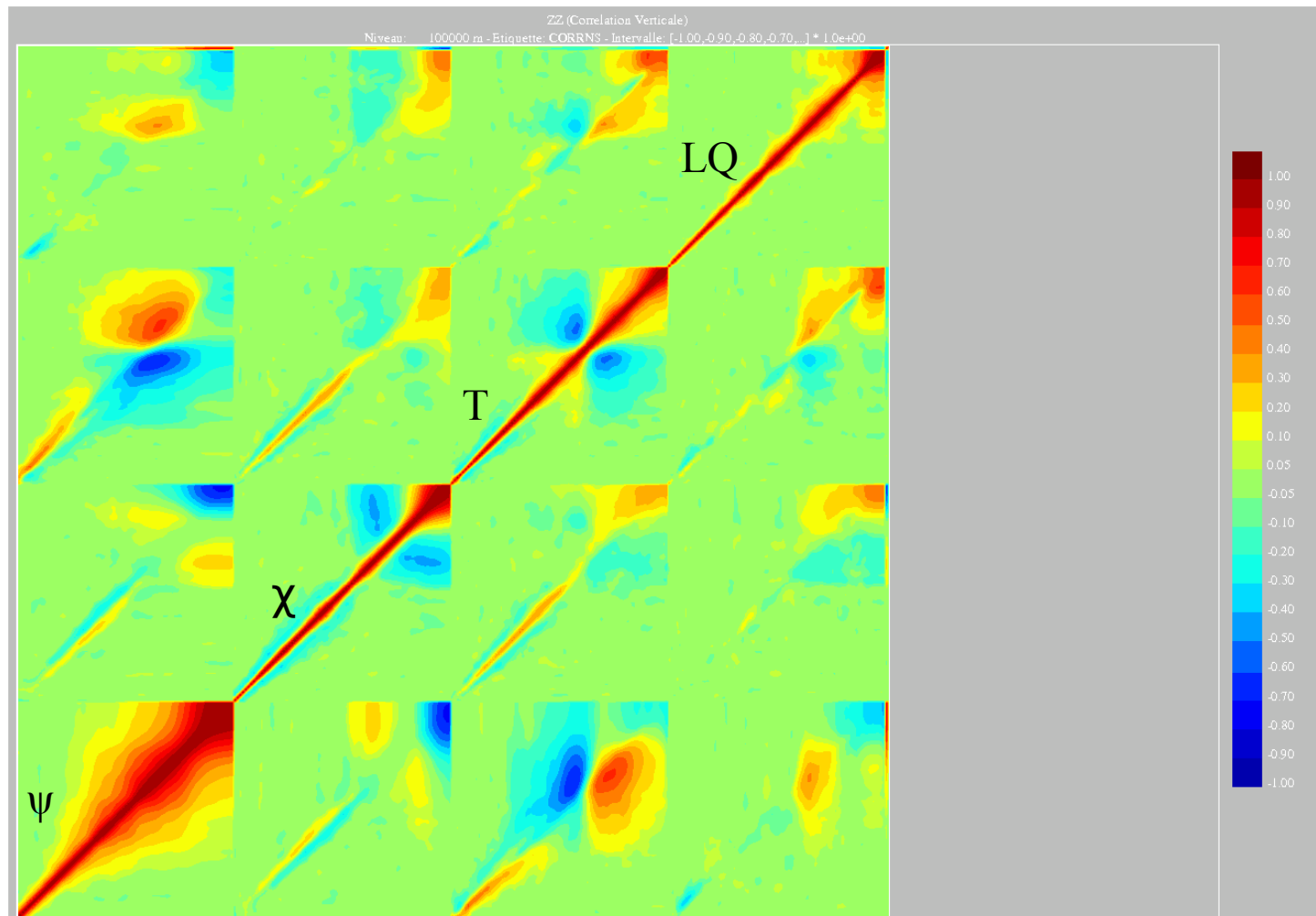
Feb. 2009: New formulation (Transfer to CMC) Unified “balance-free” control variables: mbal_order = 0 for REG-VAR & Kilometric Analyses

$$\mathbf{\Delta x} \equiv (\Delta\psi, \mathbf{\Delta}\chi, \mathbf{\Delta}T, \mathbf{\Delta}\ln q, \mathbf{\Delta}p_s)^T$$

Off-diagonal blocs are kept to represent mass-wind coupling and vort-div Eckman coupling for each total horizontal wavenumbers.

REG-LAM3D-55 km: DFT-2D-100: 250x250; NMC-24-48: Winter 2007-Oper.Strato-Jun-09

k = 5



Champ valide 12:00Z le 19 février 2007

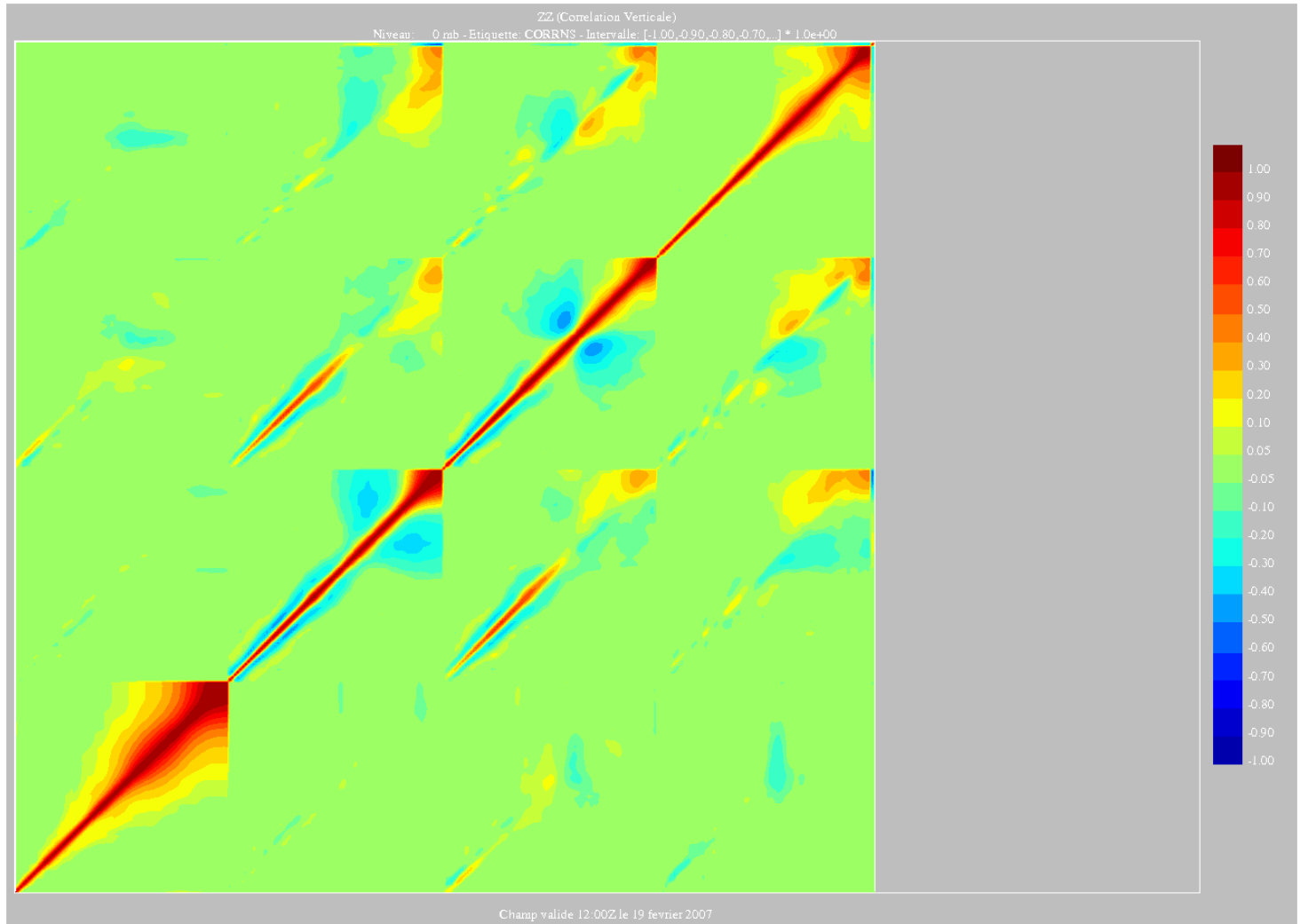


Global statistics:

Global-50 km: T-300: 720x360;

NMC-24-48: Winter 2007-Oper.Strato-Jun-09

n = 20

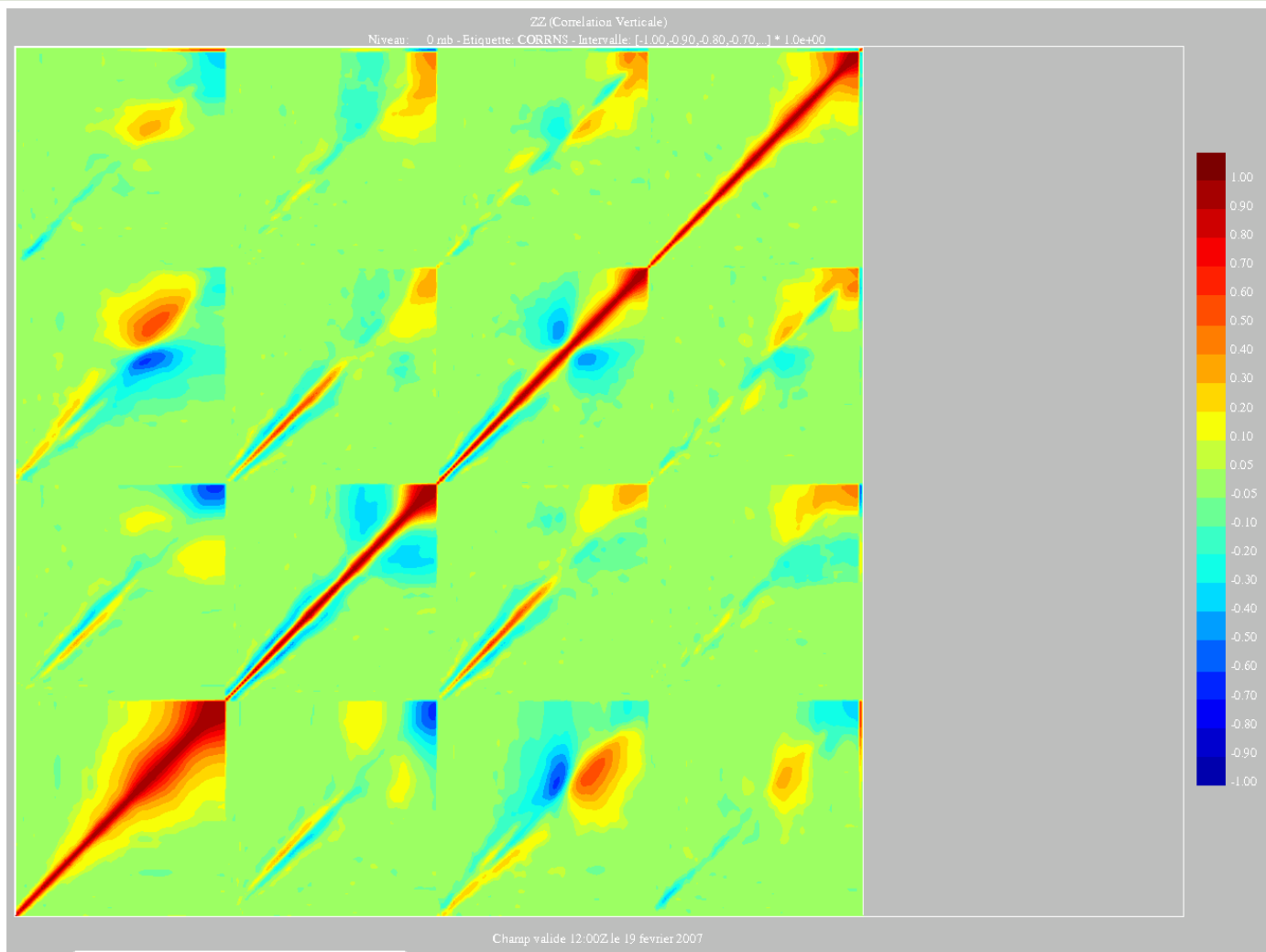


Northern-Hemisphere:

k = 20; Spectral-Hemispheric-50 km: T-300: 720x360;

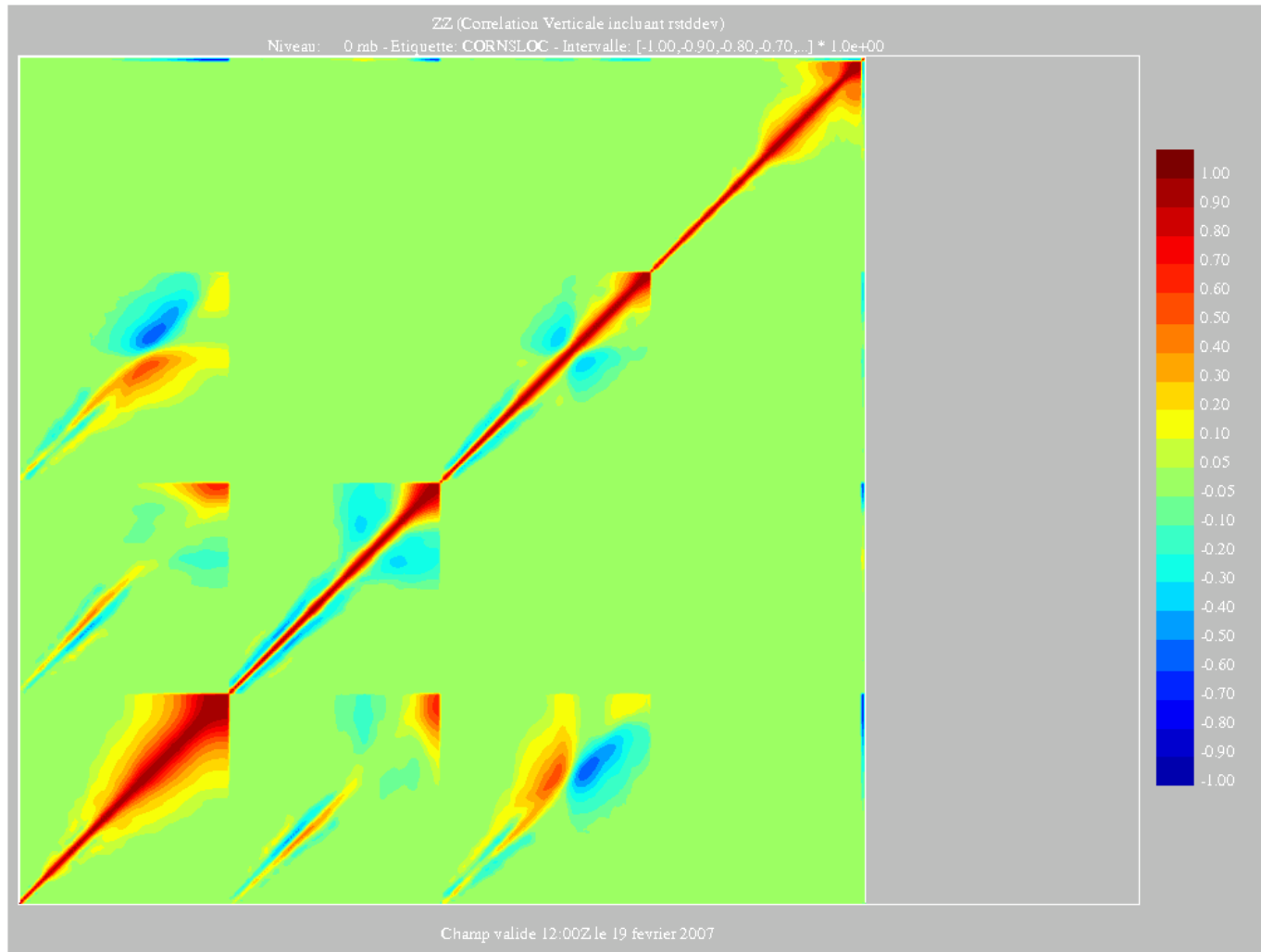
NMC-24-48: Winter 2007-Oper.Strato-Jun-09

n = 20



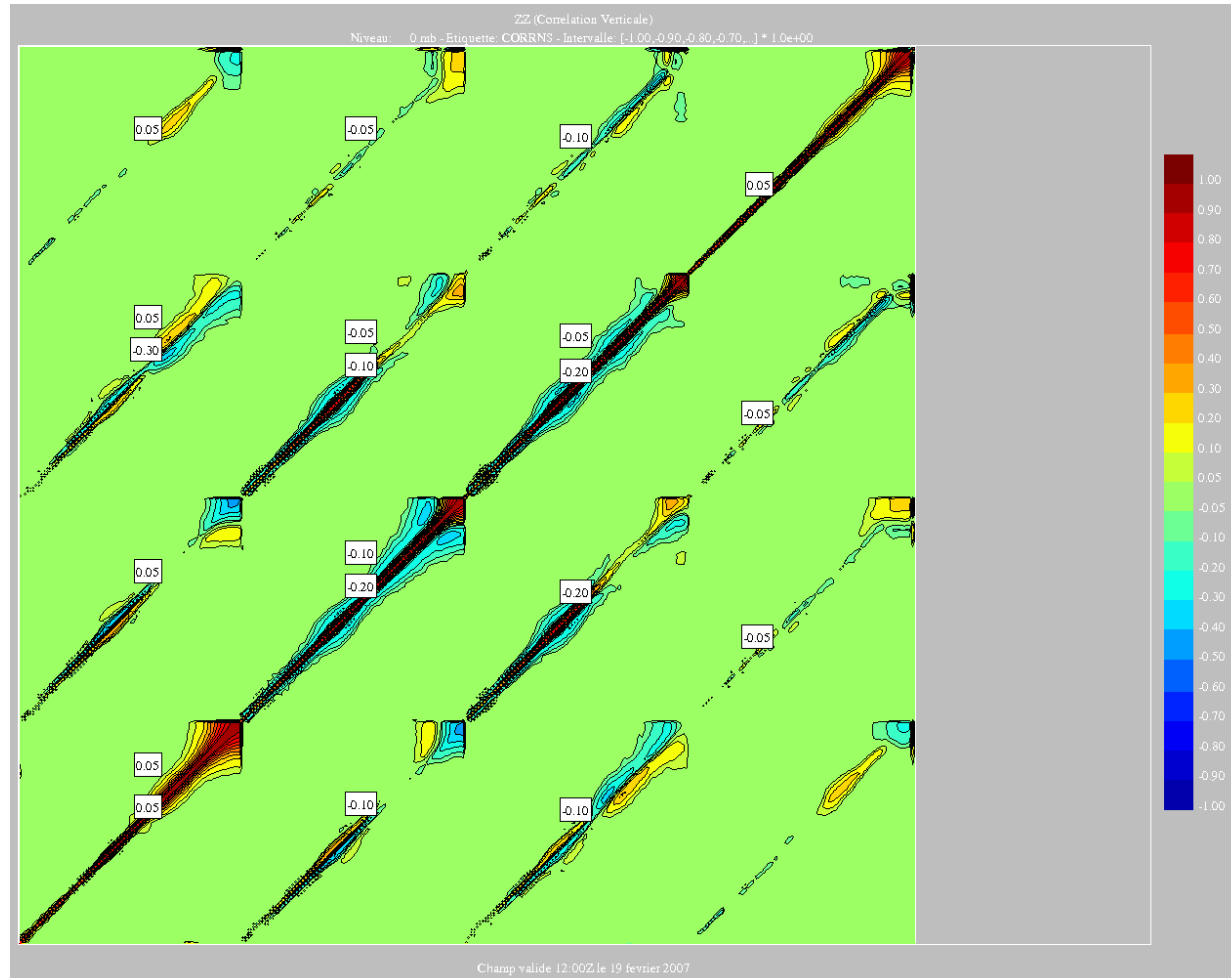
Southern-Hemisphere: Spectral-Hemispheric-50 km: T-300: 720x360; NMC-24-48: Winter 2007-Oper.Strato-Jun-09

n = 20



Spectral-Hemispheric-50 km: T-300: 720x360; NMC-24-48: Winter 2007-Oper.Strato-Jun-09

n = 100



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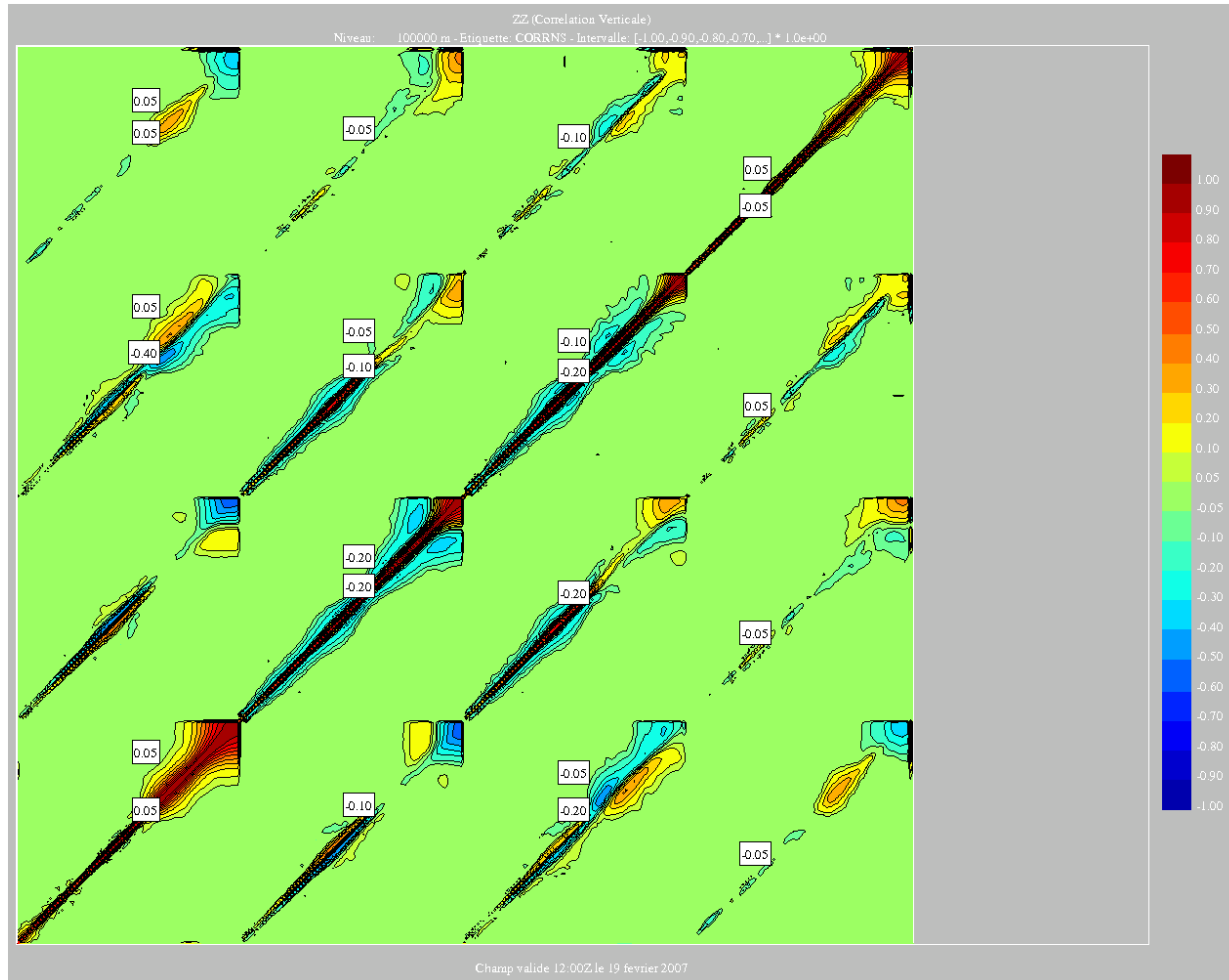
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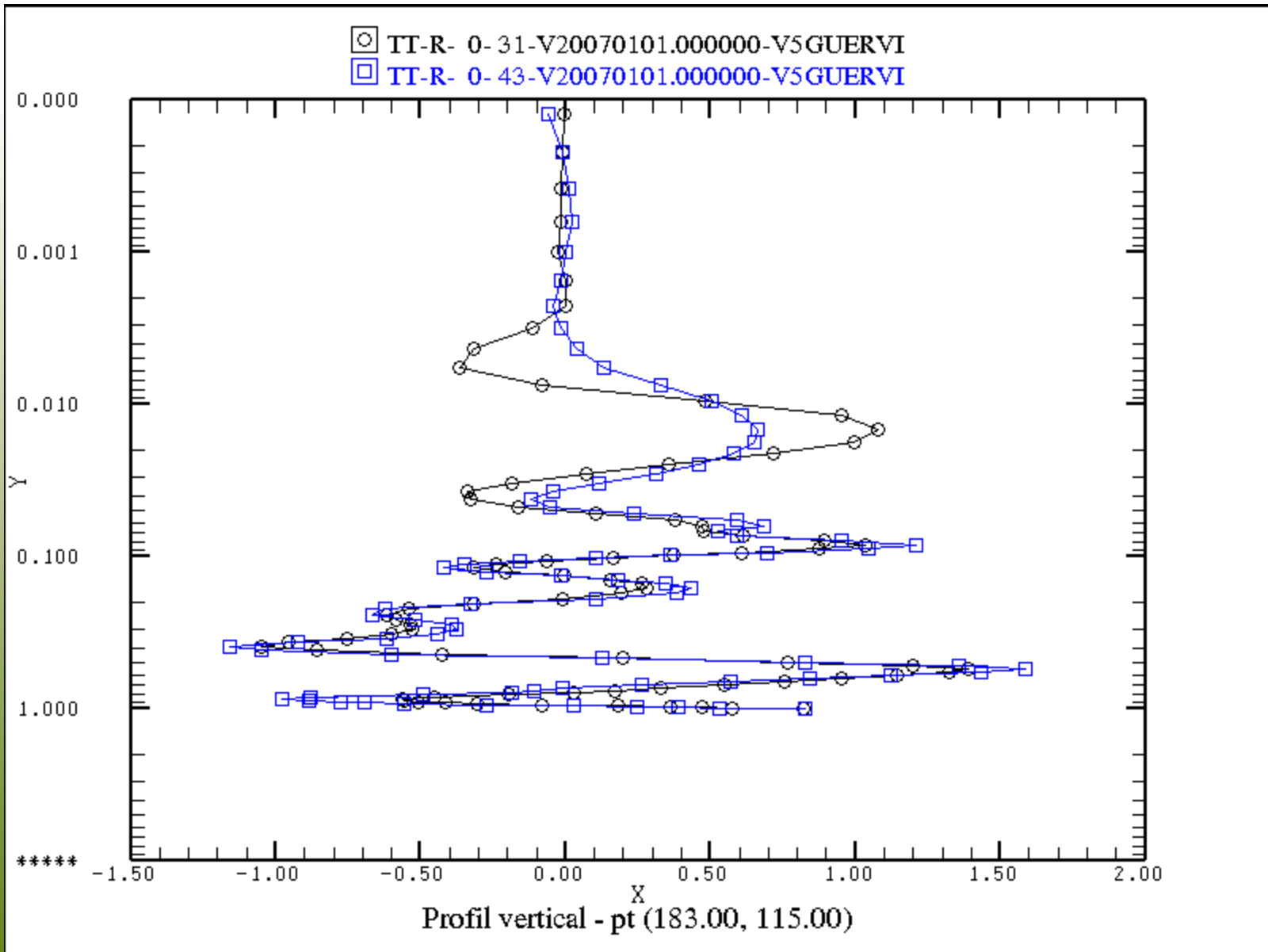
REG-LAM3D-55 km

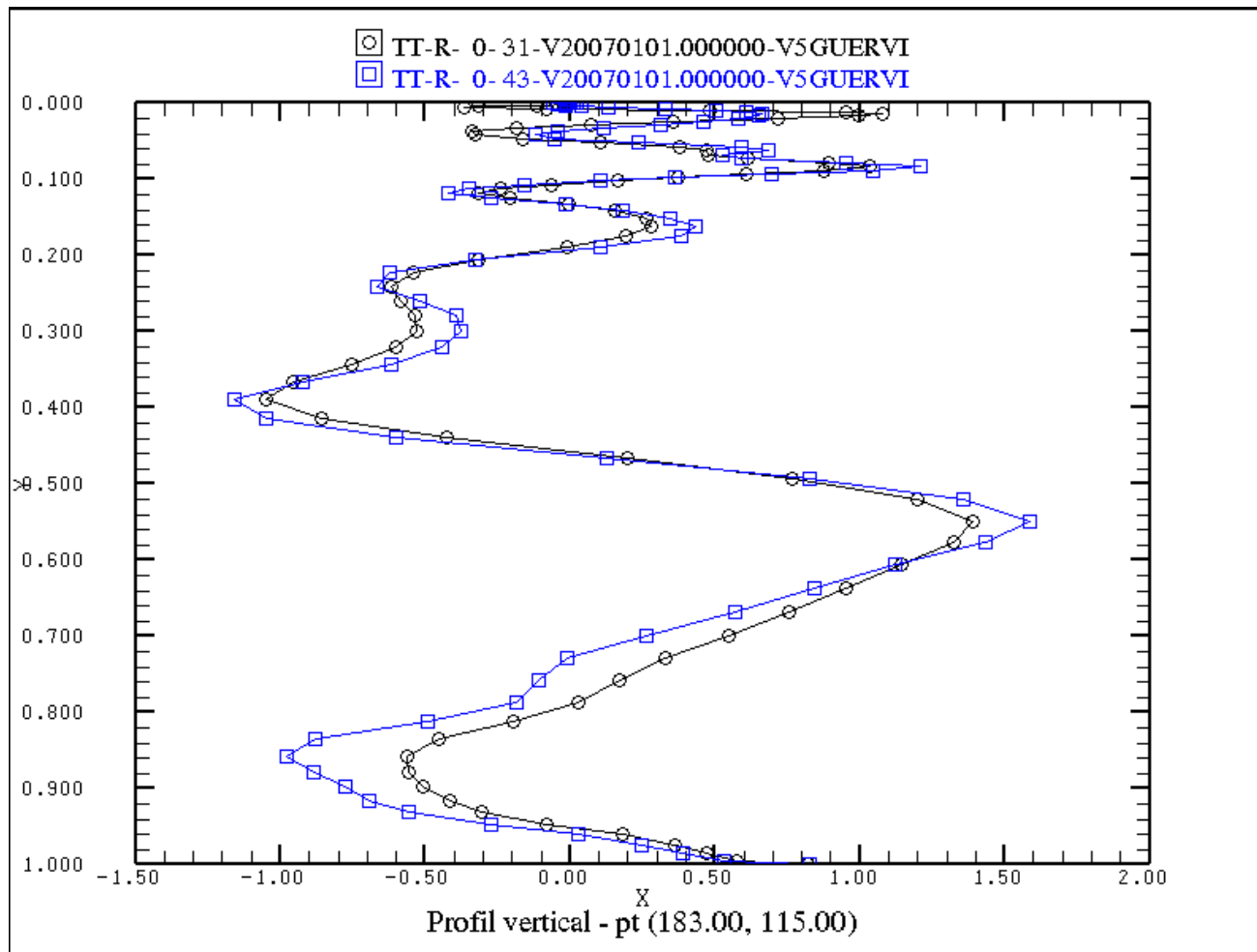
DFT-2D-100: 250x250;

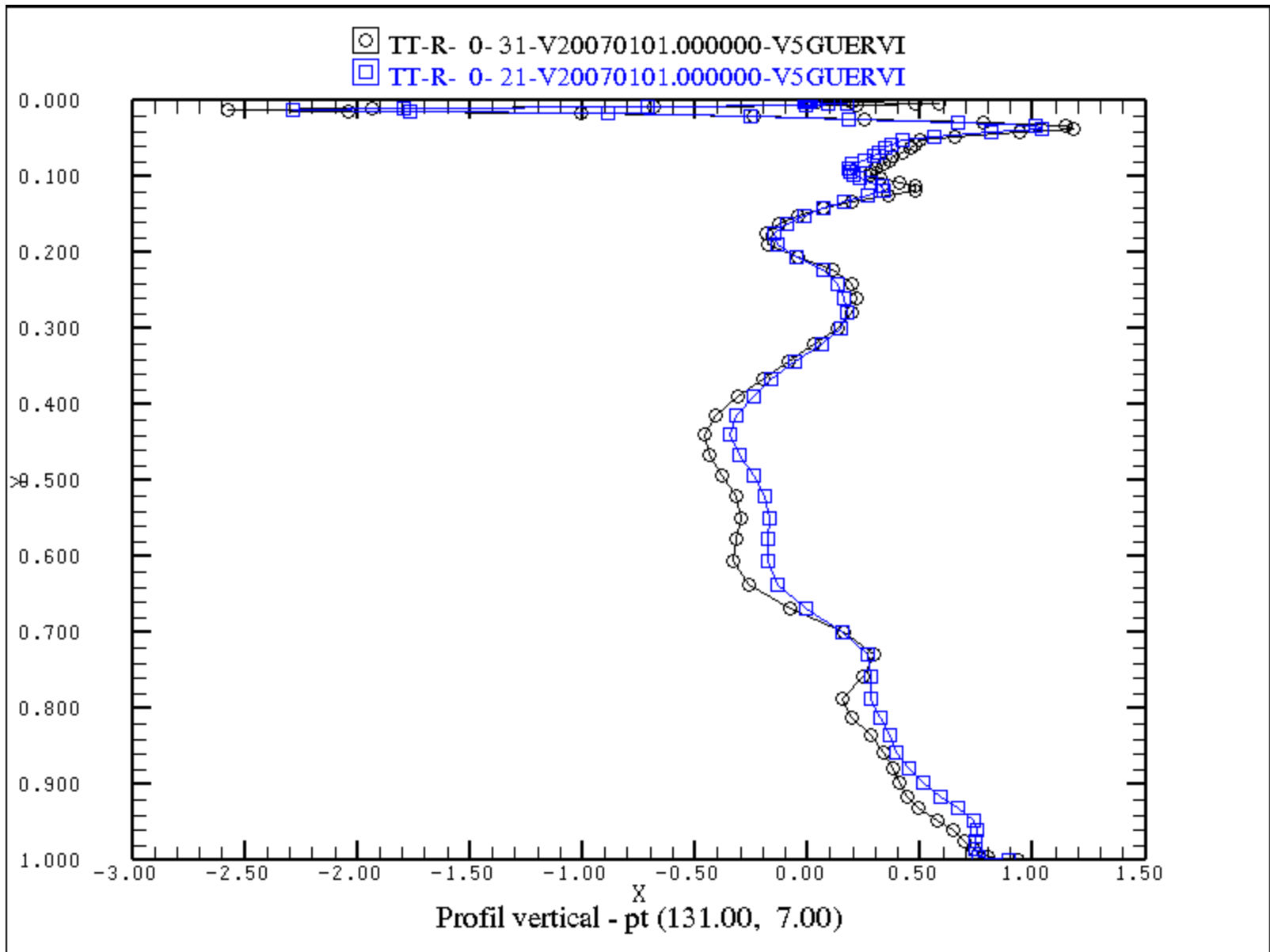
NMC-24-48: Winter 2007-Oper.Strato-Jun-09

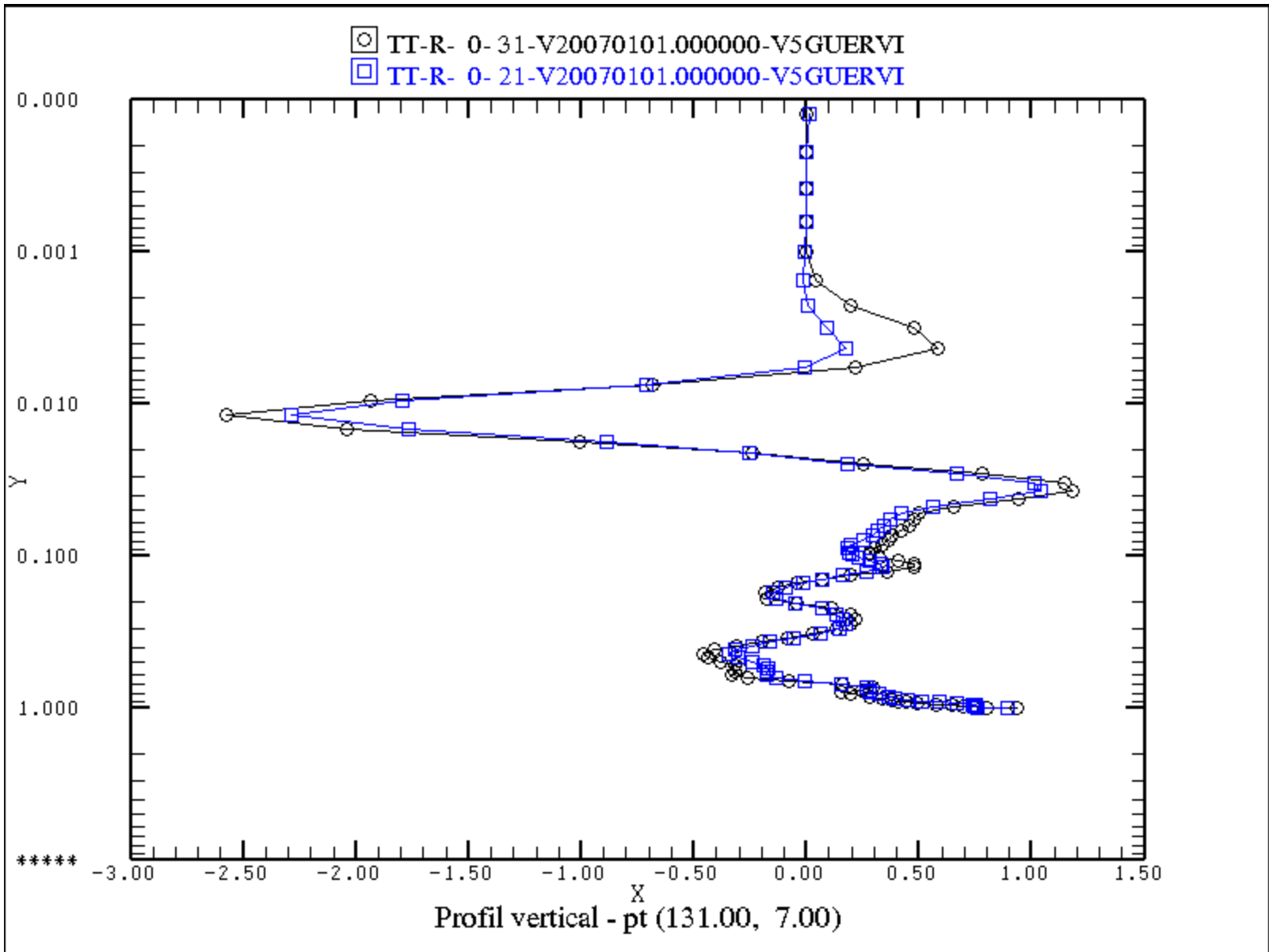
k = 25



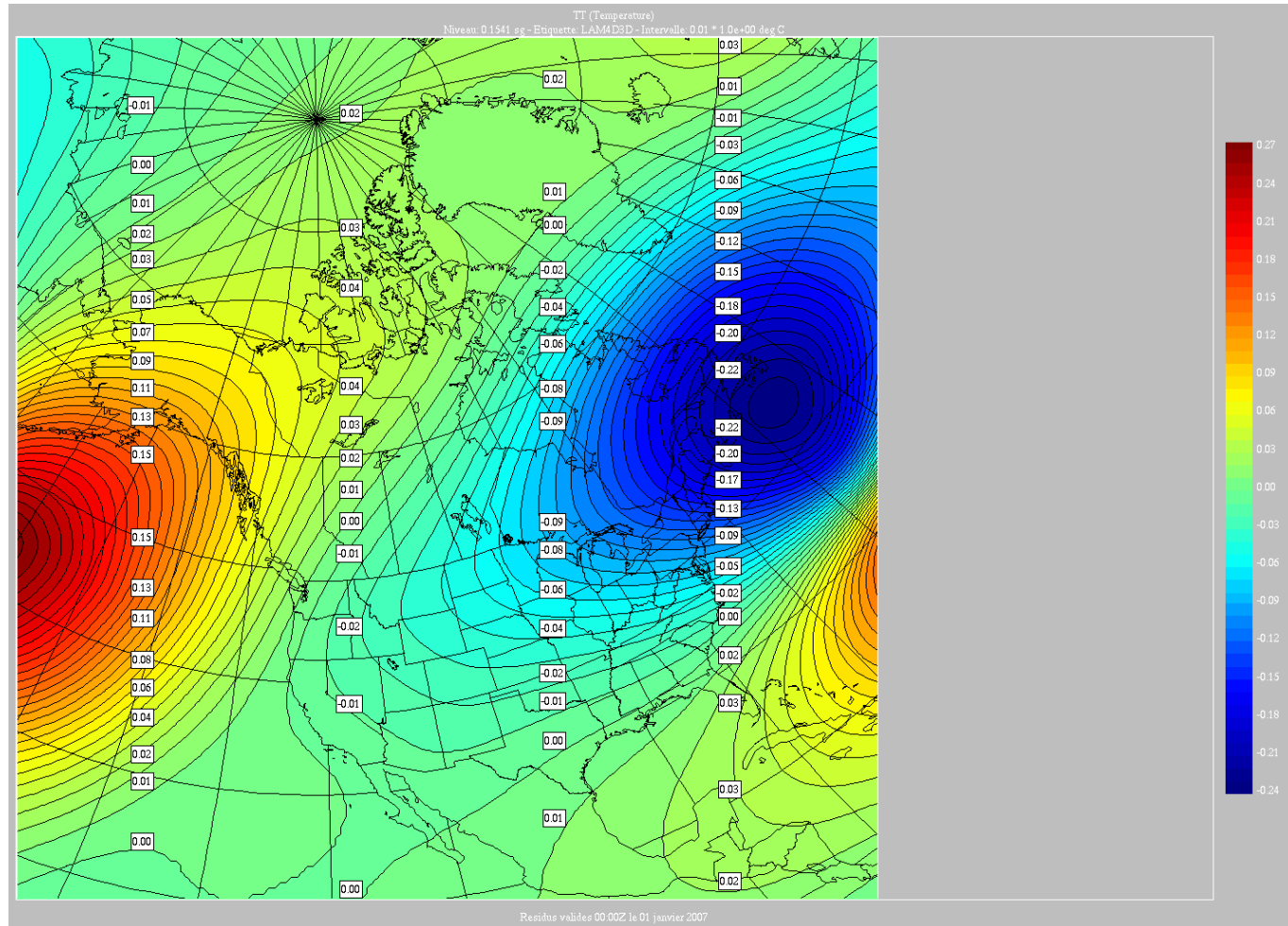








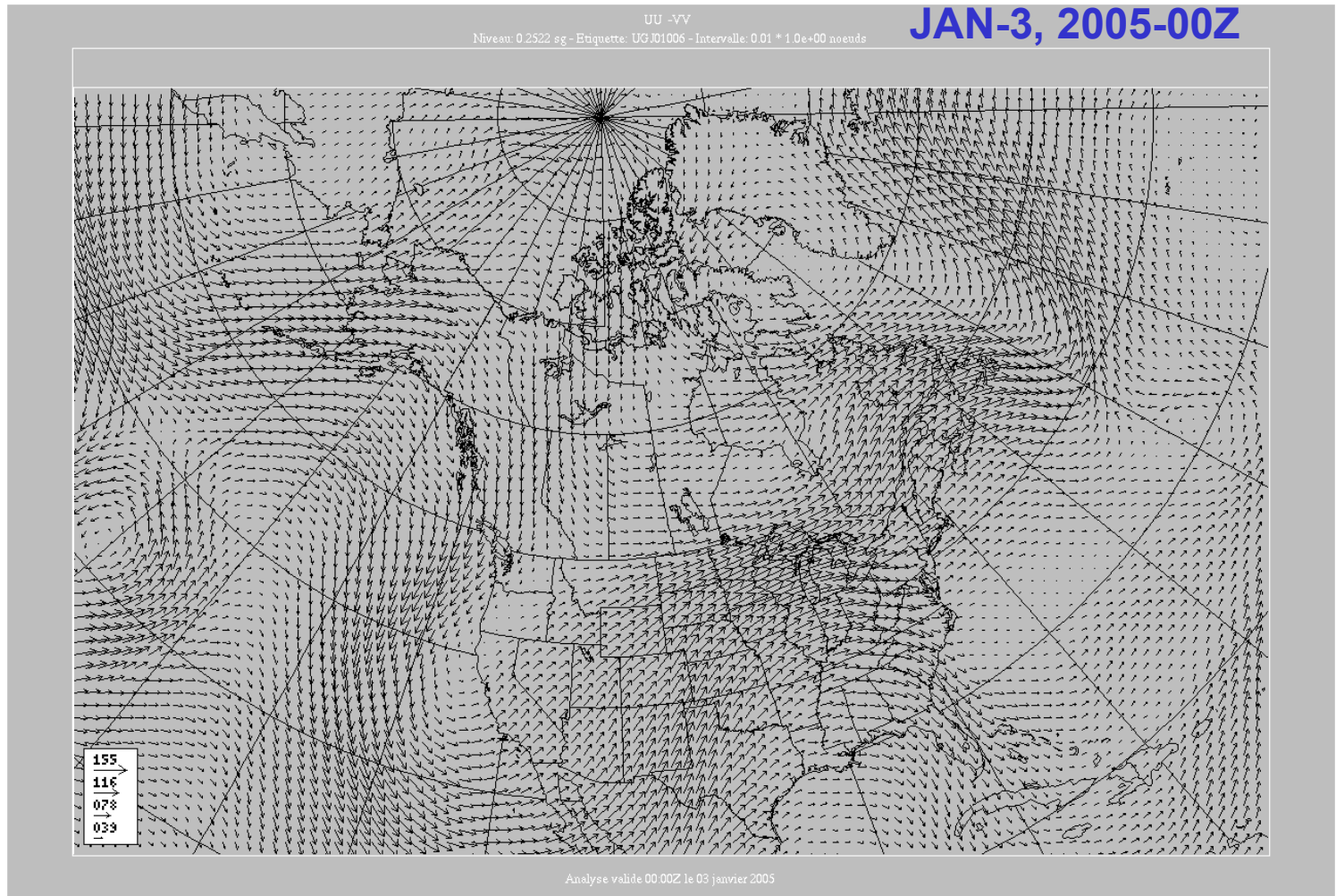
**Insufficient 20 % extension of the core NLM grid for DFT-2D:
Streamfunction correlation scale at 100 hPa = 2000 km !
→ 40 % required. For kilometric-Lam, use correlation-scale
criteria also....**



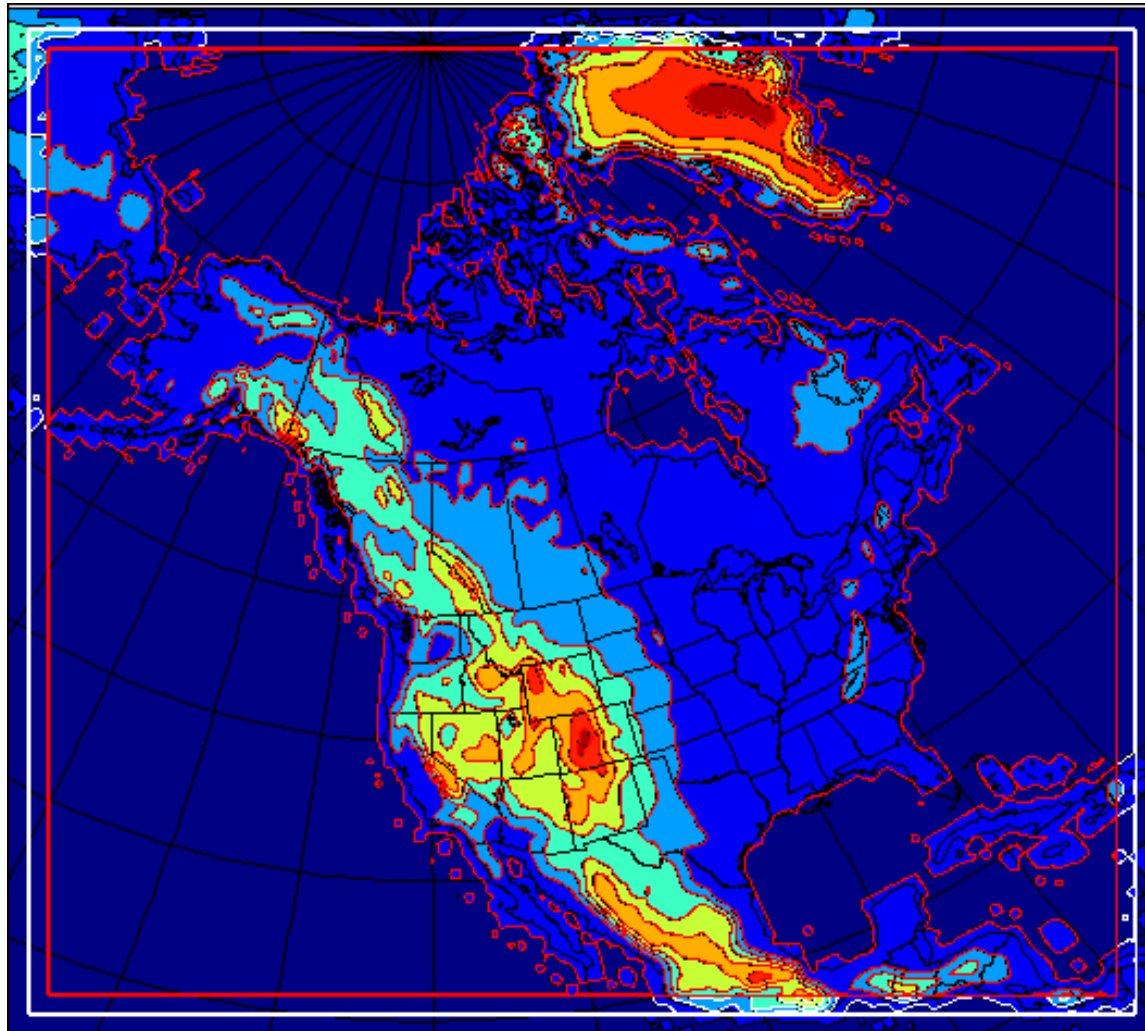
Original REG-LAM grid

Winter jet pushing far south to the wall

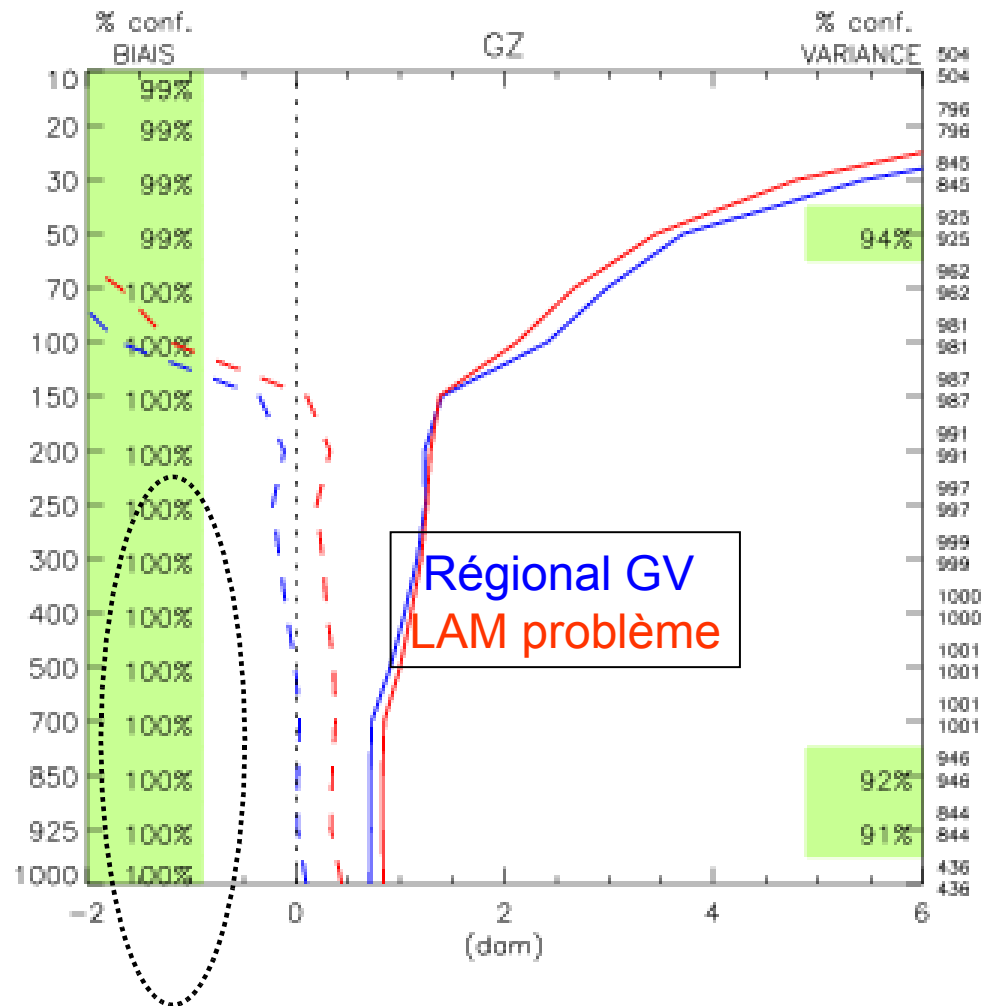
→ Push southern boundary further South.



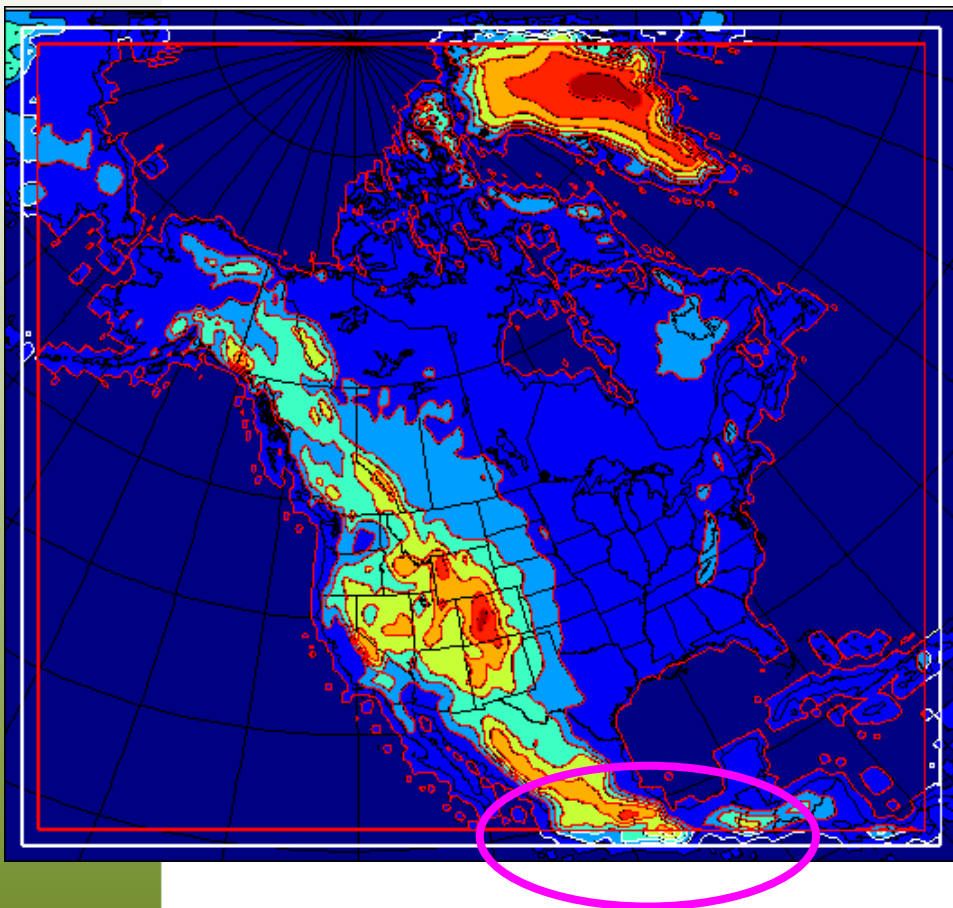
Problème du biais du géopotentiel du LAM nord-américain : Impact du positionnement de la zone de blending



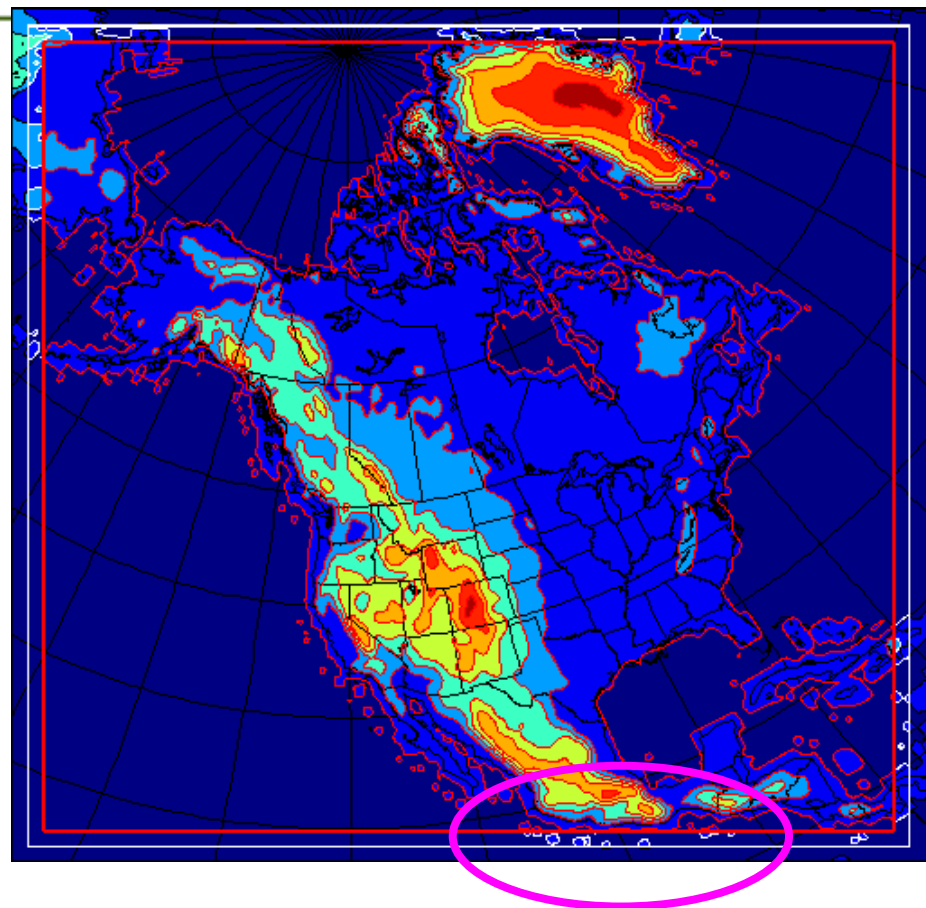
Prévision de 12 heures: moyenne 13 cas Région: Amérique du nord



La correction a été d'éloigner la frontière sud de la chaîne de montagne Sierra Madre del Sur

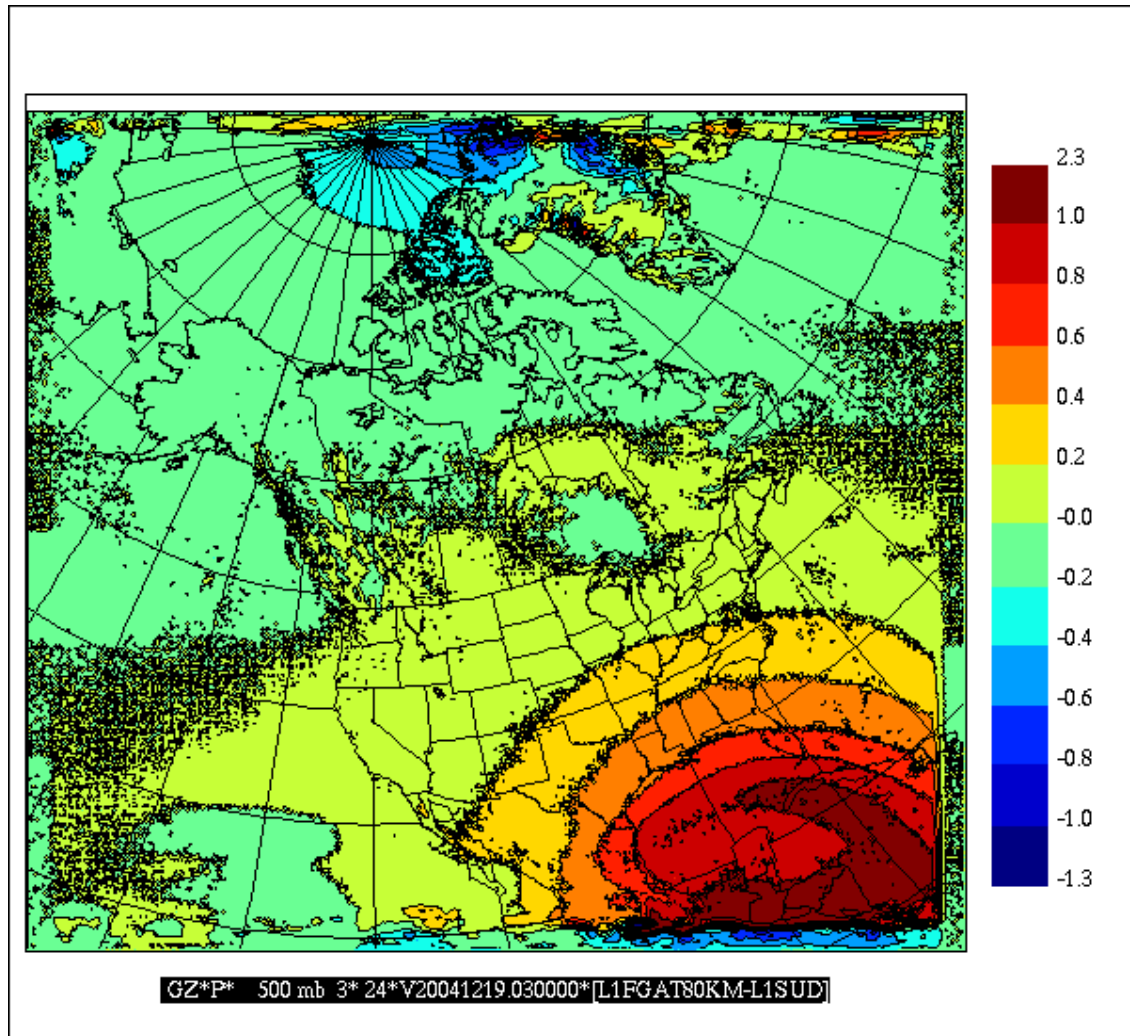


Ancien domaine

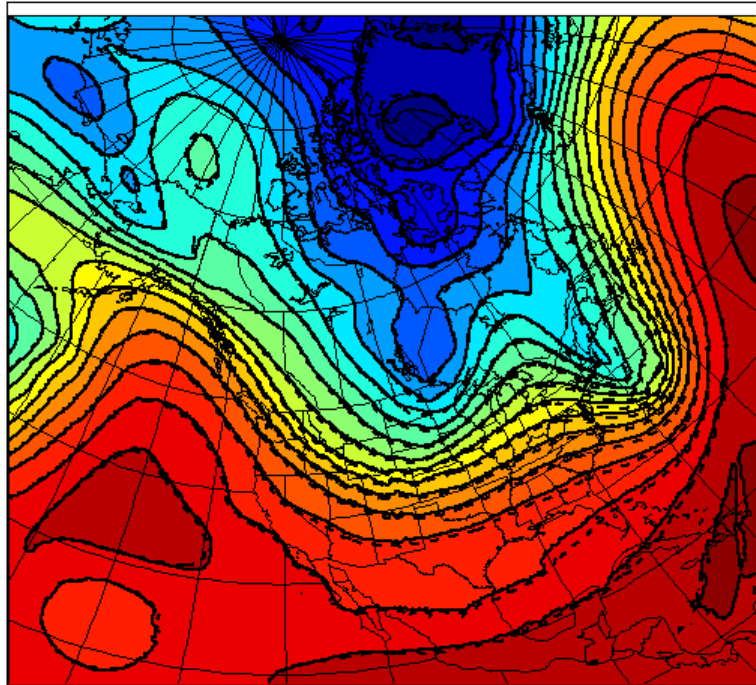


Nouveau domaine

Cas typique: 19 décembre prévision de **3 heures**
Différence GZ 500 mb (dam)

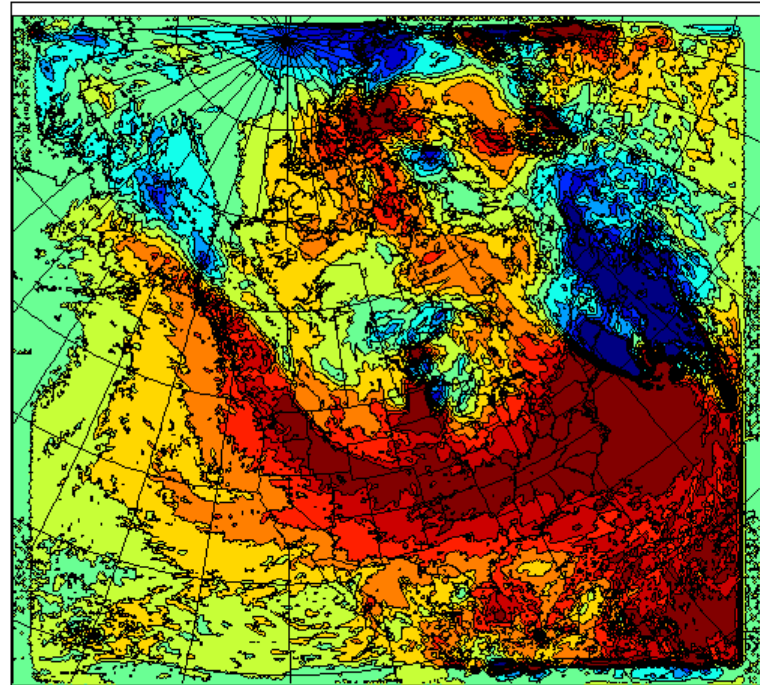


Cas typique: 19 décembre prévision de 48 heures



P- 500 mb-48-384-V20041221.000000-L1FGA | GZ-P- 500 mb-48-384-V20041221.000000-L1SUD

GZ 500 mb (dam)



GZ*P* 500 mb 48*384*V20041221.000000*[L1FGAT80KM-L1SUD]

Différence GZ 500 mb (dam)

Expérience originale: trait continu

Expérience avec frontière plus au sud: trait discontinu

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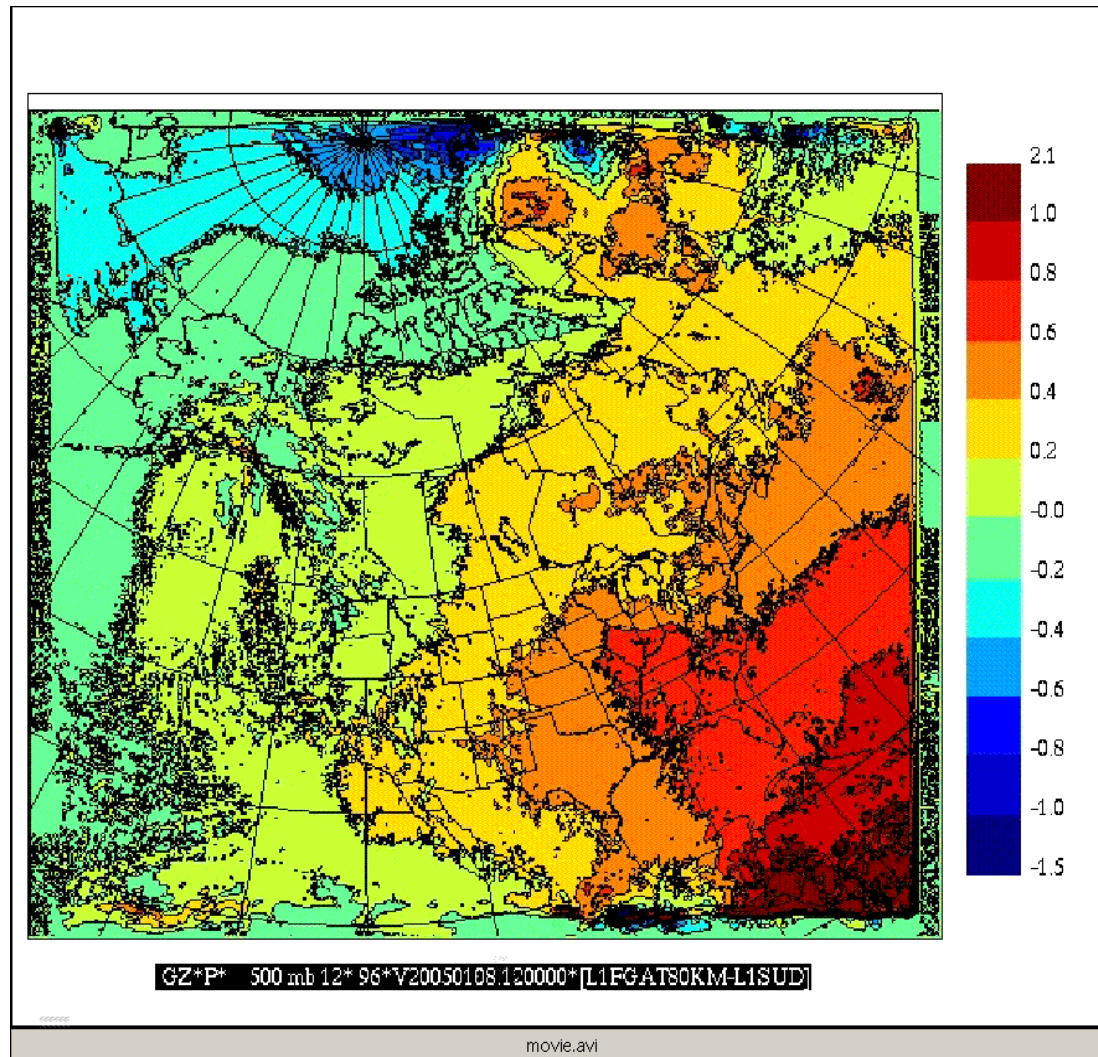
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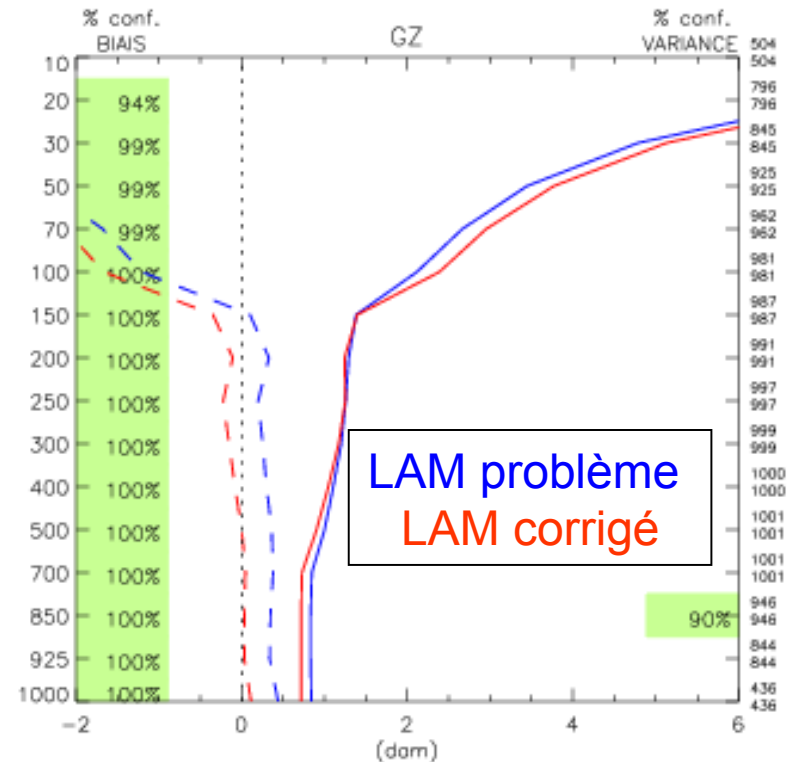
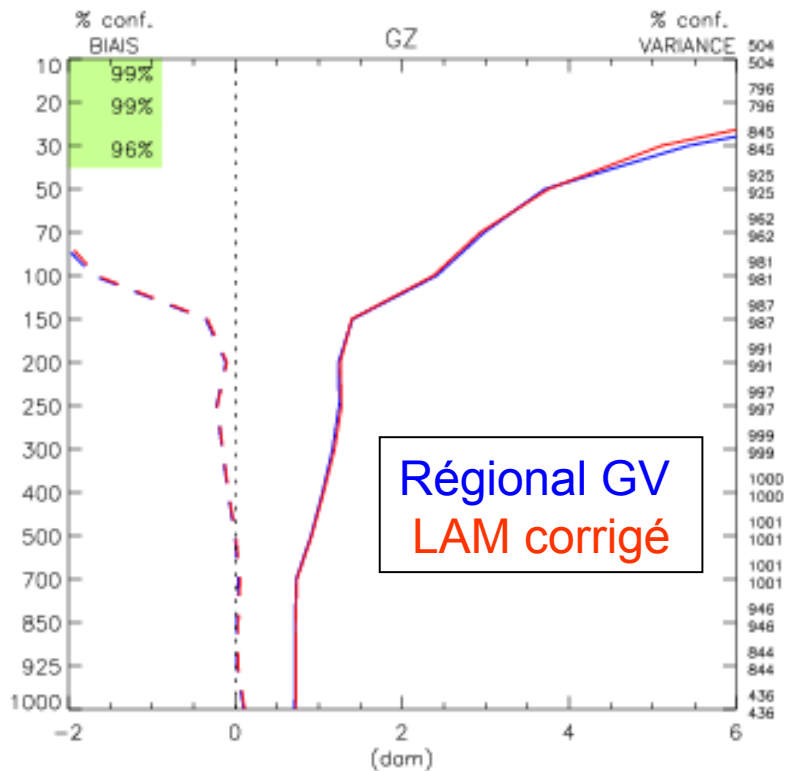
Différences GZ 500 (dam) prévisions 12h

Animation de 13 cas d'hiver montrés séparément

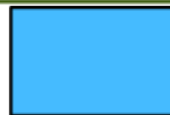
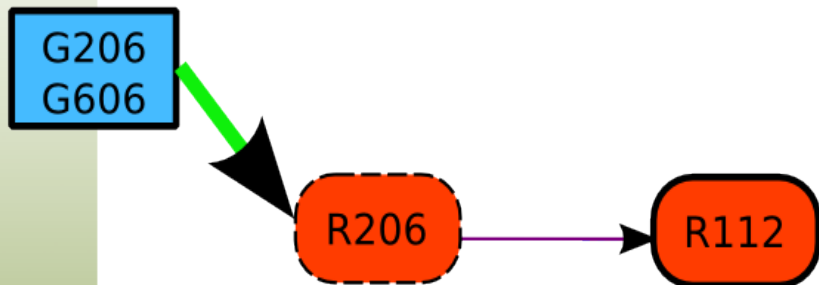


Correction du problème de biais du géopotentiel du LAM: effet sur le biais du GZ lorsque l'on éloigne la frontière sud de la chaîne des montagnes Sierra Madre

Prévision de 12 heures: moyenne 13 cas
Région: Amérique du nord



Spin-up Régional



Modèle Global 33 km



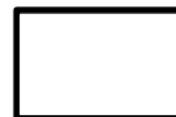
Modèle Régional 15 km



Analyse non produite



Analyse 3D-VAR FGAT



Analyse 4D-VAR



Pilote

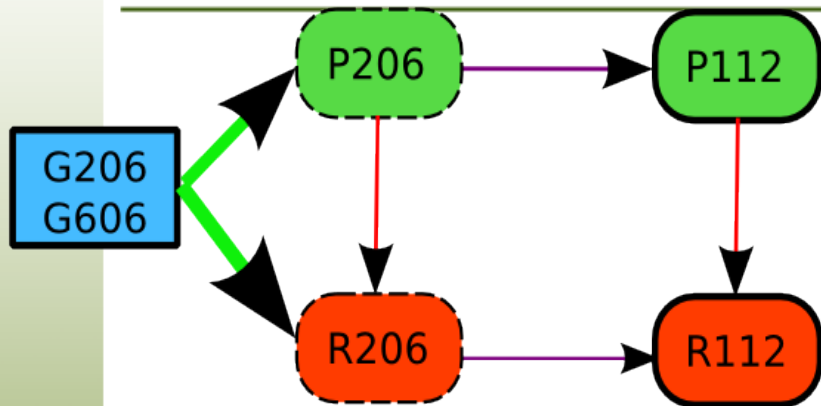





Champ d'essai








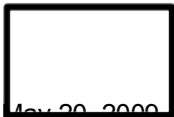
Analyse globale

Spin-up REG-LAM3D

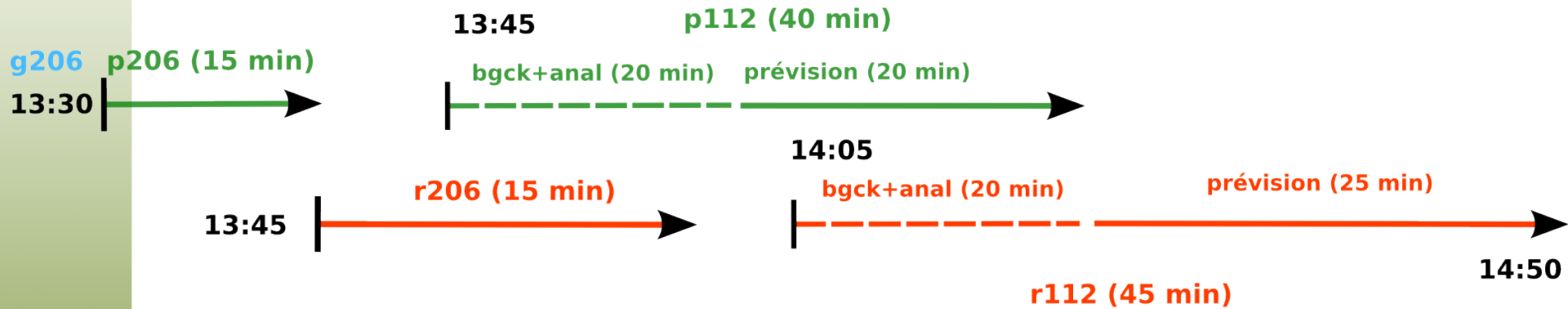


	Modèle Global 33 km
	Modèle Global 55 km
	Modèle LAM 15 km

	Pilote
	Champ d'essai
	Analyse globale

	Analyse non produite
	Analyse 3D-VAR FGAT
	Analyse 4D-VAR

Timings⁺

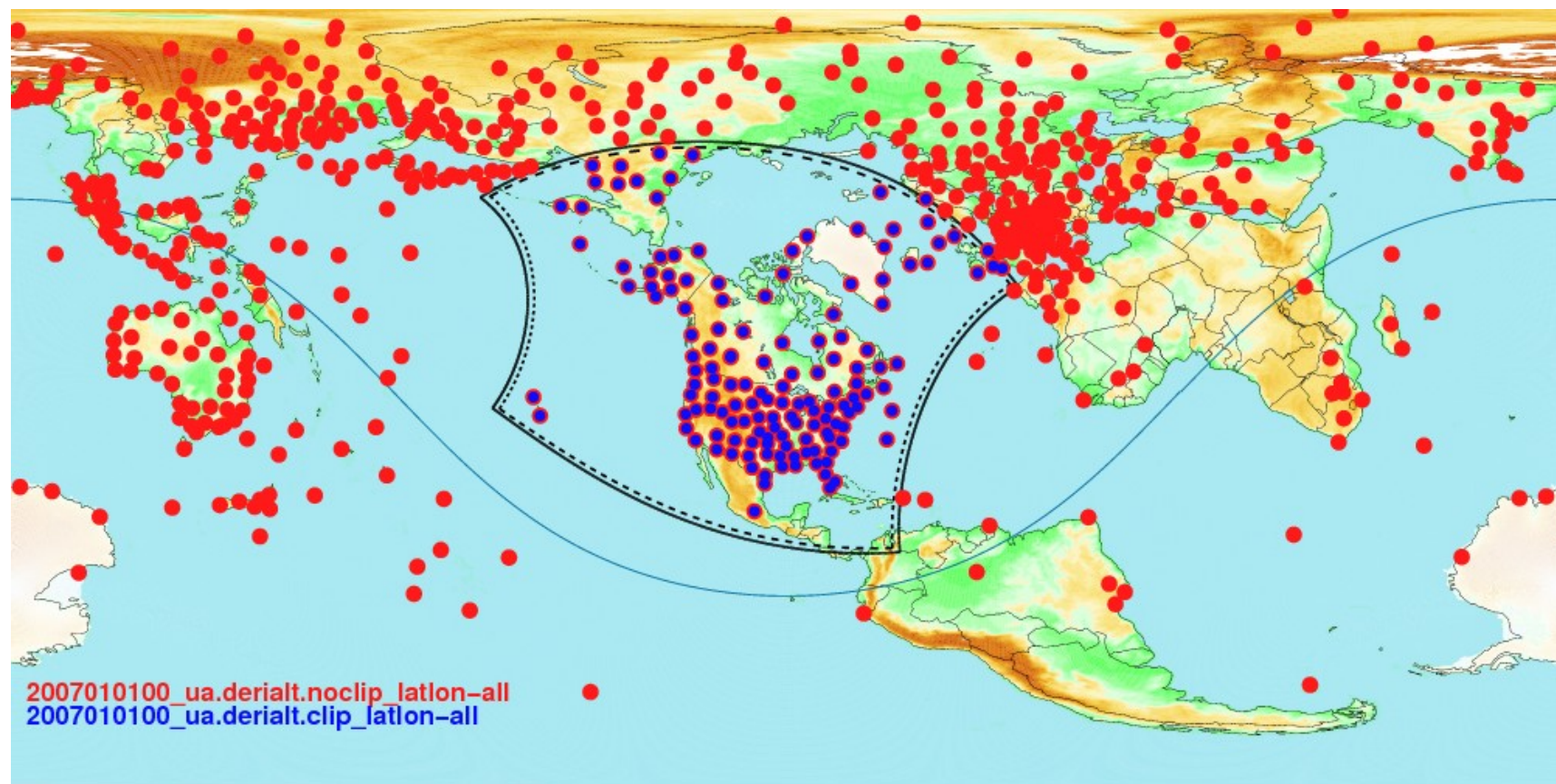


Le régional actuel sort à 14h45

	Modèle Global 33 km
	Modèle Global 55 km
	Modèle LAM 15 km

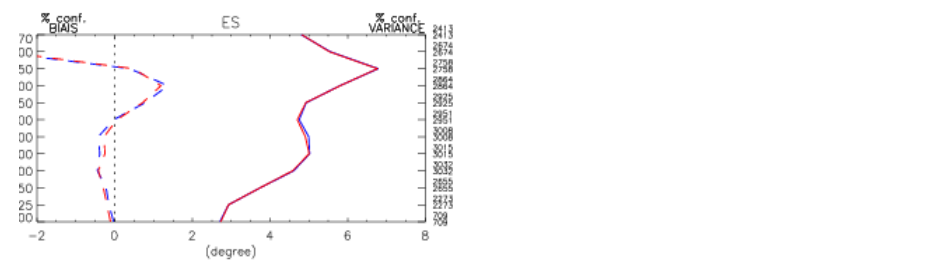
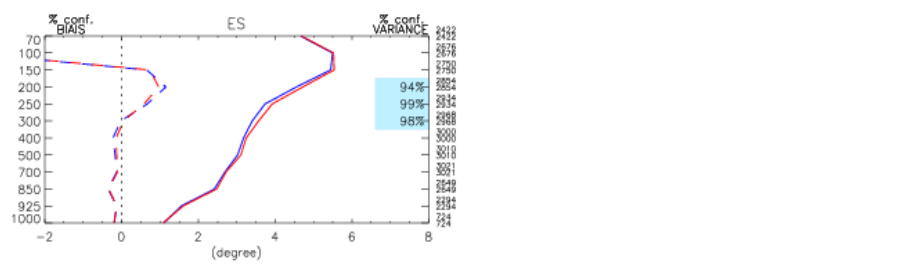
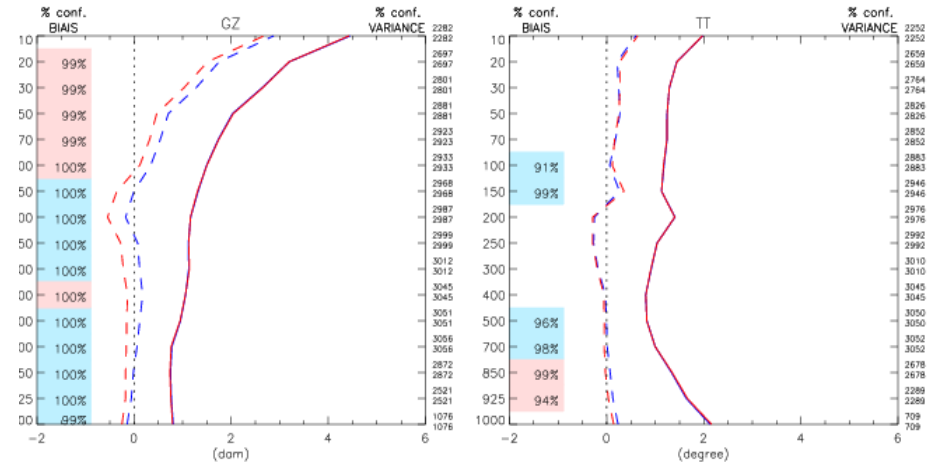
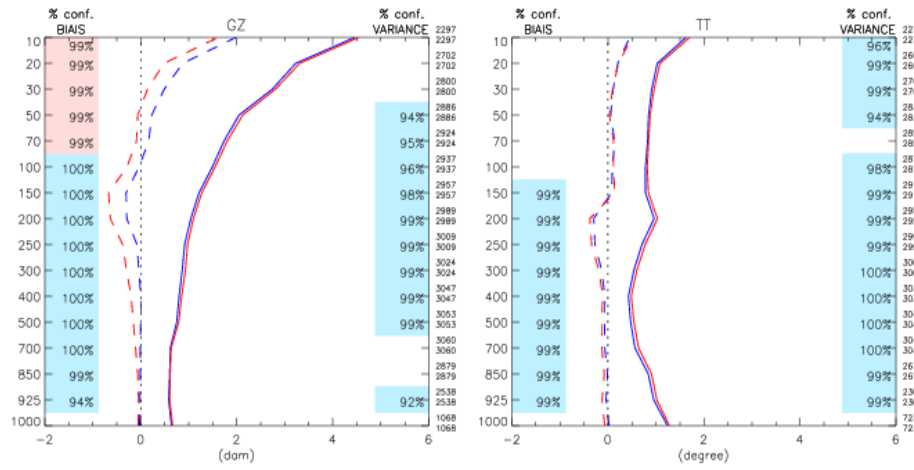
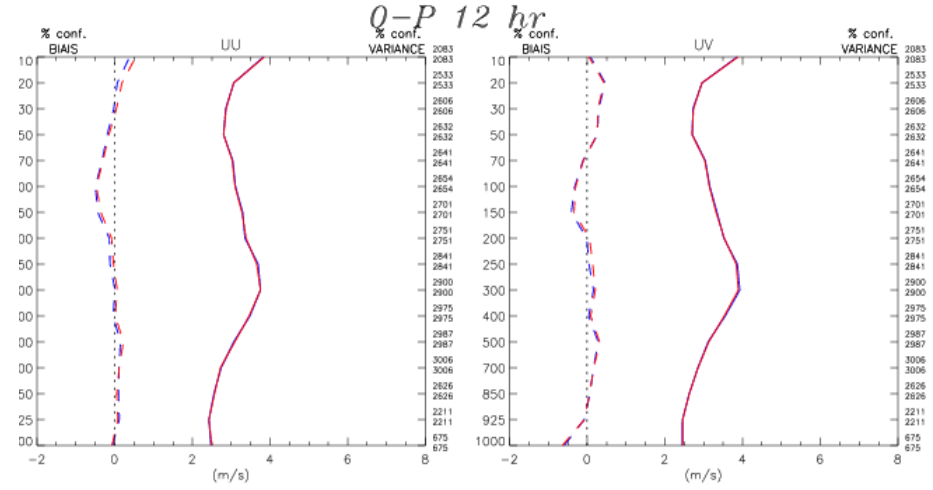
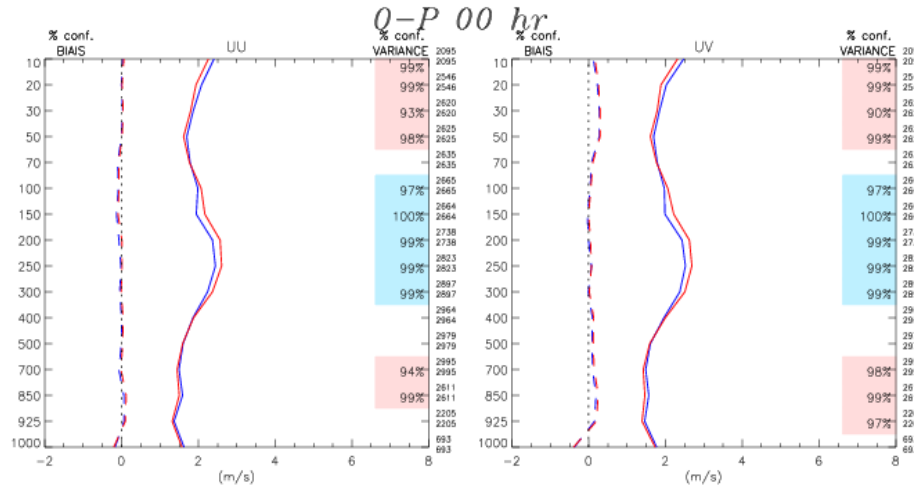
Clipping des observations

Combinaison de BURP2RDB et d'un programme C pour filtrer les observations hors du domaine REG-LAM3D



Évaluations

- 40 cas de l'hiver 2007 (1er janvier au 28 février 2007) à toutes les 36 hrs
- Régional Strato (ZDA41)
- REG-LAM3D (lam3d_hiv_hemis_bgcklam)
(ce système sera proposé au CPOP du 7 juillet)
- mêmes observations et même résolution de thinning (e.g. 250km pour les obs. satellitaires)
 - thinning 3D pour REG
 - thinning 4D pour REG-LAM3D



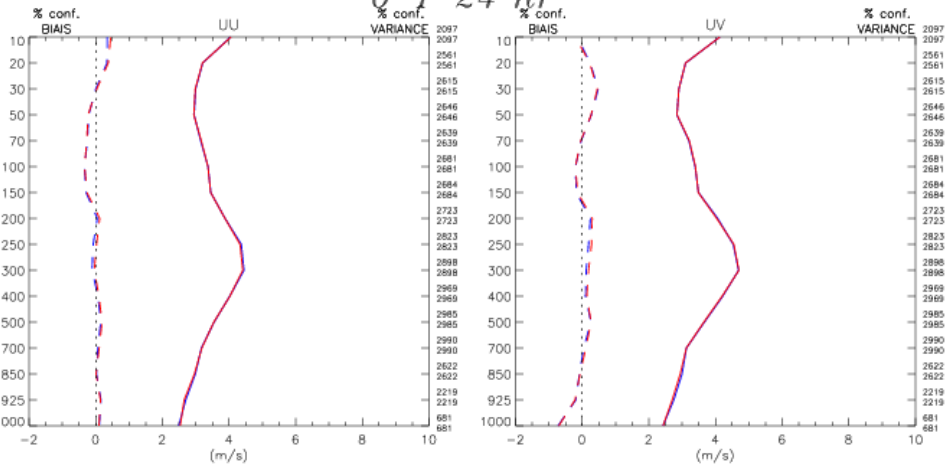
◆ E-T m_uo_04B_regzda41 (40)
 □ BIAS m_uo_04B_regzda41
 ◆ E-T m_uo_04B_lamlam3d_hiv_hemis_bgcklam (40)
 □ BIAS m_uo_04B_lamlam3d_hiv_hemis_bgcklam

Type : 0-P 00 hr
Region : Amerique du Nord LAM
Lat-lon: (30N, 150W) (73N, 50W)
Stat. communes

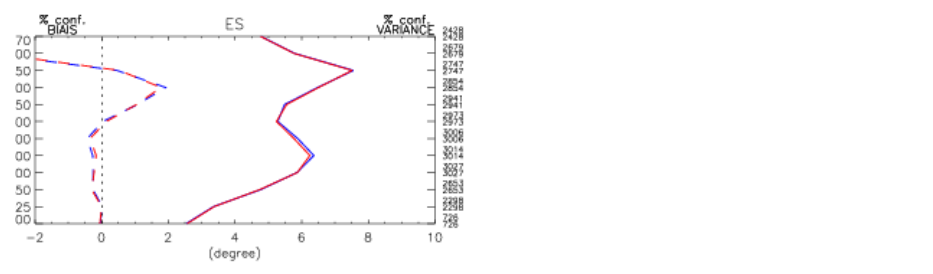
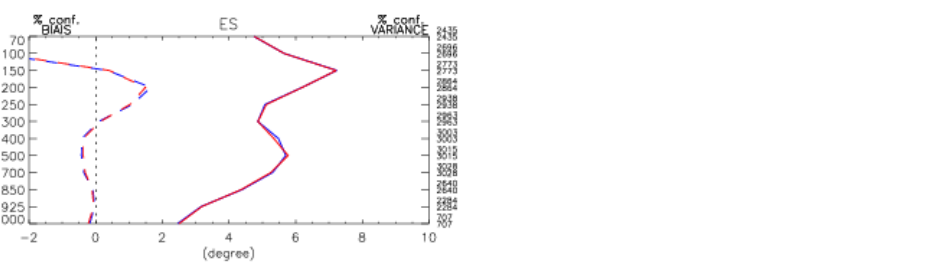
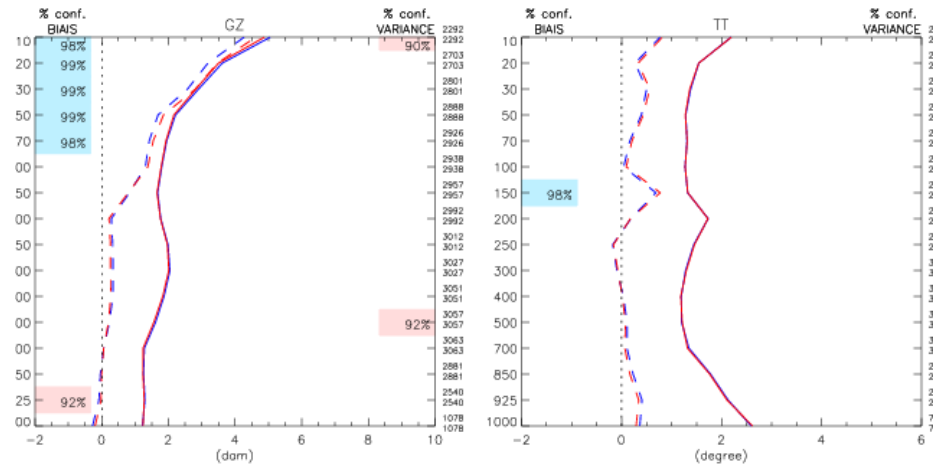
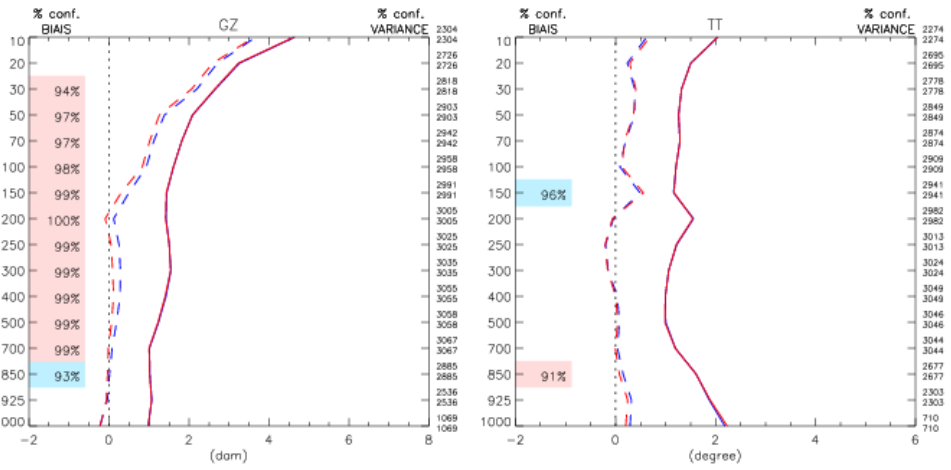
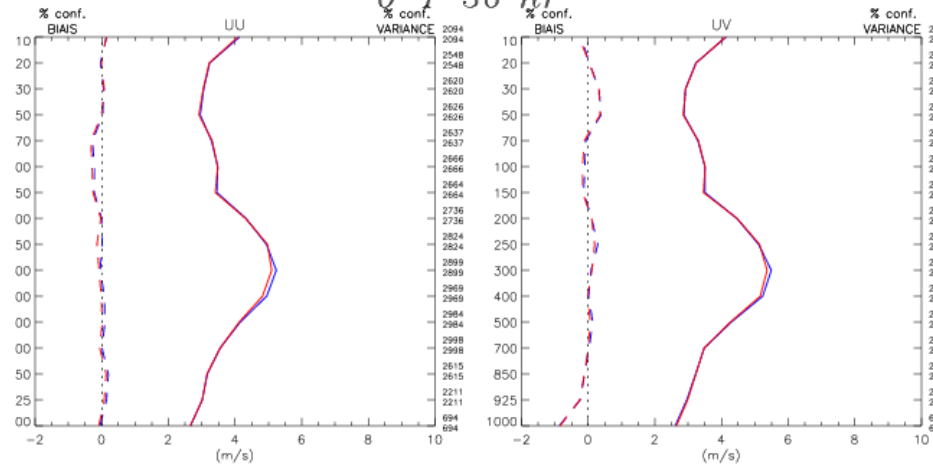
◆ E-T m_uo_04B_regzda41 (40)
 □ BIAS m_uo_04B_regzda41
 ◆ E-T m_uo_04B_lamlam3d_hiv_hemis_bgcklam (40)
 □ BIAS m_uo_04B_lamlam3d_hiv_hemis_bgcklam

Type : 0-P 12 hr
Region : Amerique du Nord LAM
Lat-lon: (30N, 150W) (73N, 50W)
Stat. communes

0-P 24 hr



0-P 36 hr



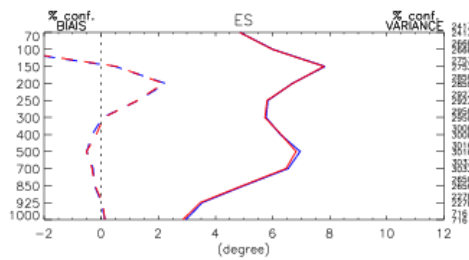
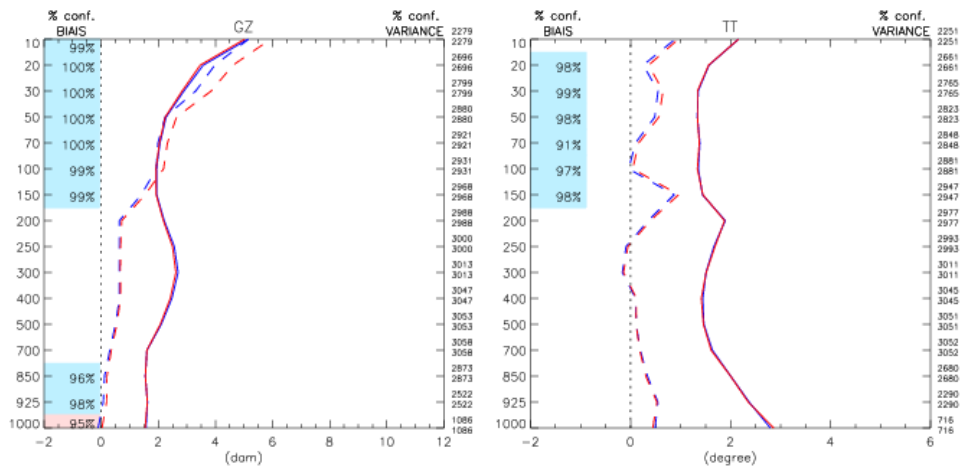
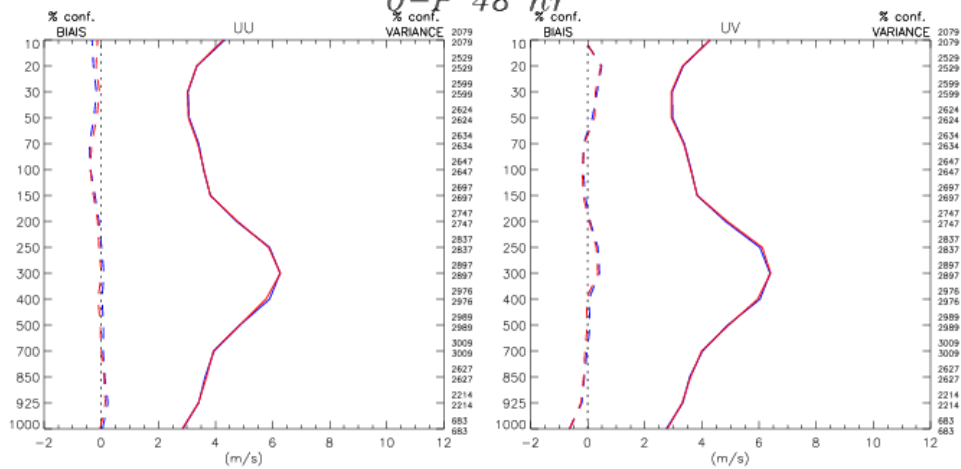
Type : 0-P 24 hr
 Region : Amerique du Nord LAM
 Lat-lon: (30N, 150W) (73N, 50W)
 Stat. communes

— E-T m_ua_048_regzda41 (40)
- - - BIAS m_ua_048_regzda41
— E-T m_ua_048_lamlam3d_hiv_hemis_bgcklam (40)
- - - BIAS m_ua_048_lamlam3d_hiv_hemis_bgcklam

Type : 0-P 36 hr
 Region : Amerique du Nord LAM
 Lat-lon: (30N, 150W) (73N, 50W)
 Stat. communes

— E-T m_ua_048_regzda41 (40)
- - - BIAS m_ua_048_regzda41
— E-T m_ua_048_lamlam3d_hiv_hemis_bgcklam (40)
- - - BIAS m_ua_048_lamlam3d_hiv_hemis_bgcklam

0-P 48 hr



• https://wiki/wiki/REG-LAM3D/Ervig/Description_des_suites_

◇	—	E-T m_ua_048_regzda41 (40)
◇	- - -	BIAS m_ua_048_regzda41
◇	—	E-T m_ua_048_lamlam3d_hiv_hemis_bgcklam (40)
◇	- - -	BIAS m_ua_048_lamlam3d_hiv_hemis_bgcklam

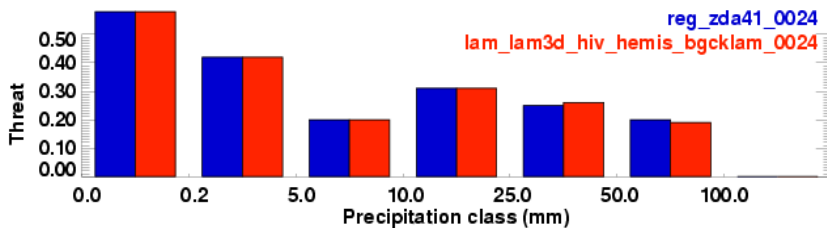
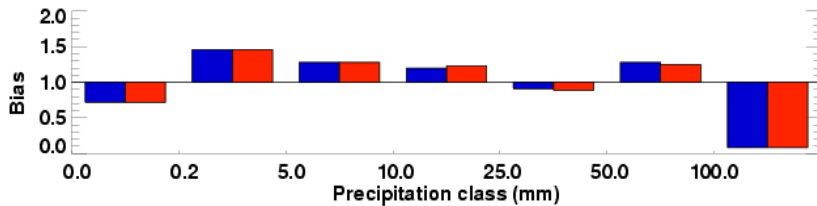
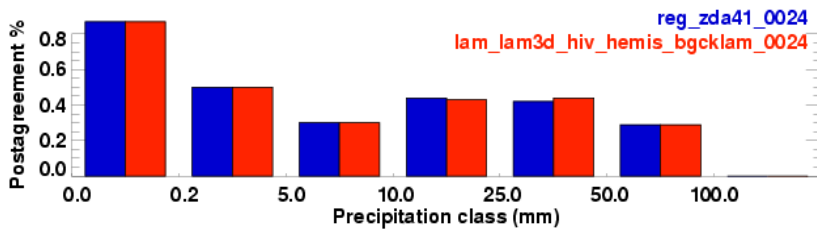
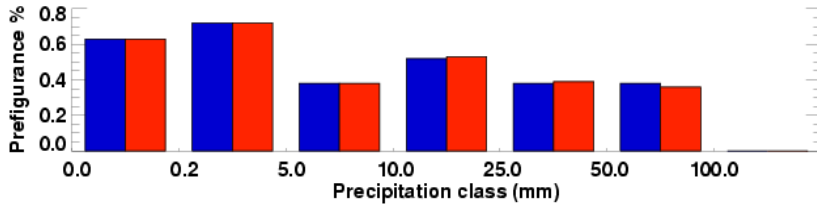
Type : 0-P 48 hr
 Region : Amerique du Nord LAM
 Lat-lon: (30N, 150W) (73N, 50W)
 Stat. communes

ly 20, 2009



24 hours precipitation forecast verification against observation

Synoptic network data for valid time 00-12z
00 to 24 hours forecast North AMERICA
hiv2007



Number of observation

16166	8629	1230	944	328	61	13
16166	8629	1230	944	328	61	13

0.0 0.2 5.0 10.0 25.0 50.0 100.0

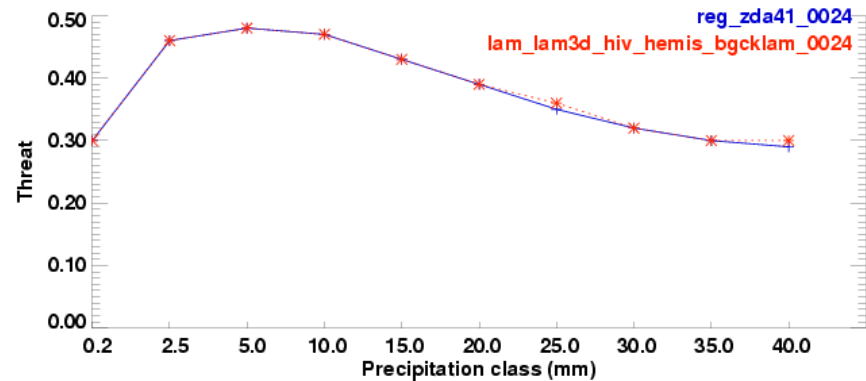
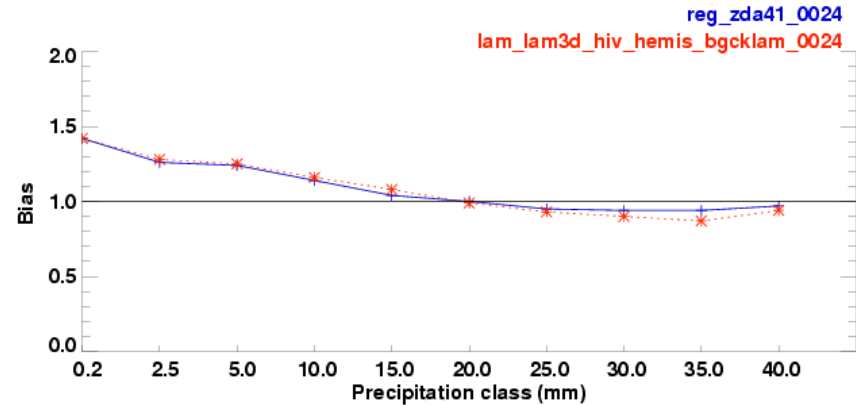


Environment
Canada

Environnement
Canada

24 hours precipitation forecast verification against observation

Synoptic network data for valid time 00-12z
00 to 24 hours forecast North AMERICA
hiv2007



Number of observation

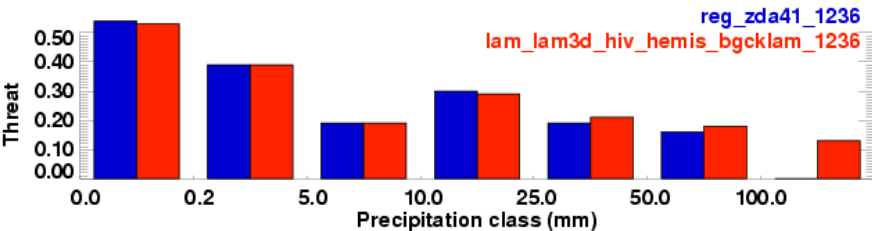
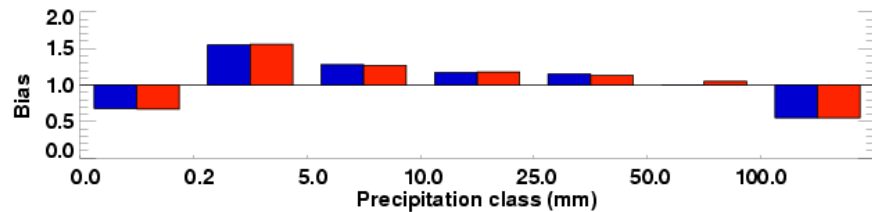
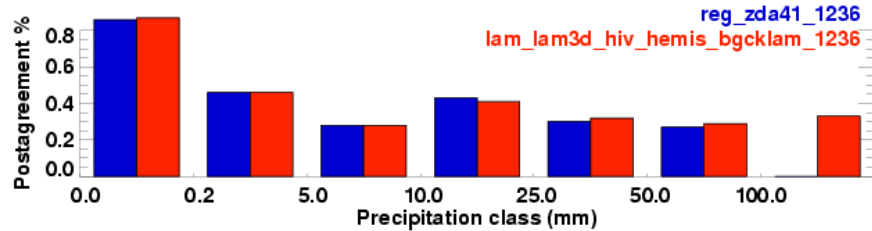
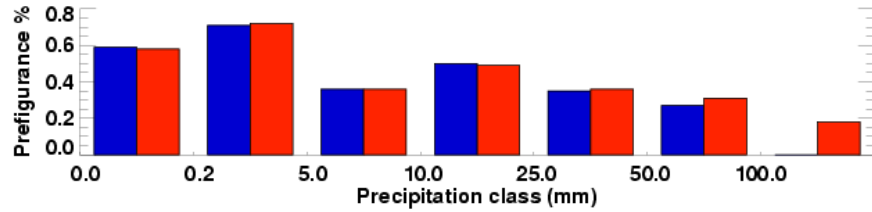
10929	4117	2483	1324	830	566	397	280	207	144
10929	4117	2483	1324	830	566	397	280	207	144

0.2 2.5 5.0 10.0 15.0 20.0 25.0 30.0 35.0 40.0



24 hours precipitation forecast verification against observation

Synoptic network data for valid time 00-12z
12 to 36 hours forecast North AMERICA
hiv2007



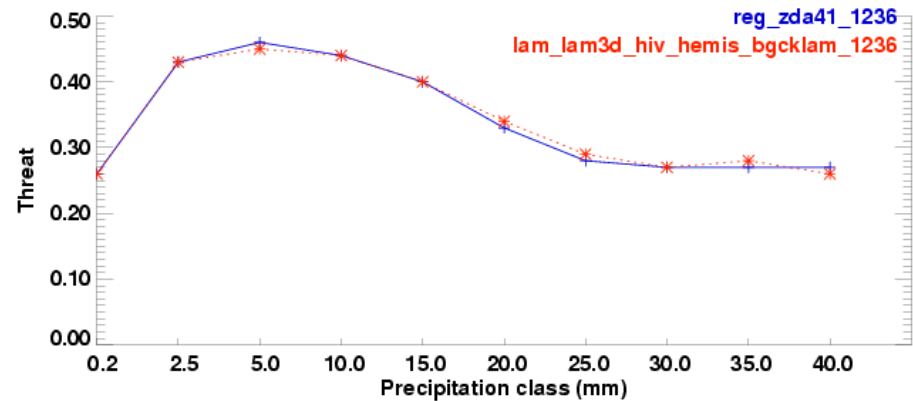
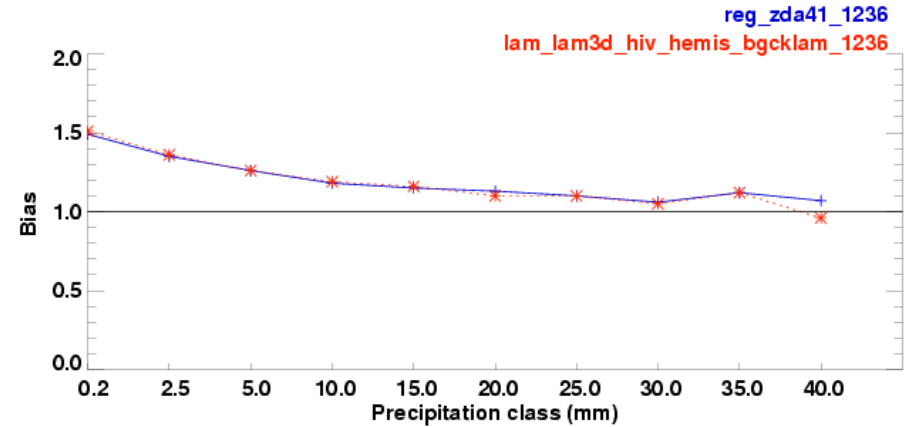
Number of observation

15873	8340	1272	963	266	62	11
15873	8340	1272	963	266	62	11

0.0 0.2 5.0 10.0 25.0 50.0 100.0

24 hours precipitation forecast verification against observation

Synoptic network data for valid time 00-12z
12 to 36 hours forecast North AMERICA
hiv2007



Number of observation

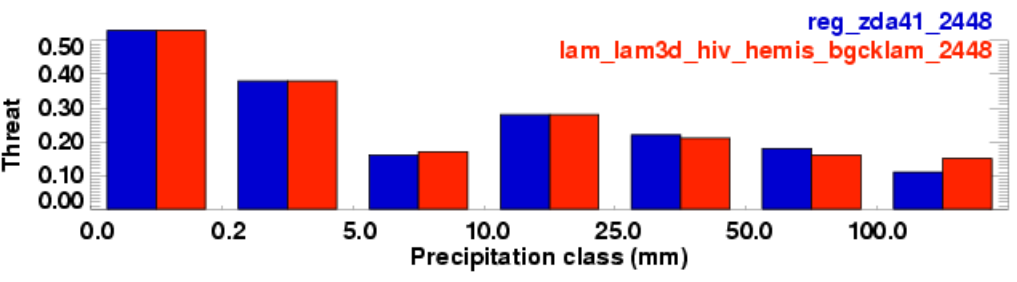
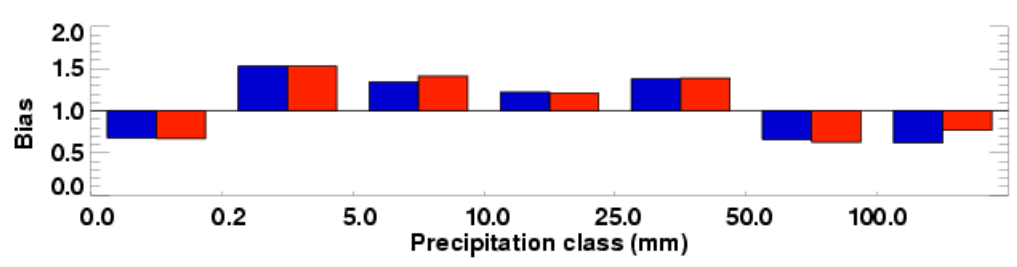
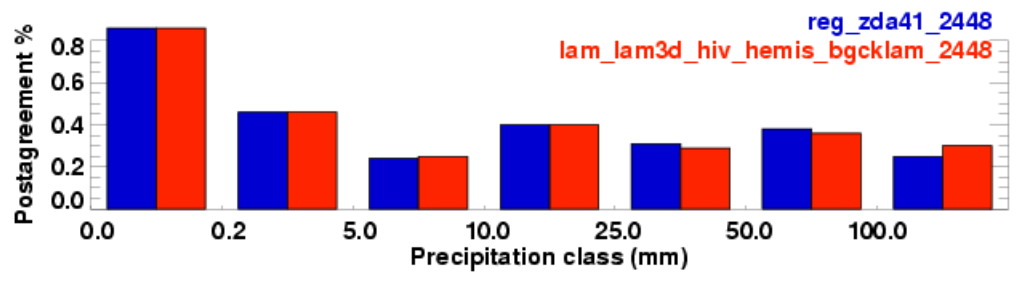
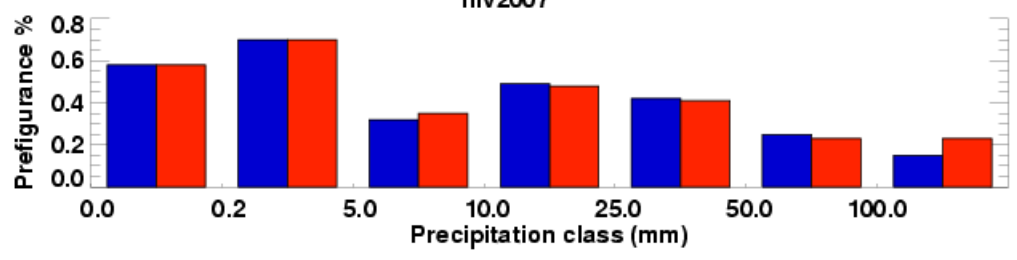
10624	3995	2485	1269	769	510	337	236	164	119
10624	3995	2485	1269	769	510	337	236	164	119

0.2 2.5 5.0 10.0 15.0 20.0 25.0 30.0 35.0 40.0



24 to 48 hours precipitation forecast verification against observation

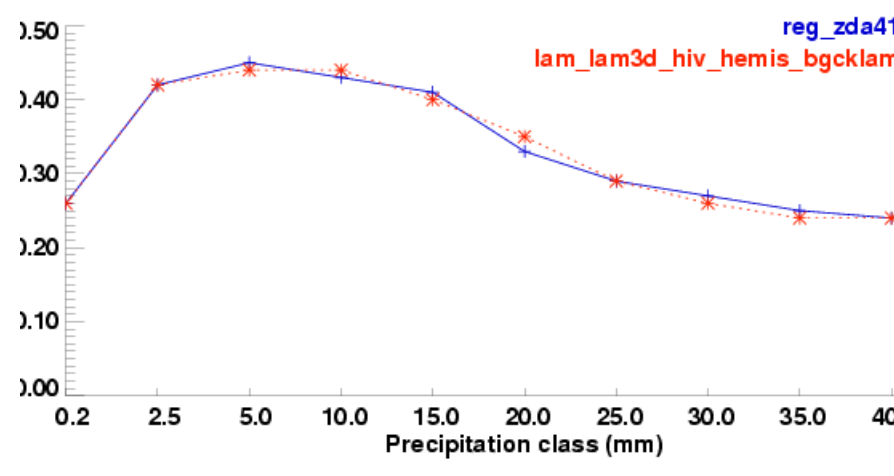
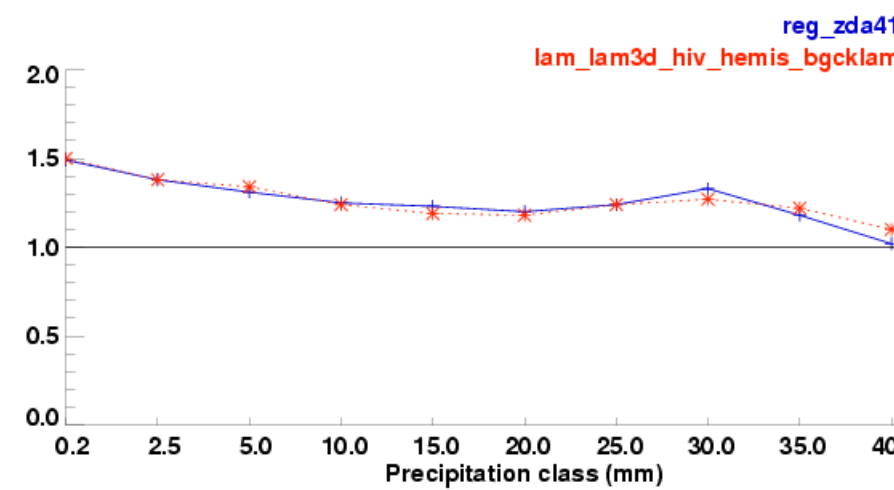
Synoptic network data for valid time 00-12z
24 to 48 hours forecast North AMERICA
hiv2007



Number of observation	
15757	8281
1188	1033
284	71
13	

24 to 48 hours precipitation forecast verification against observation

Synoptic network data for valid time 00-12z
24 to 48 hours forecast North AMERICA
hiv2007



Number of observation	
10601	4090
2512	1369
856	553
361	233
171	

Upgrades to come

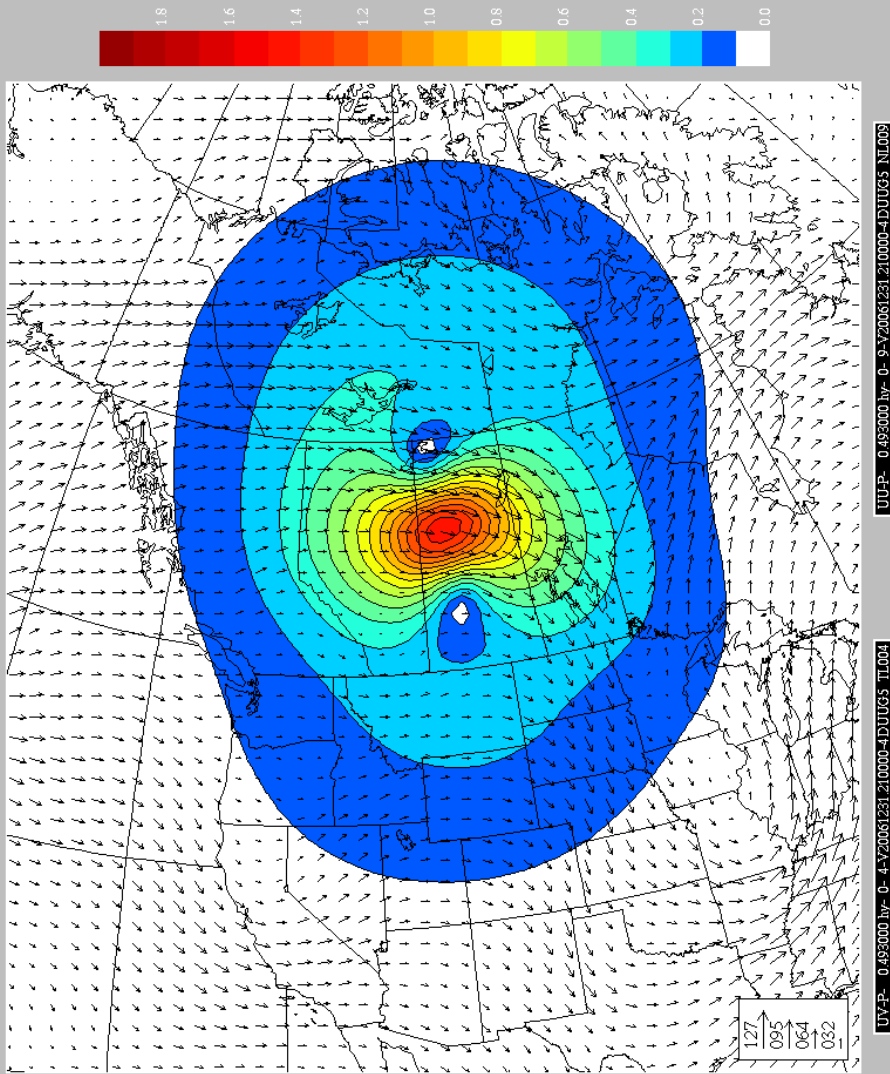
REG-LAM3D Schedule

- Increase horizontal resolution on observation thinning (< 250 km)
- Ground-based GPS (end of 2009)
- NH-T200 → NH-T300, (50 km) analysis (MPI 3D-VAR code, 2009)
- Vertical staggering (Completed by end of 2009)
- 80 Levels Tropospheric Version

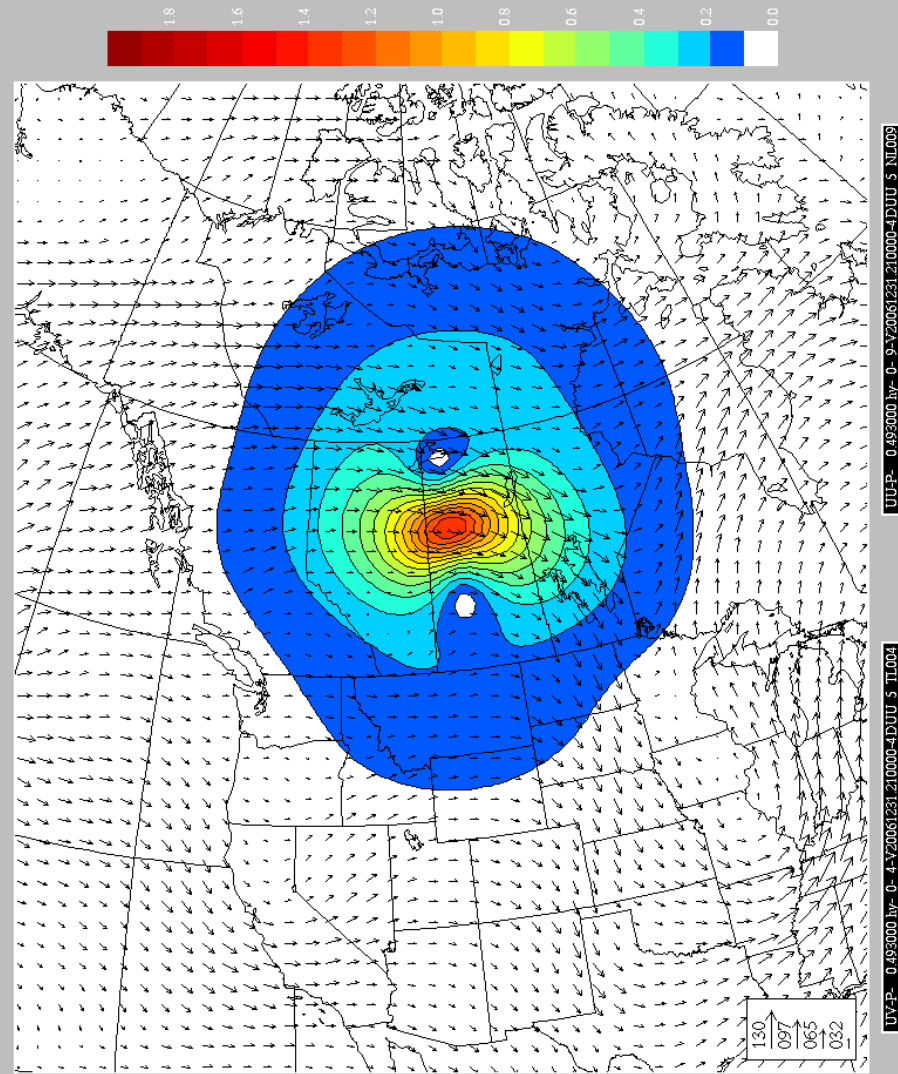
Vertical piloting (Implement RPN's approach within REG-LAM3D. 2010)

- Diabatic INMI constraint (improving initial vertical motions w.r.t moist-physical processes. Adiabatic version implemented at NCEP in GSI, March 2007). Fillion Internal seminar on this, end of 2009.
- Large-scale Ensemble based background-error covariances (2010)
- Improved coupling with the surface analysis (Marco et al., 2009-2010)
- Pursue REG-LAM4D (???)
- ?? km horizontal resolution (2011)
- Meso-scale observations (radar radial-winds)
- LAM 4D-Var at mesoscale.
- Include real assimilation for 2.5 km LAM's.



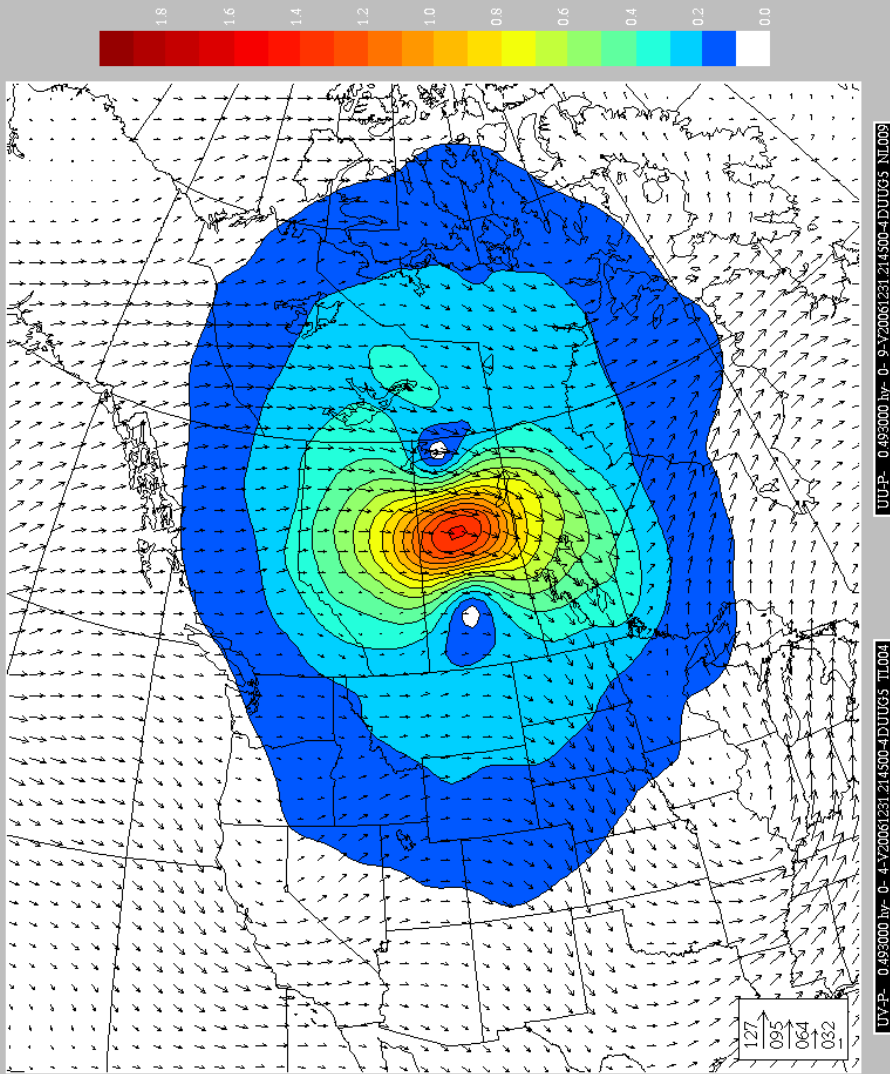


4D-Var GLB 170km

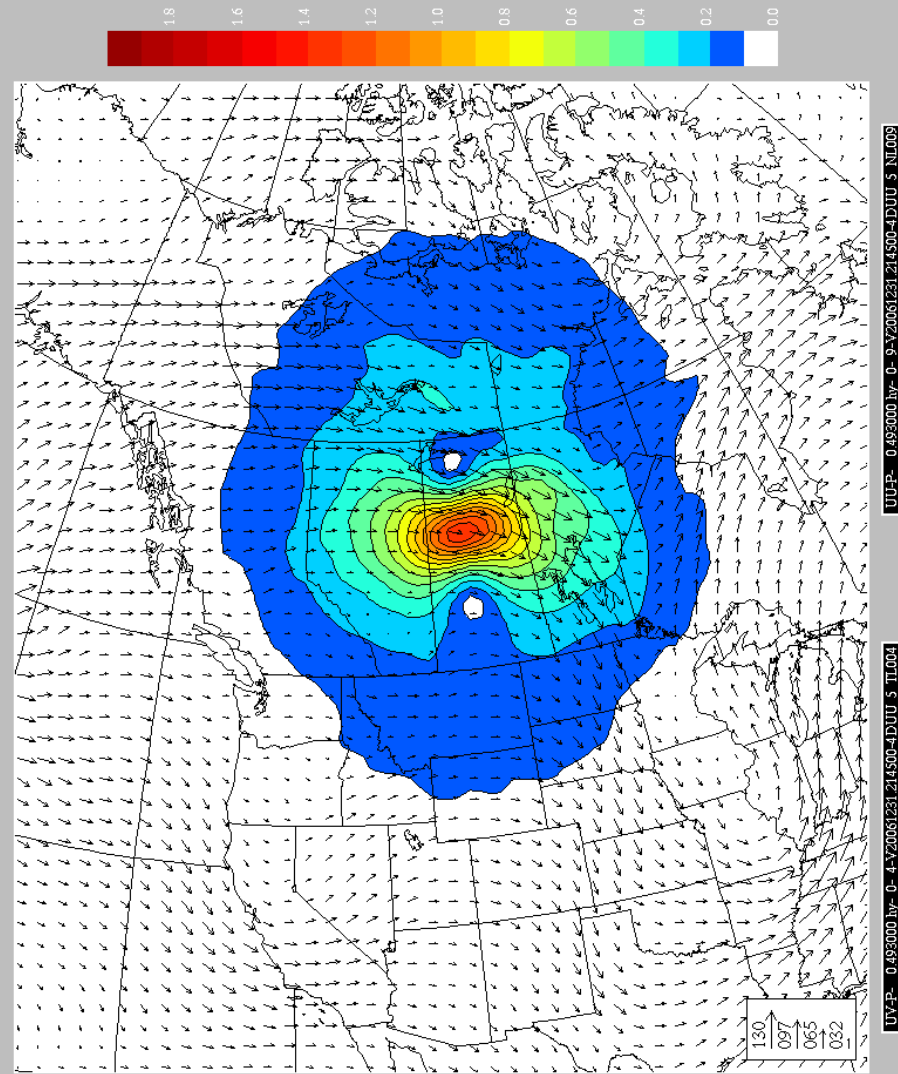


4D-Var LAM 55km

T = -3.00 hr



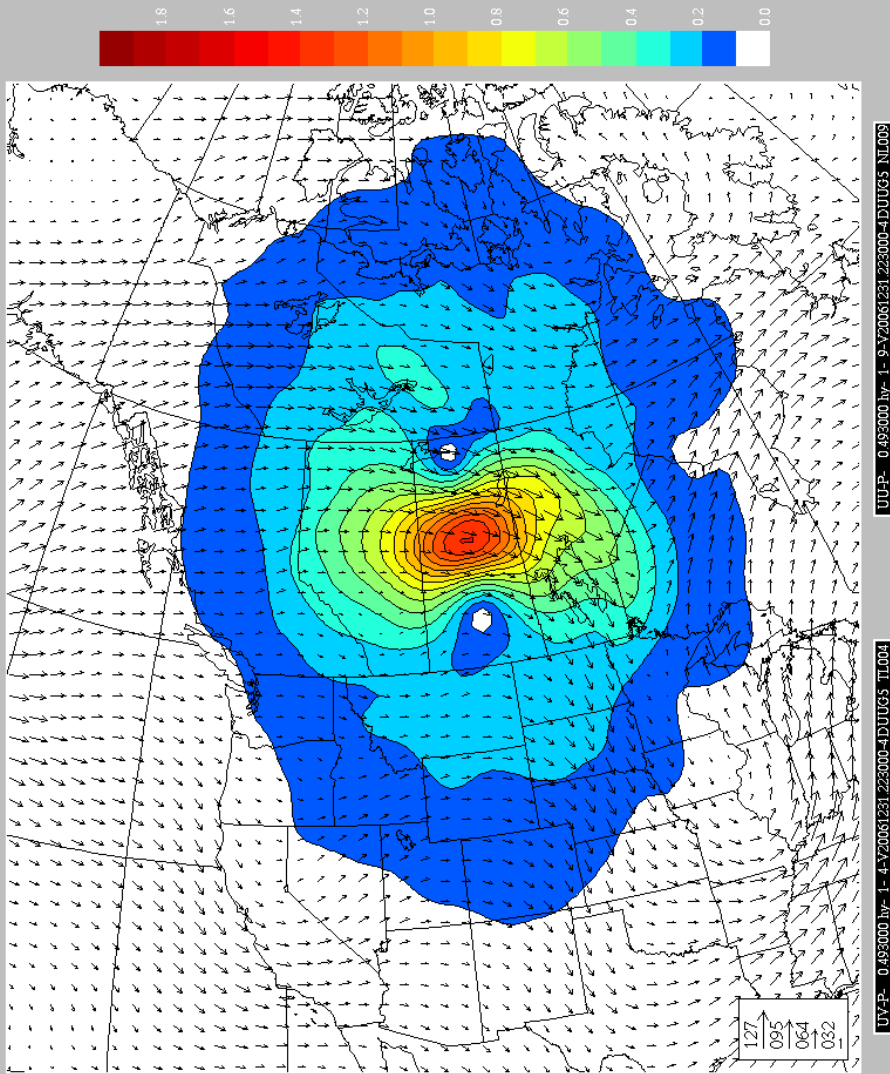
4D-Var GLB 170km



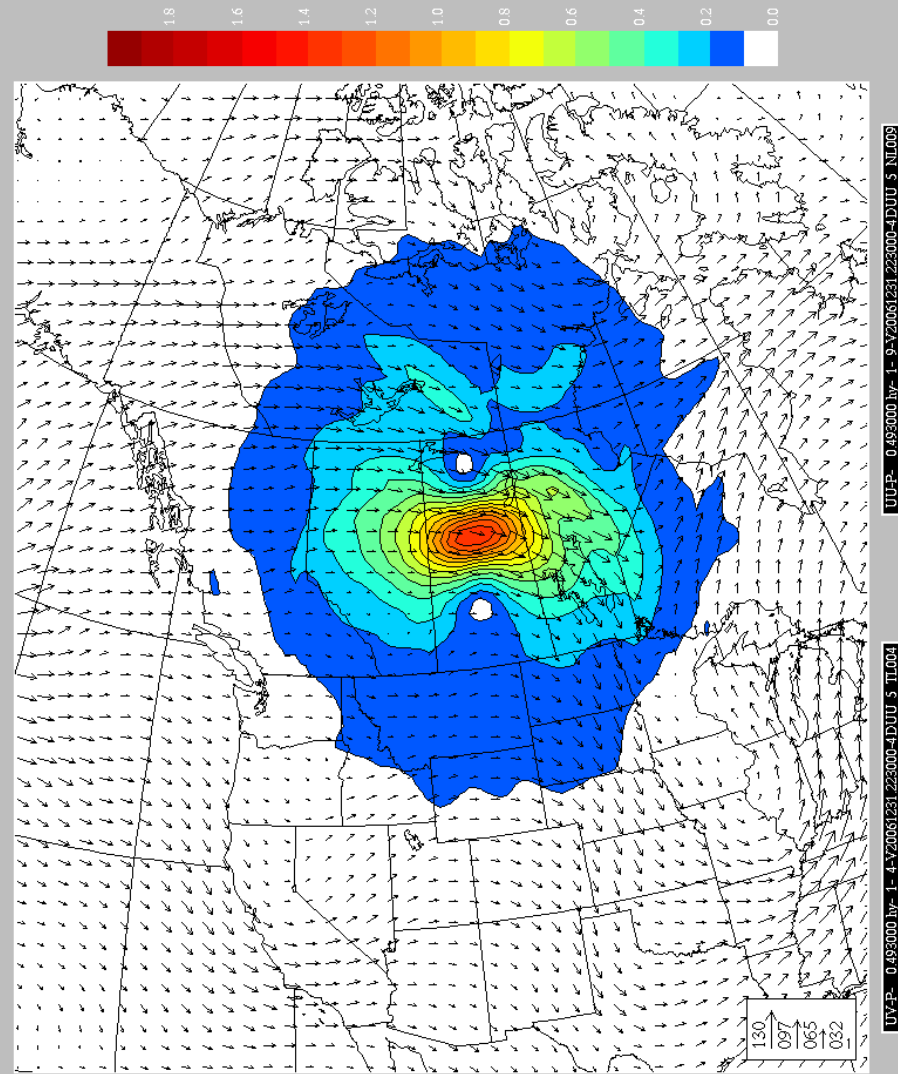
4D-Var LAM 55km

T = -2.15 hr





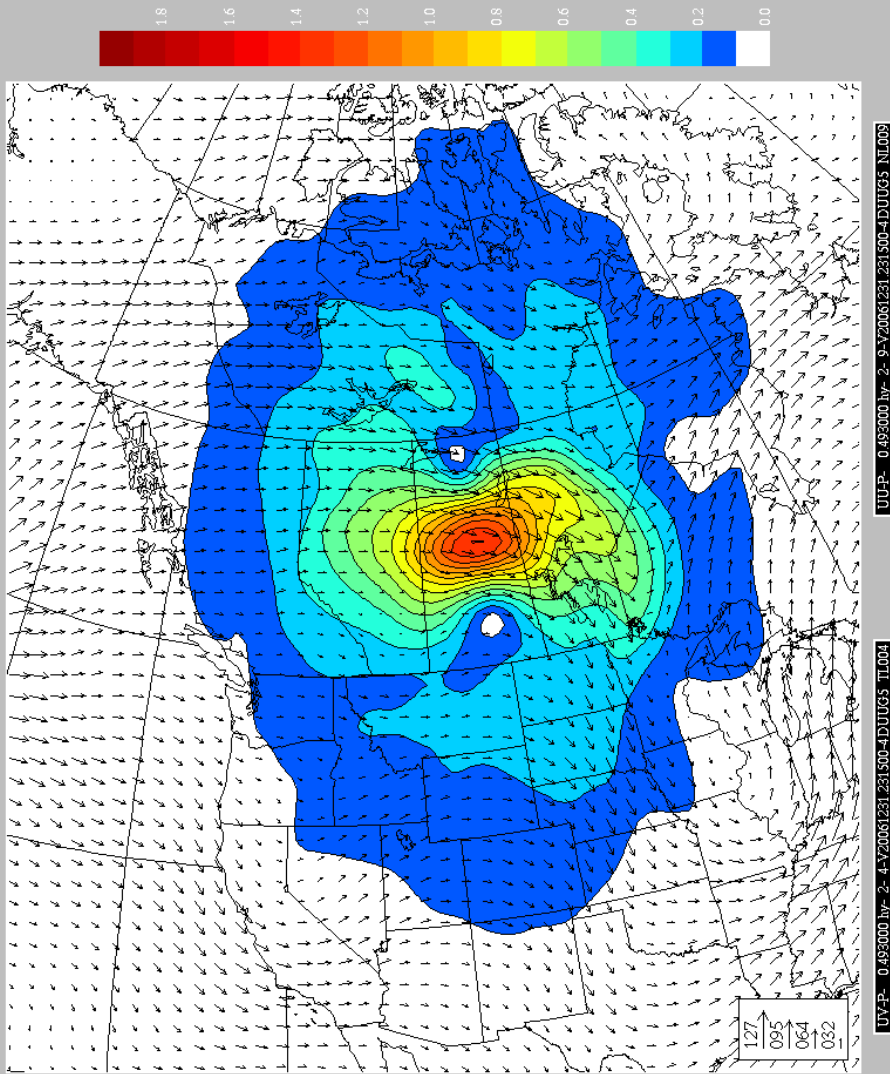
4D-Var GLB 170km



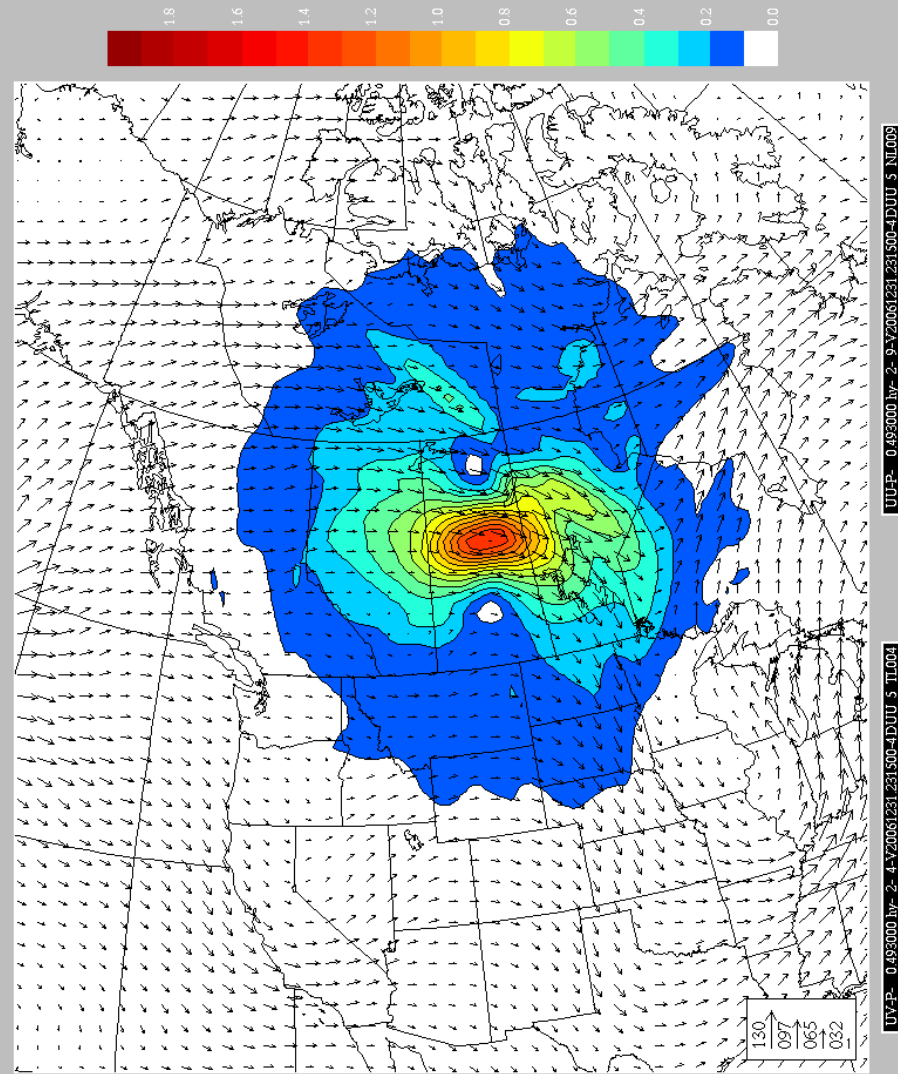
4D-Var LAM 55km

T = -1.30 hr





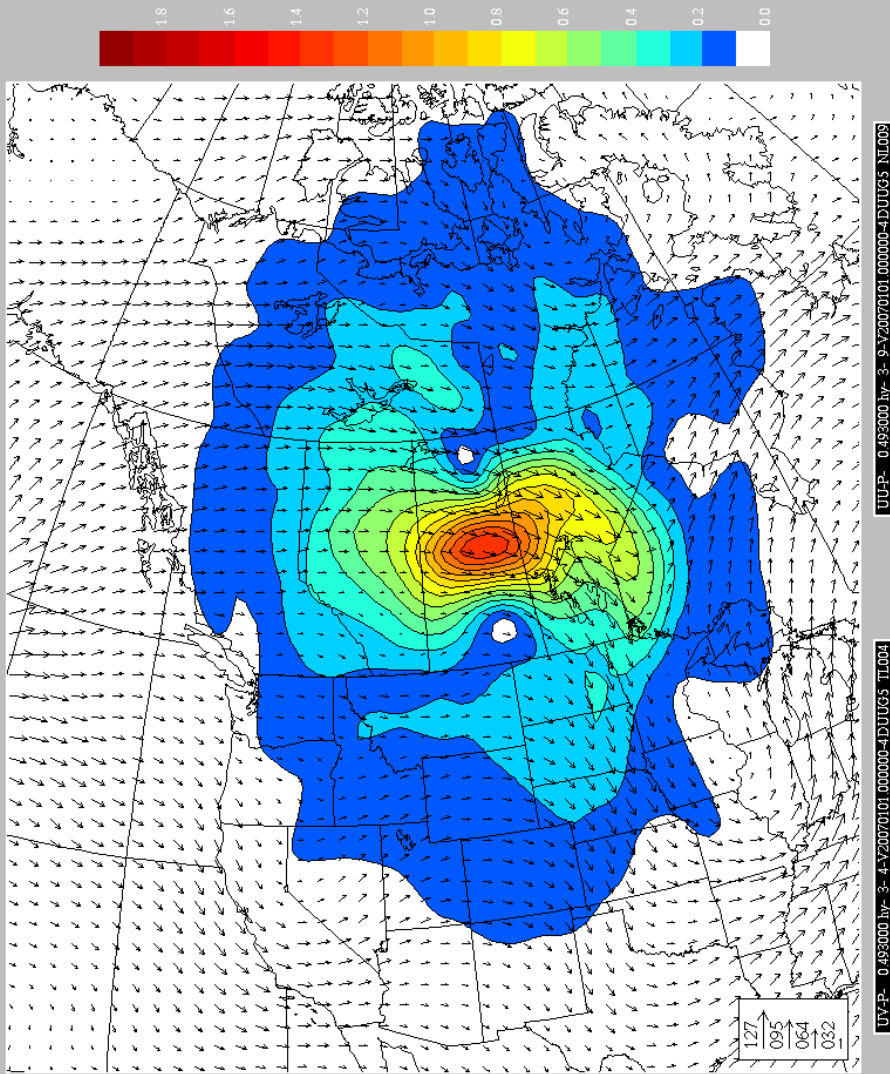
4D-Var GLB 170km



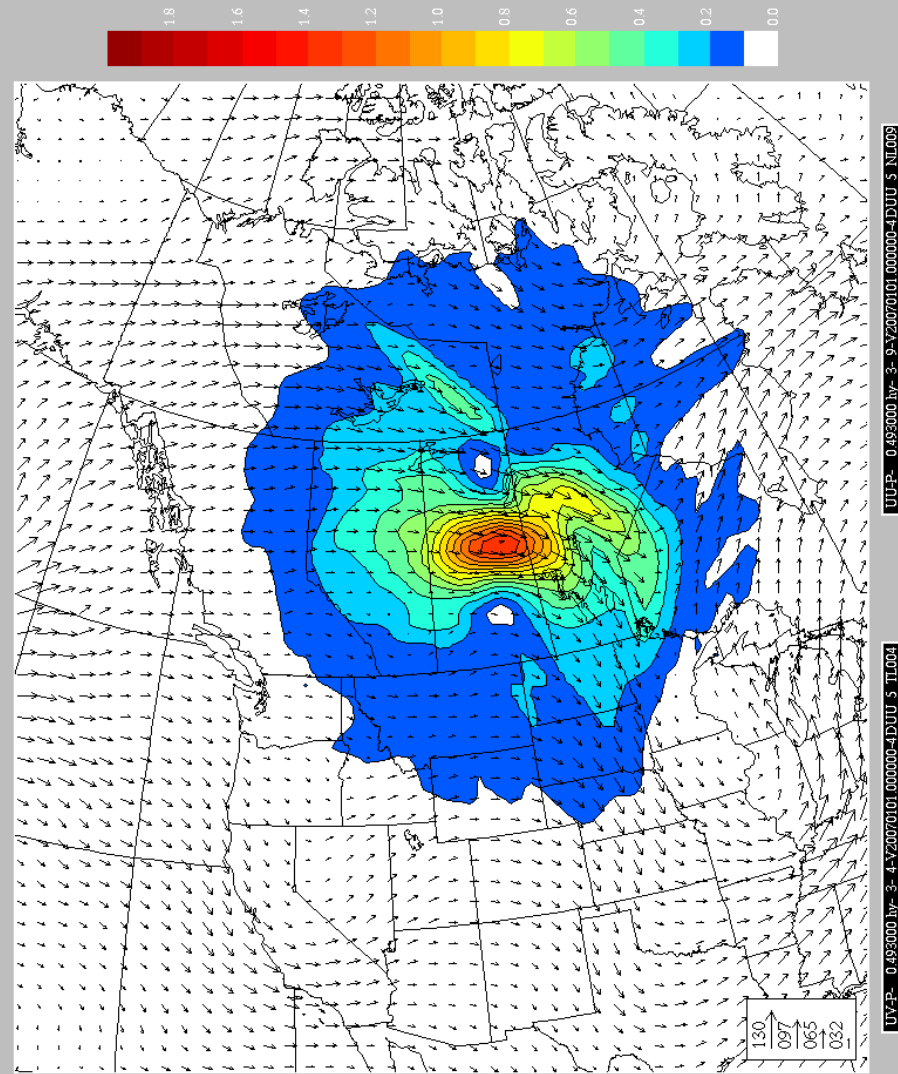
4D-Var LAM 55km

T = -0.45 hr





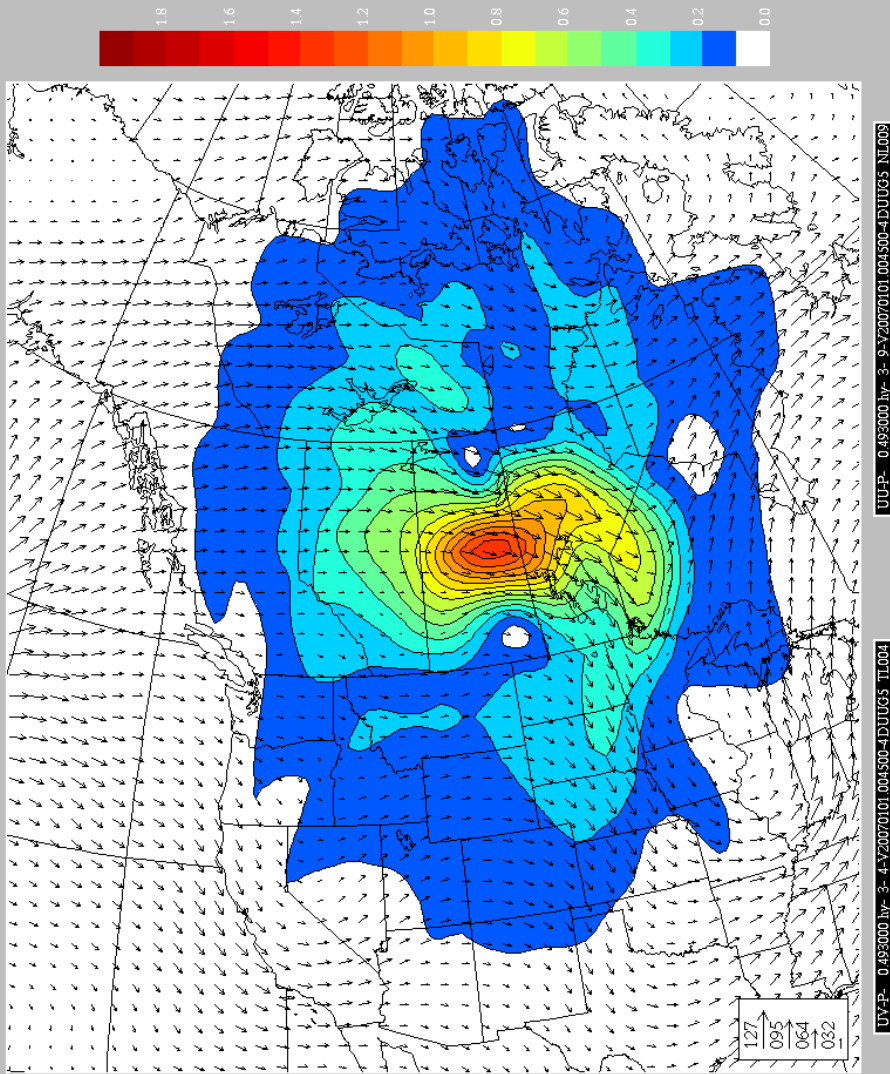
4D-Var GLB 170km



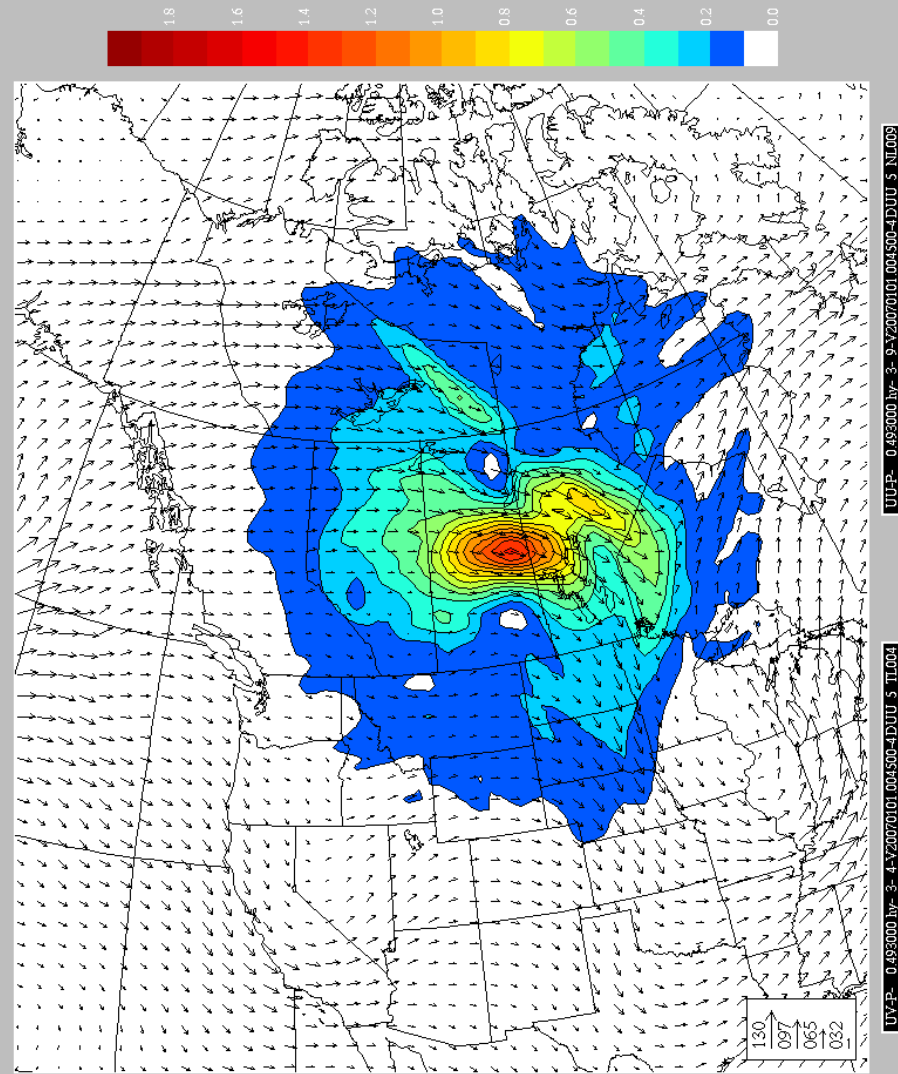
4D-Var LAM 55km

T = +0.00 hr





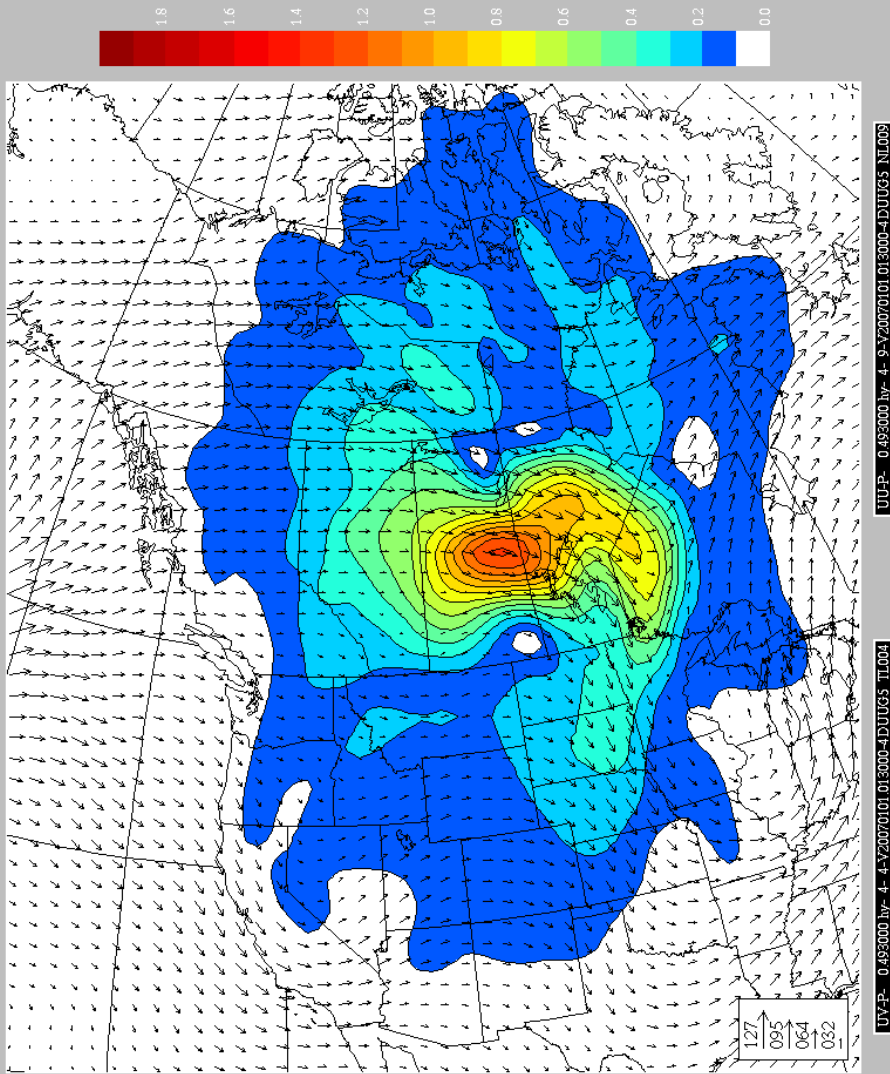
4D-Var GLB 170km



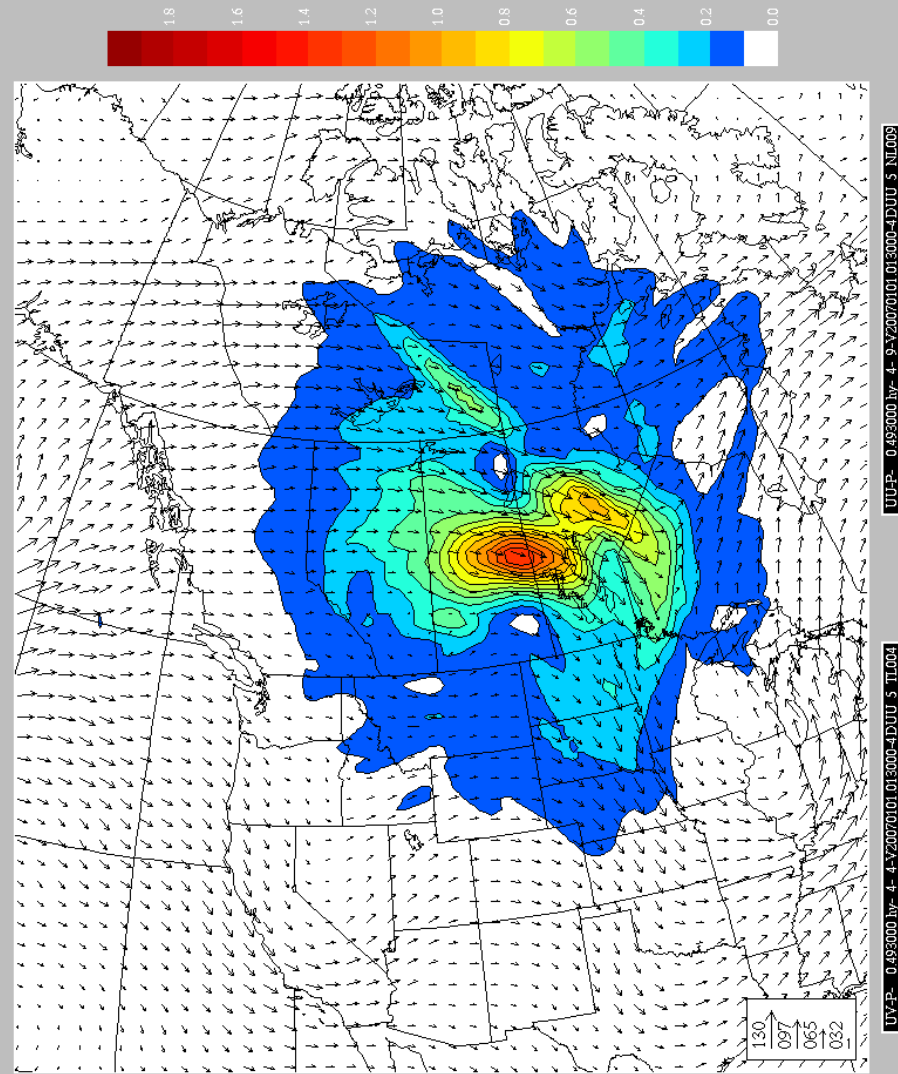
4D-Var LAM 55km

T = +0.45 hr



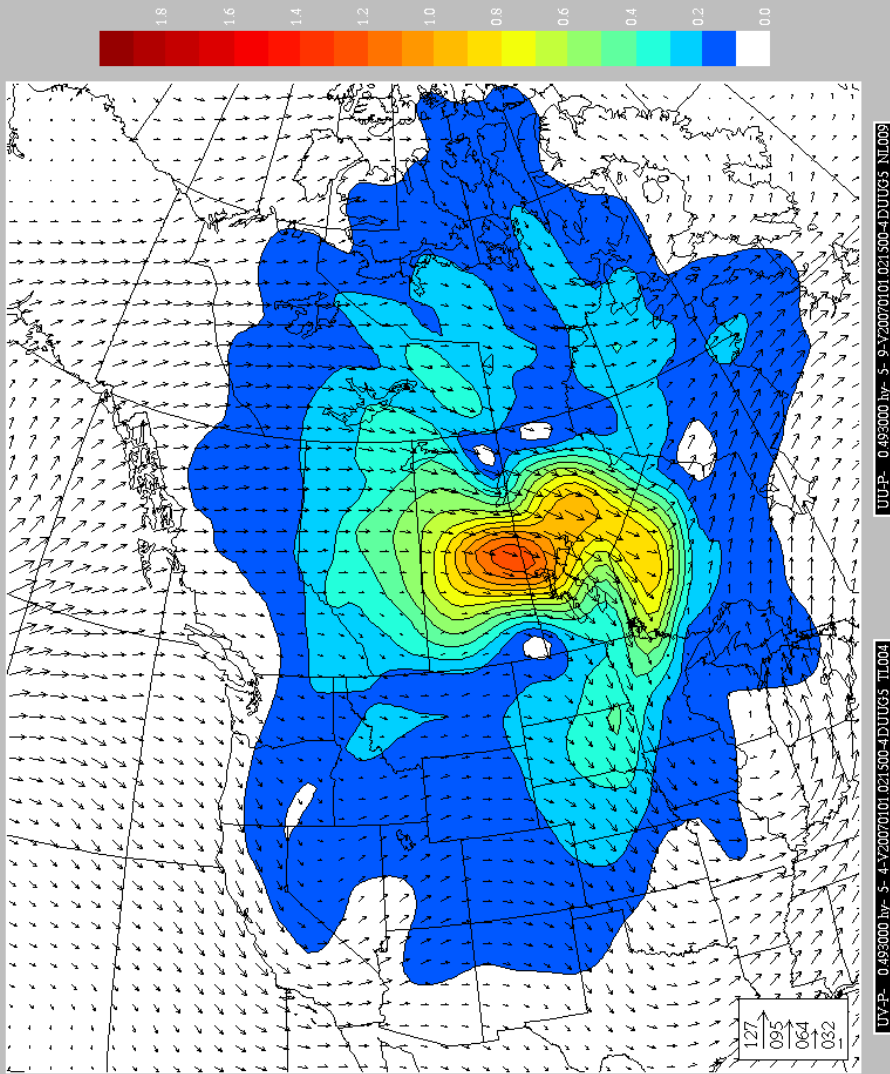


4D-Var GLB 170km

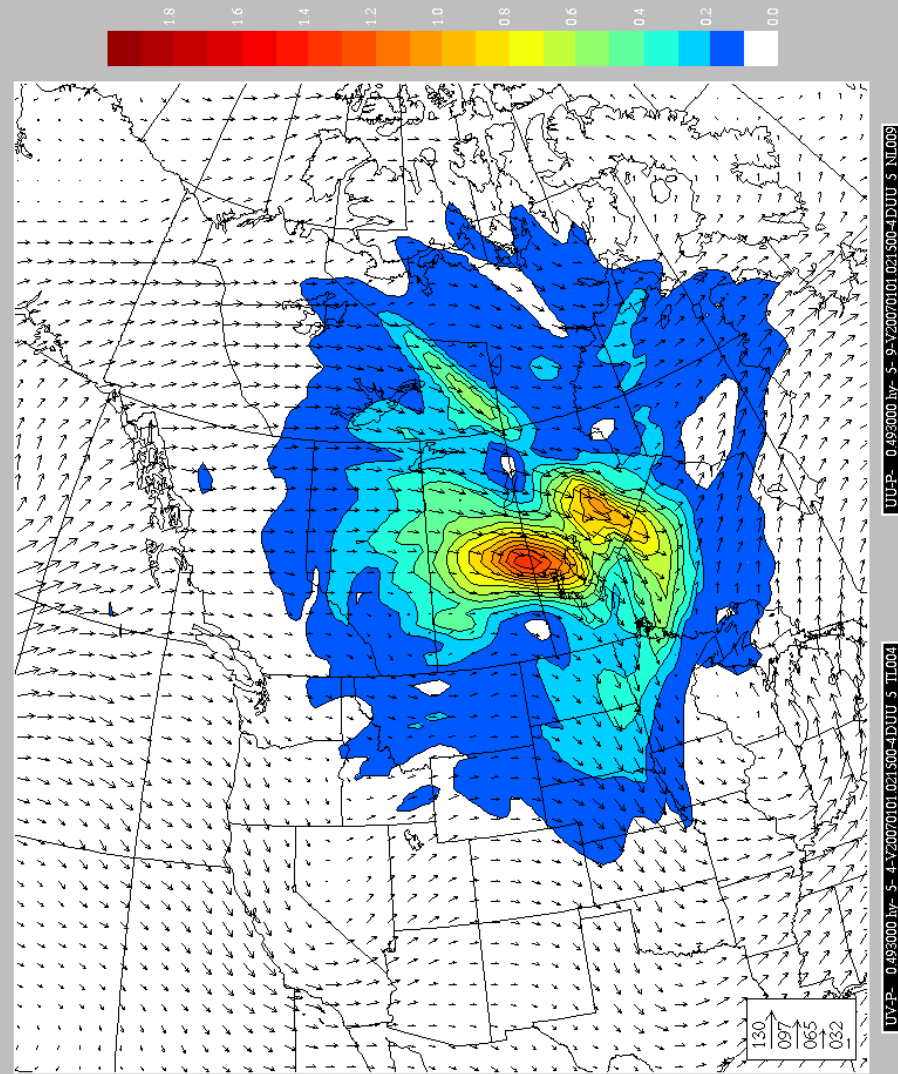


4D-Var LAM 55km

T = +1.30 hr



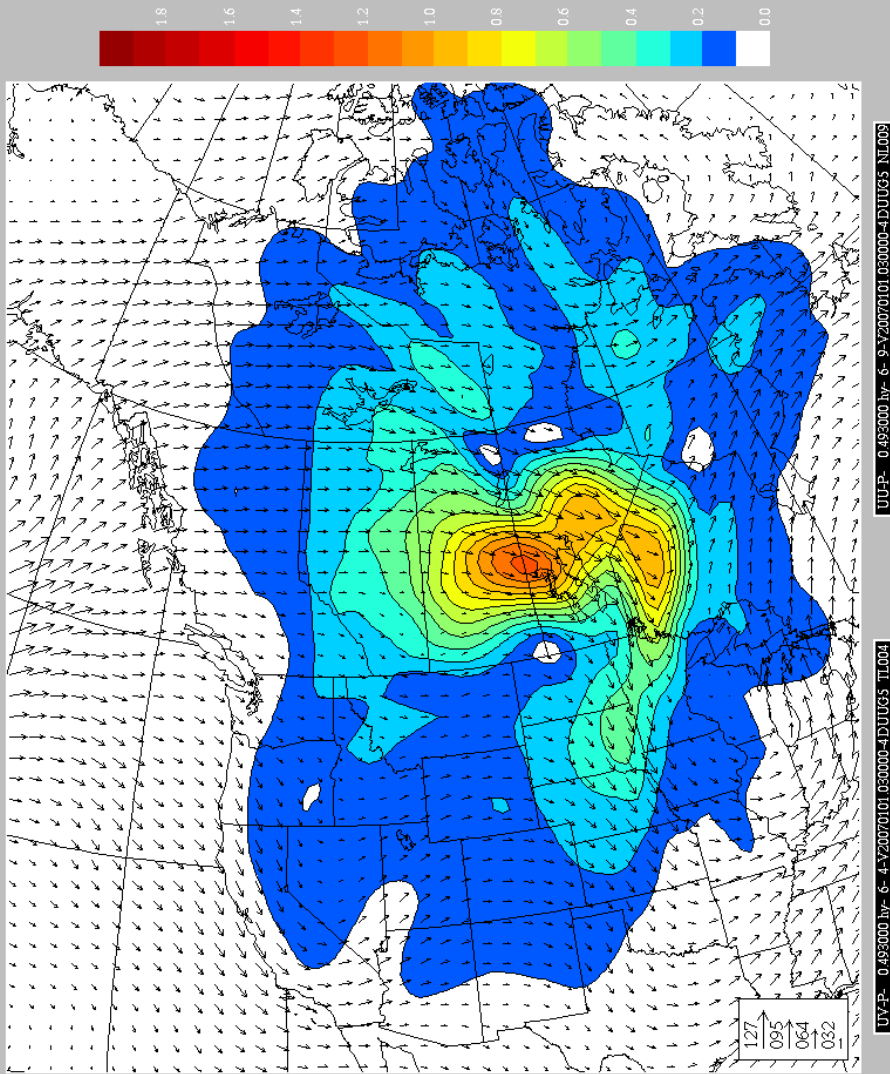
4D-Var GLB 170km



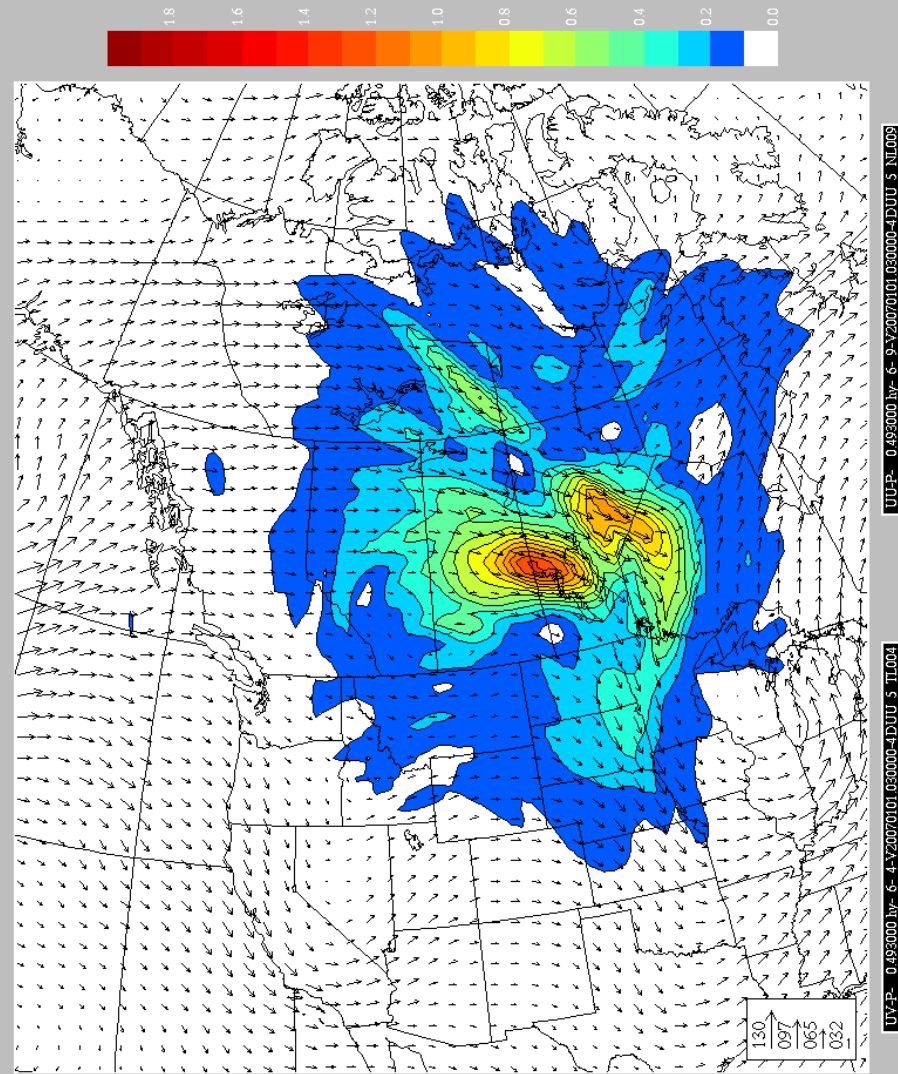
4D-Var LAM 55km

T = +2.15 hr





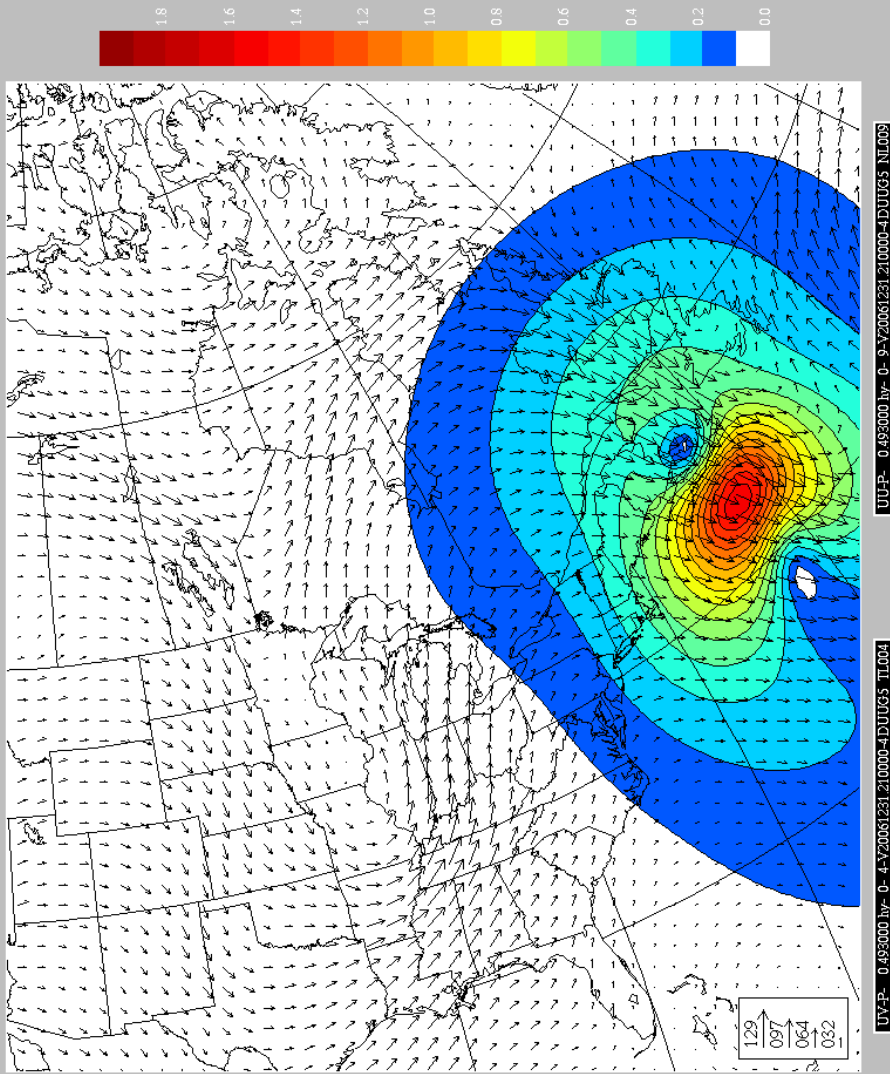
4D-Var GLB 170km



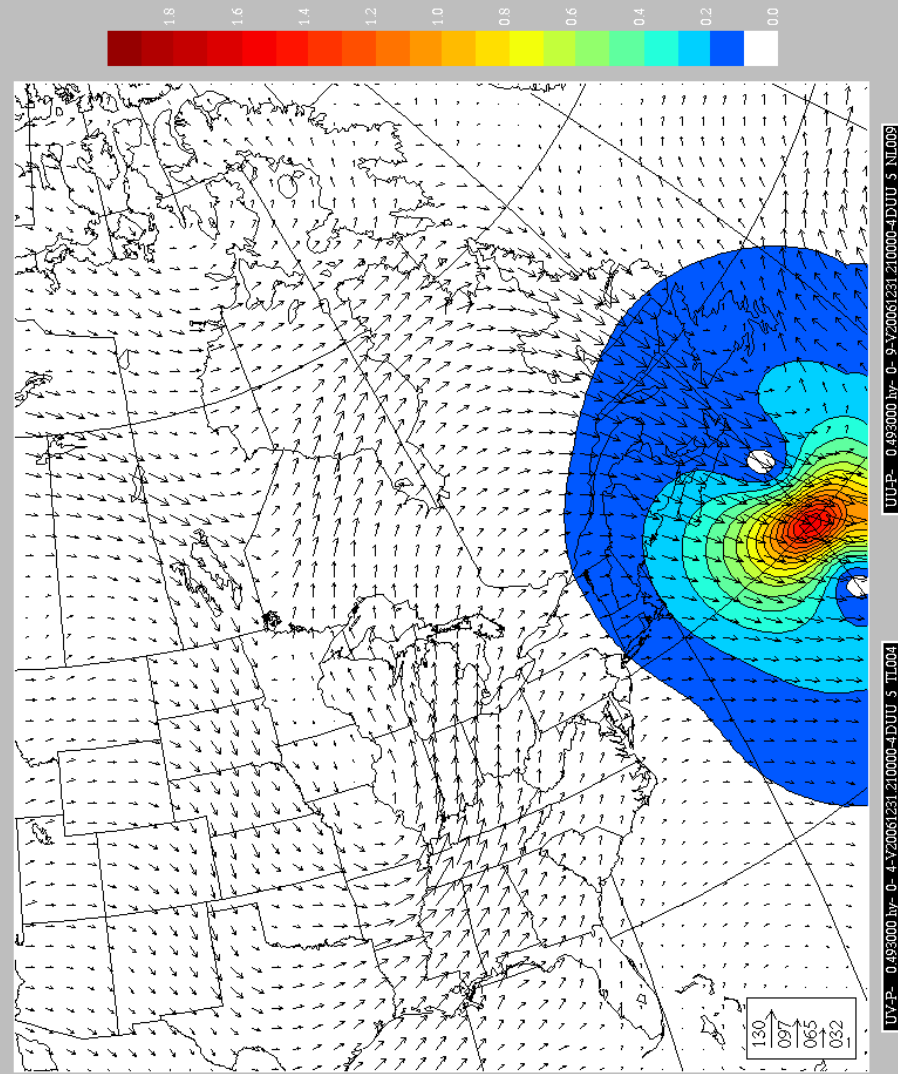
4D-Var LAM 55km

T = +3.00 hr





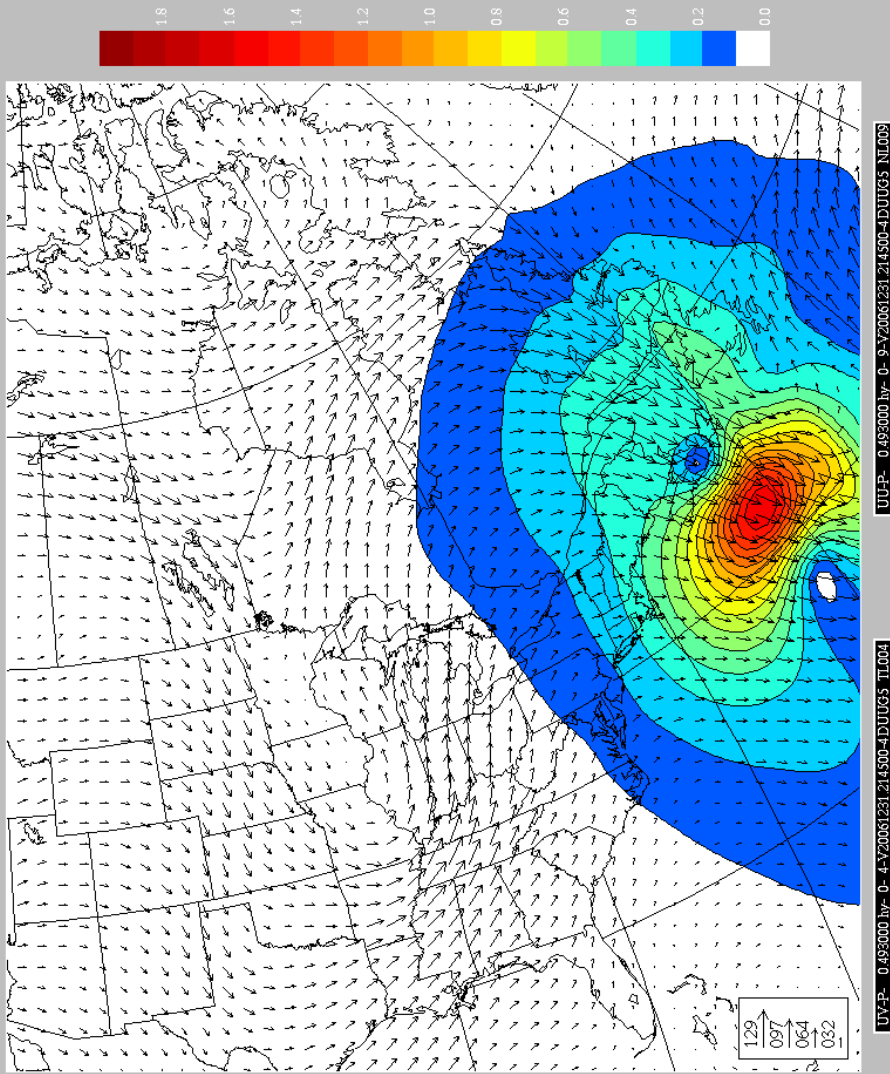
4D-Var GLB 170km



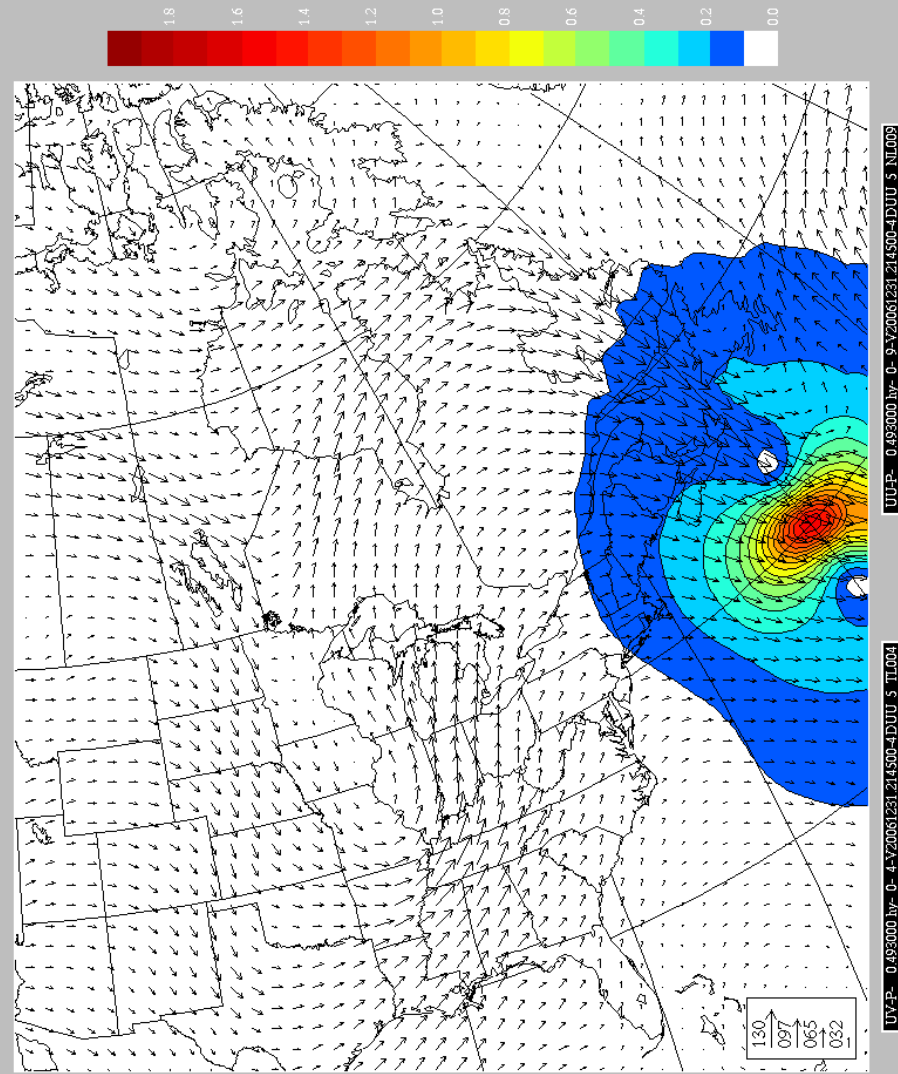
4D-Var LAM 55km

T = -3.00 hr





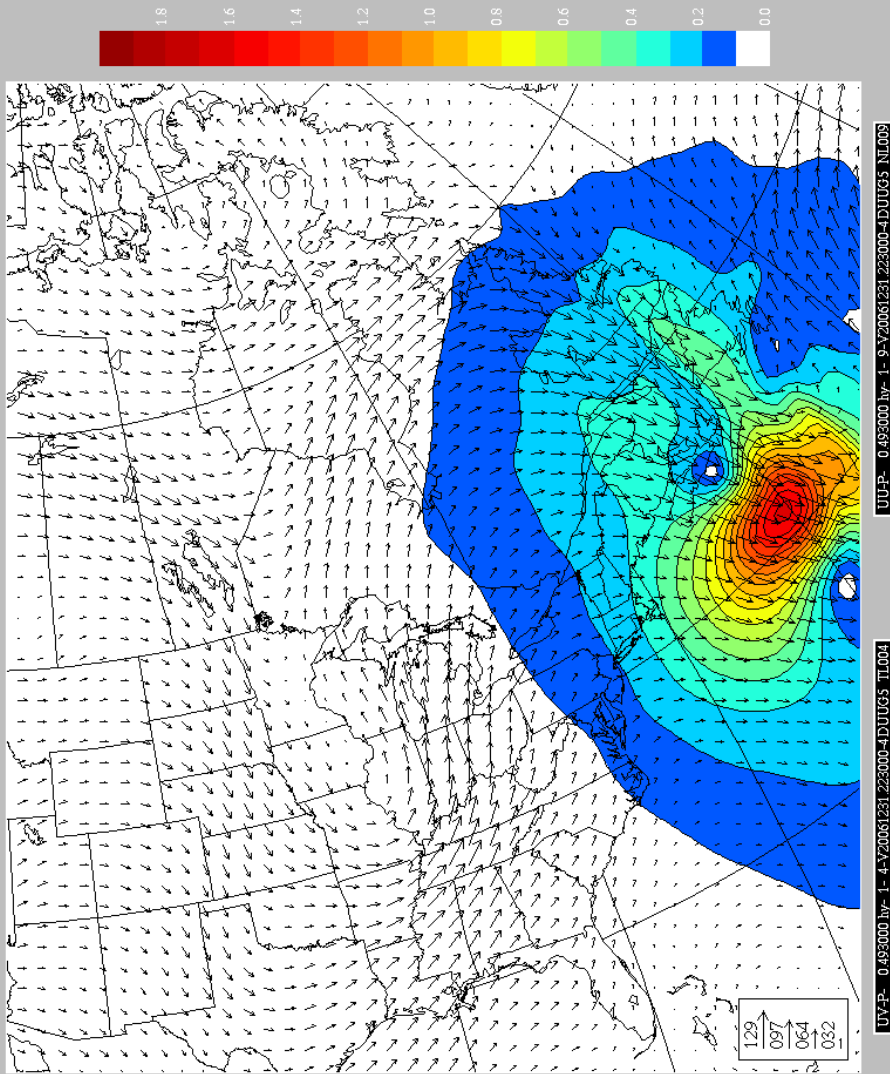
4D-Var GLB 170km



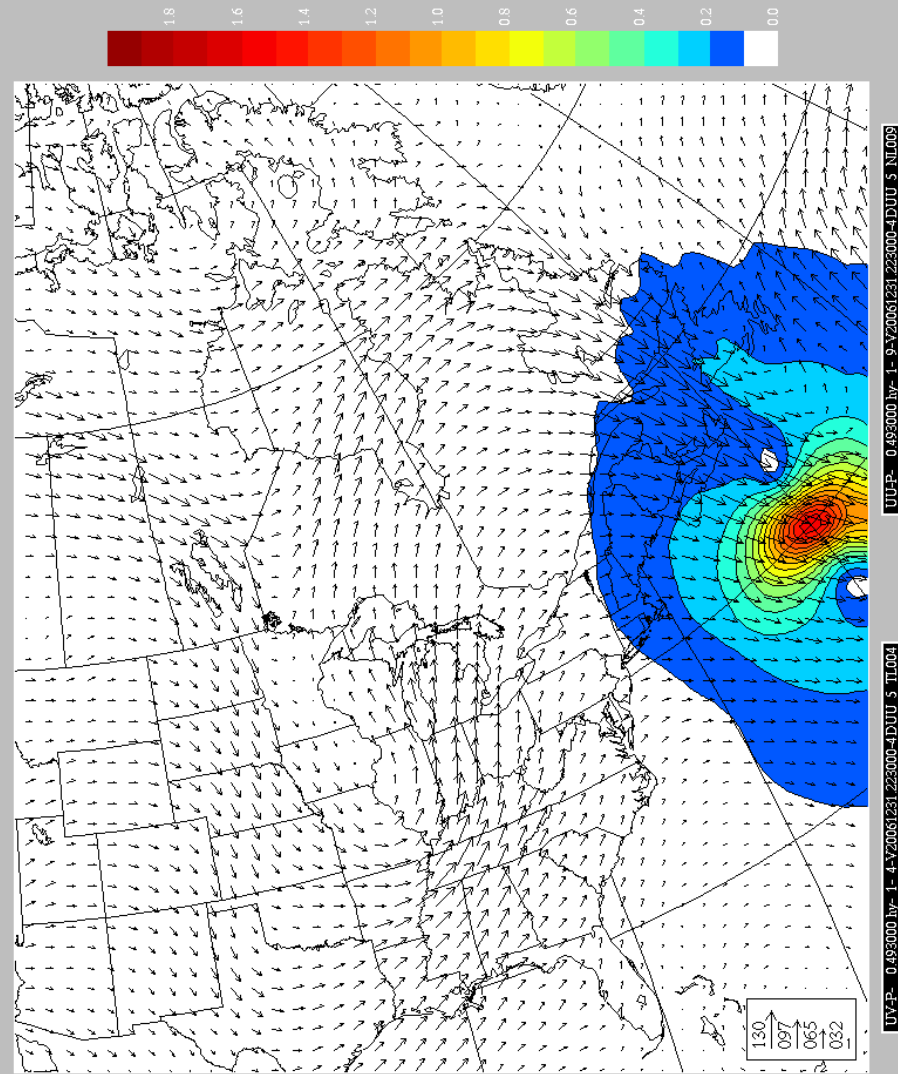
4D-Var LAM 55km

T = -2.15 hr





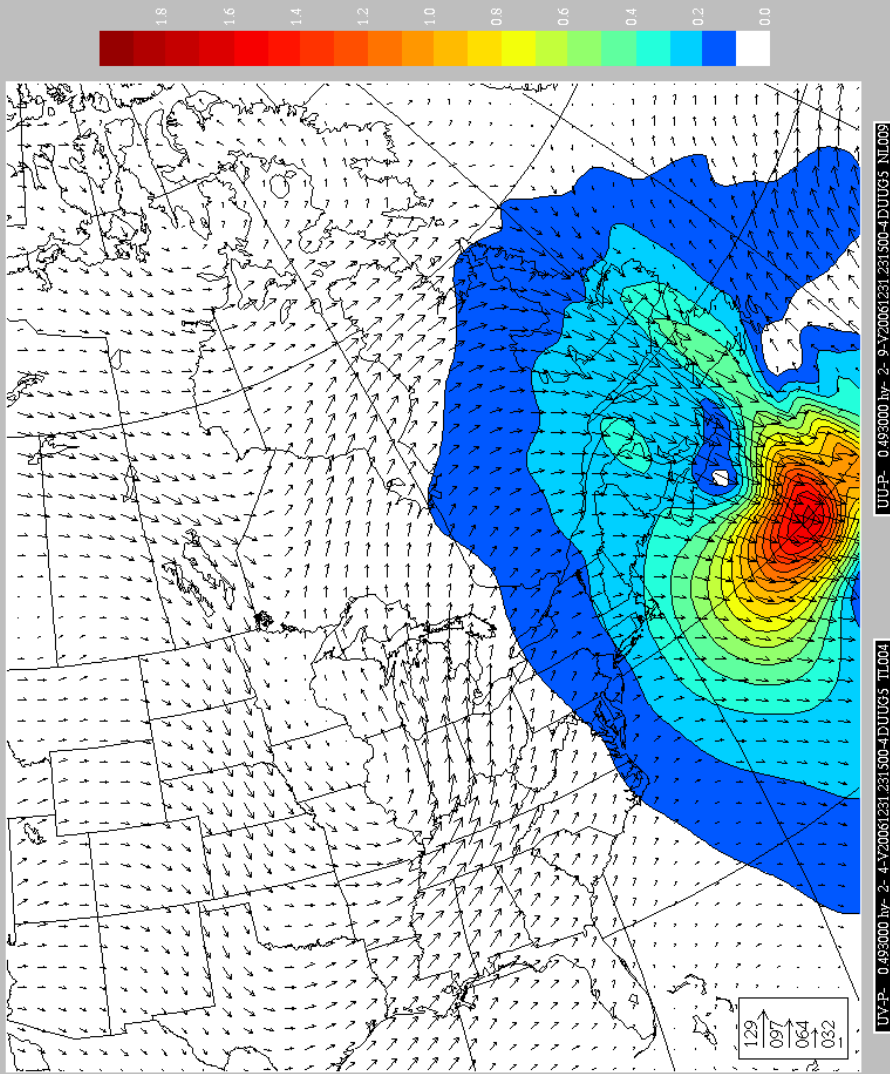
4D-Var GLB 170km



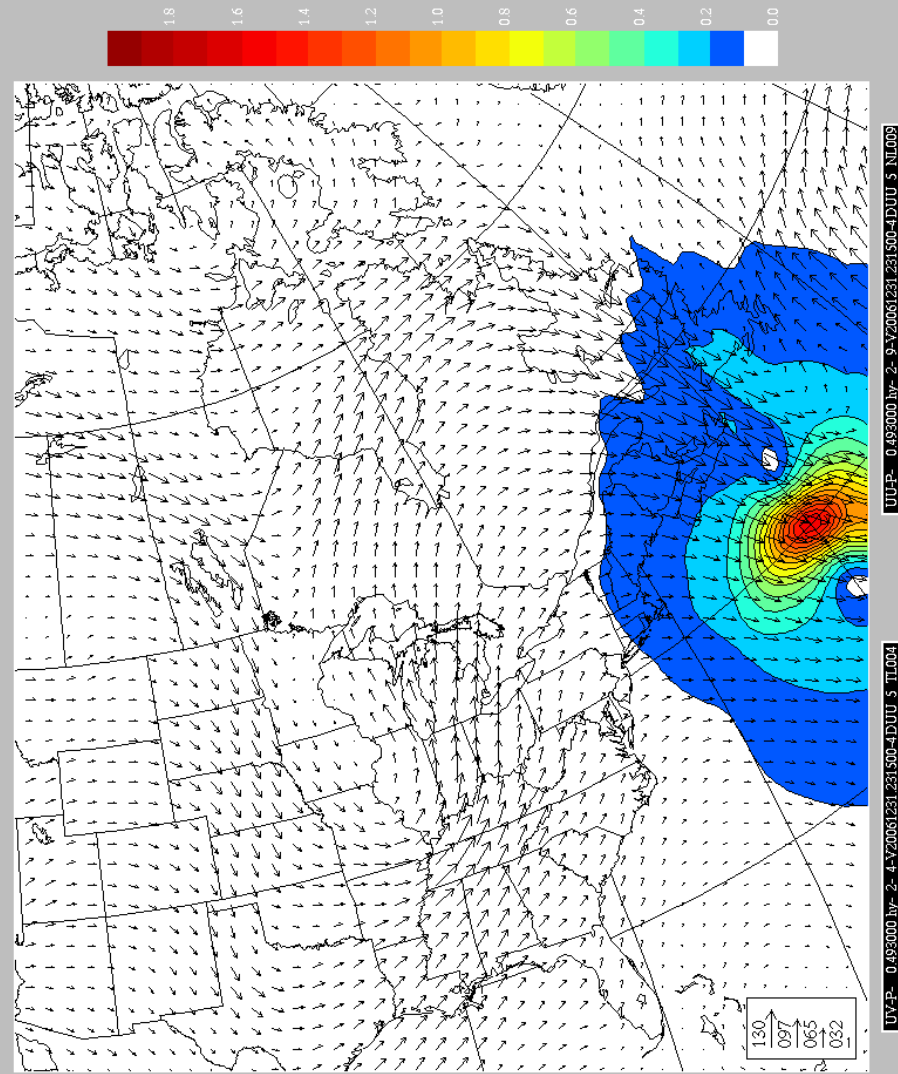
4D-Var LAM 55km

T = -1.30 hr





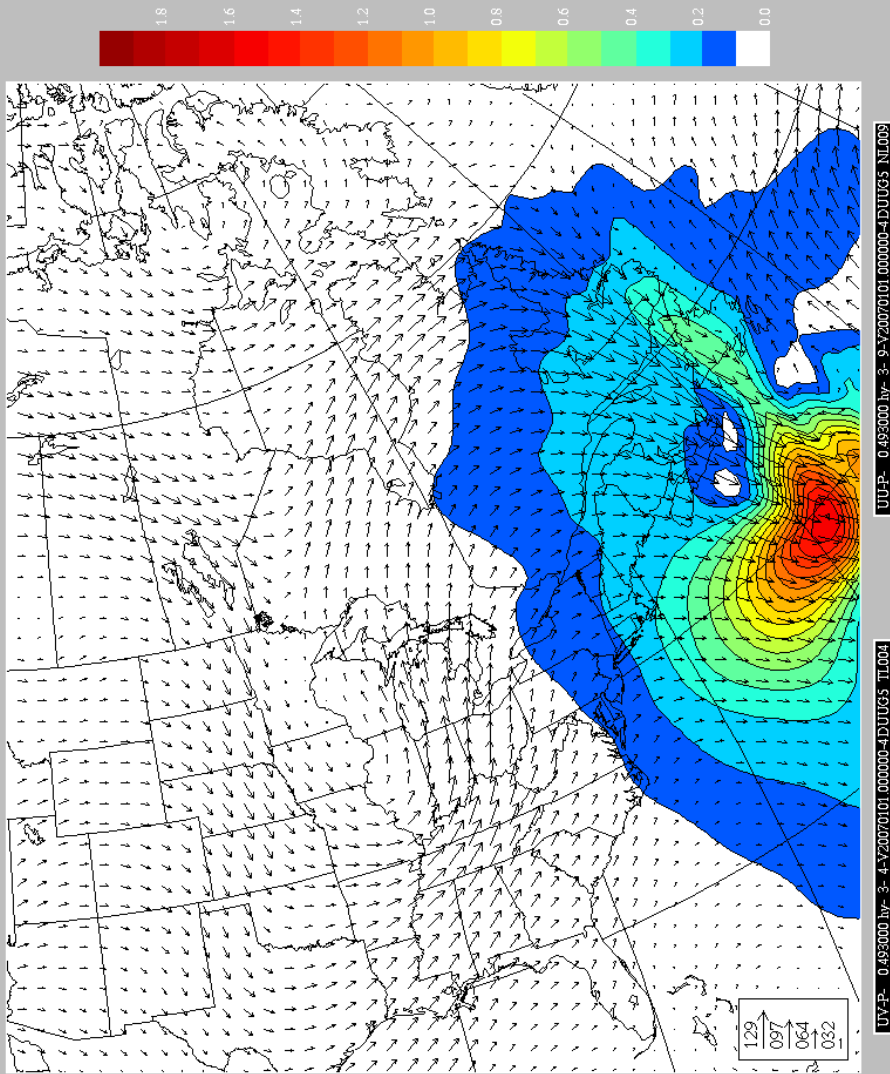
4D-Var GLB 170km



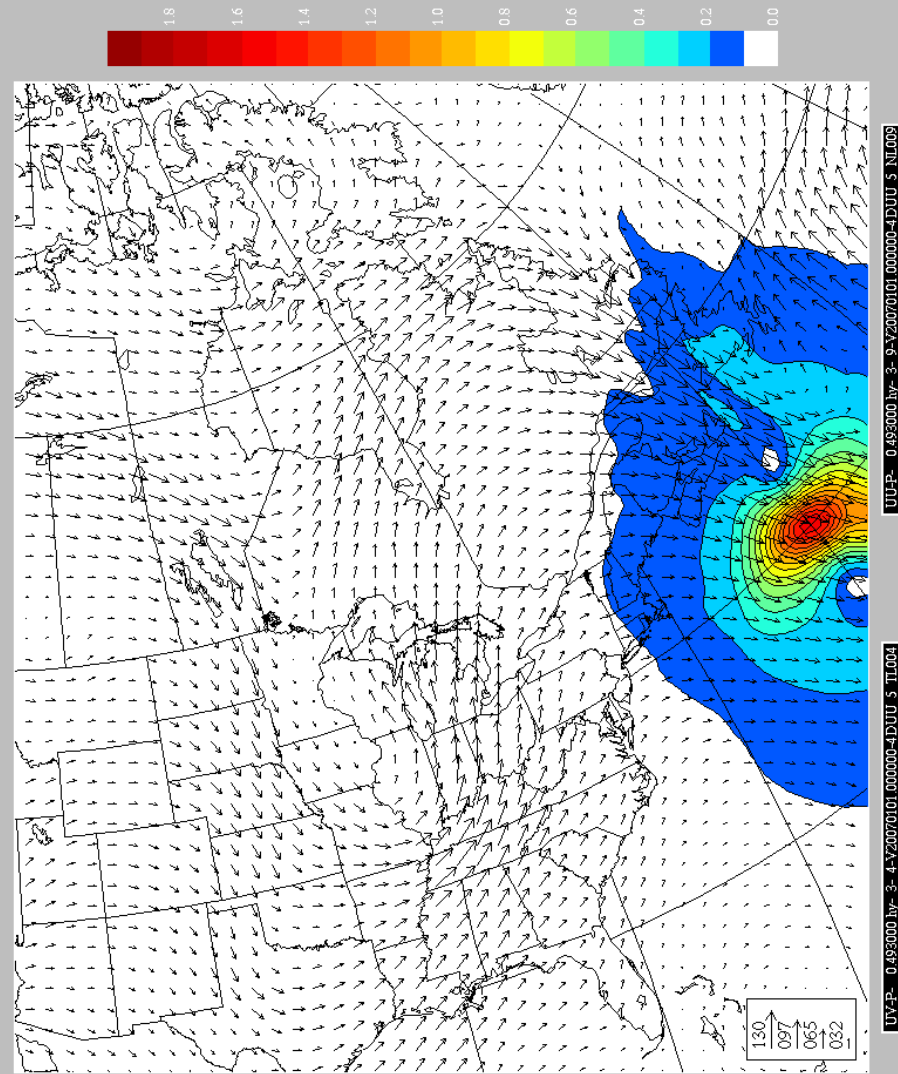
4D-Var LAM 55km

T = -0.45 hr





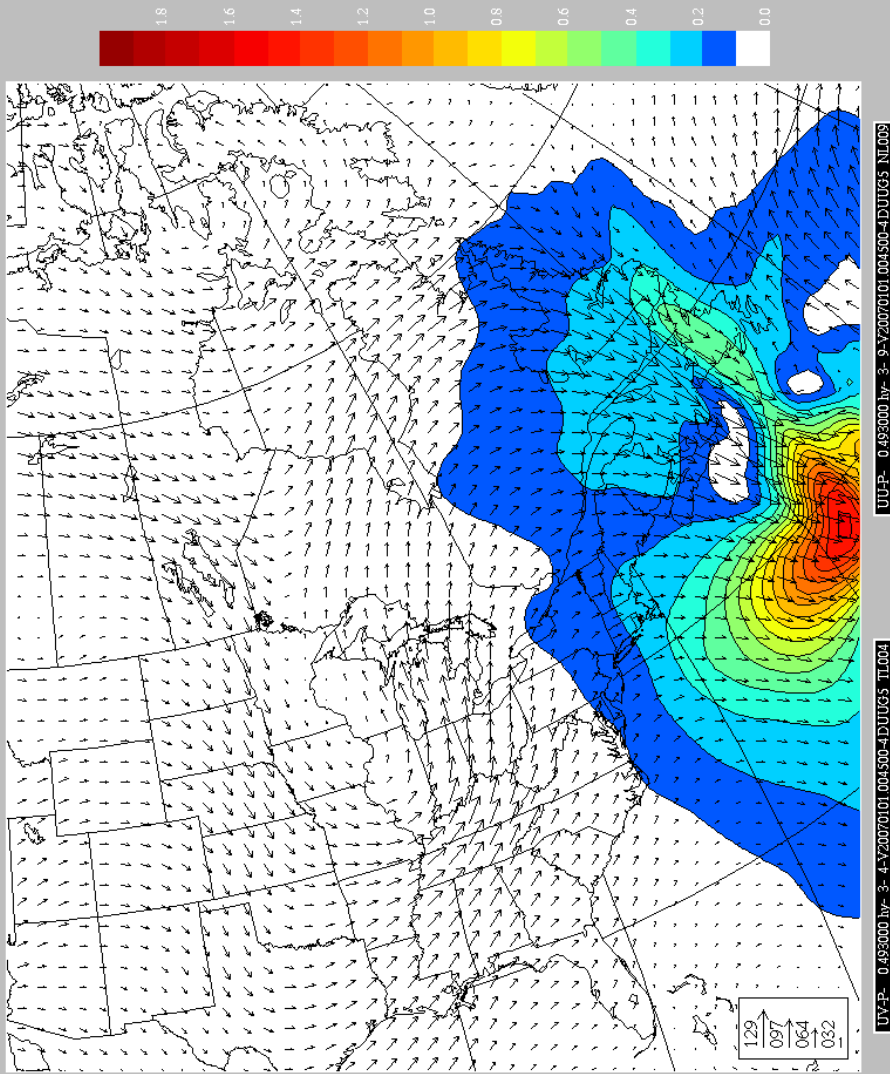
4D-Var GLB 170km



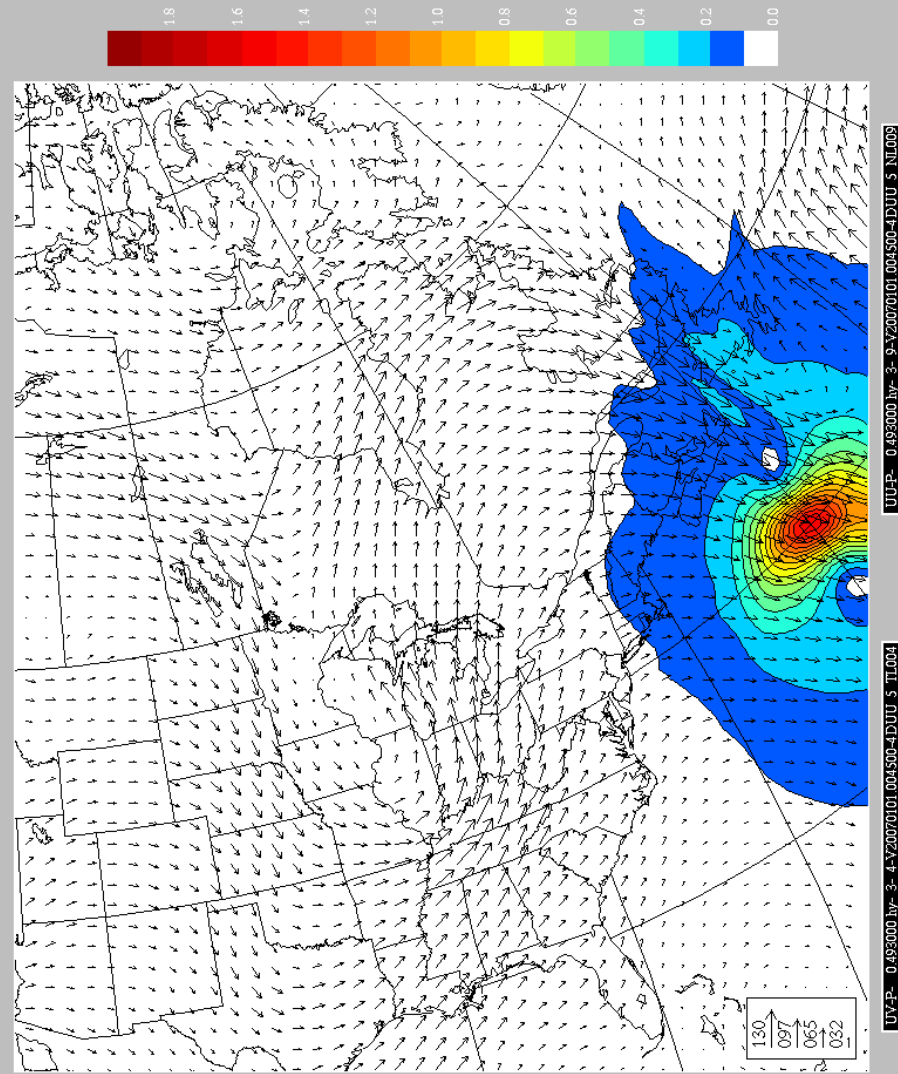
4D-Var LAM 55km

T = +0.00 hr





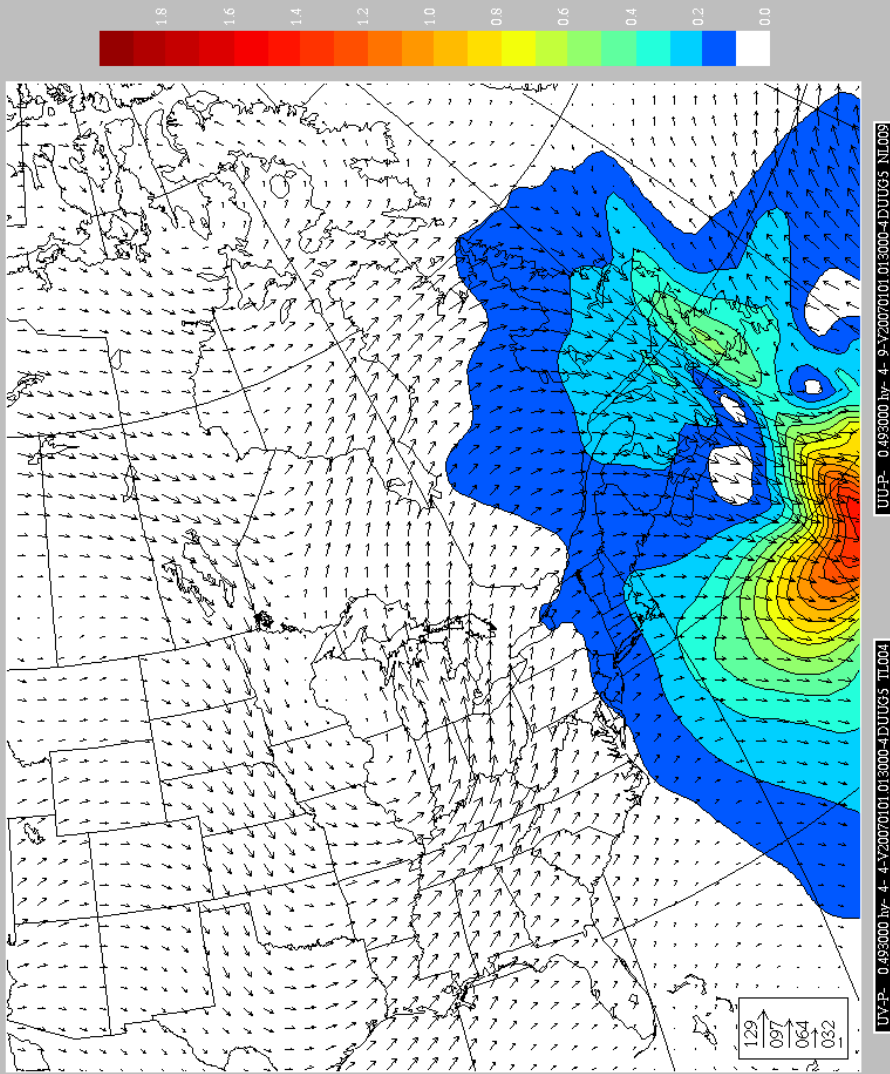
4D-Var GLB 170km



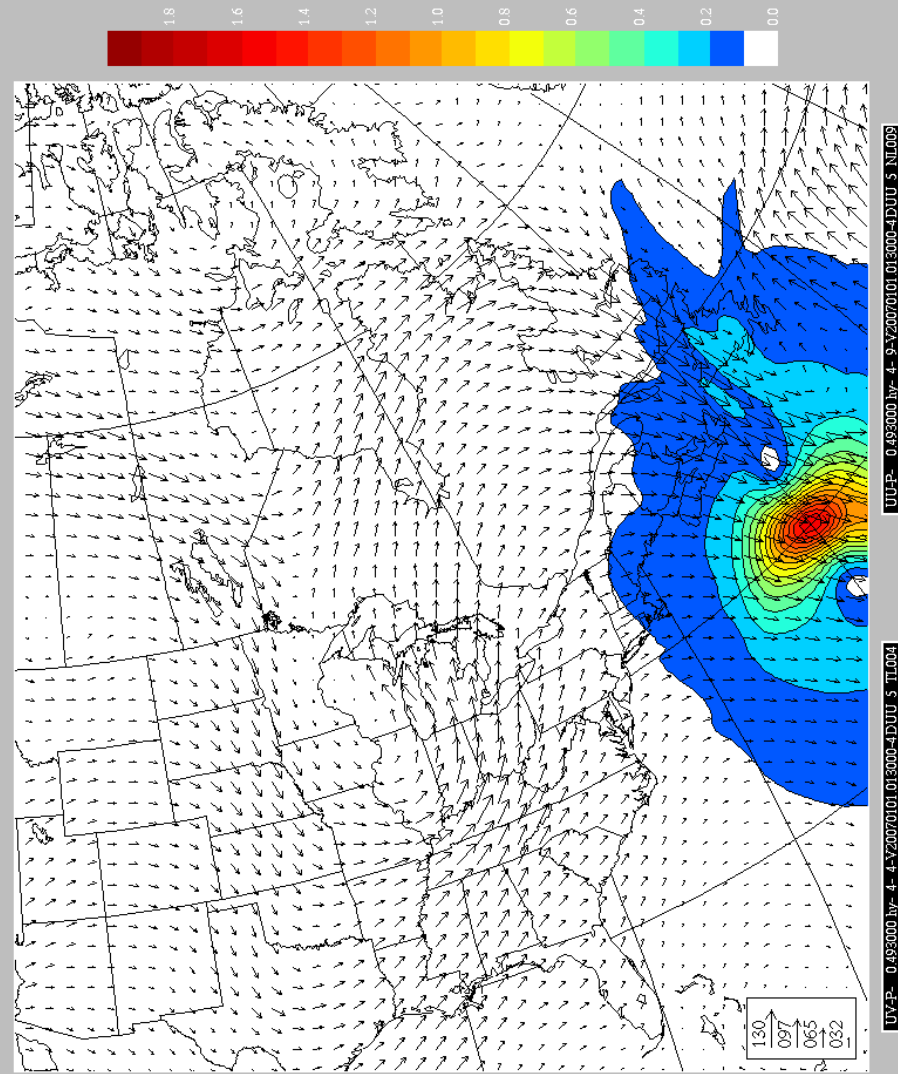
4D-Var LAM 55km

T = +0.45 hr





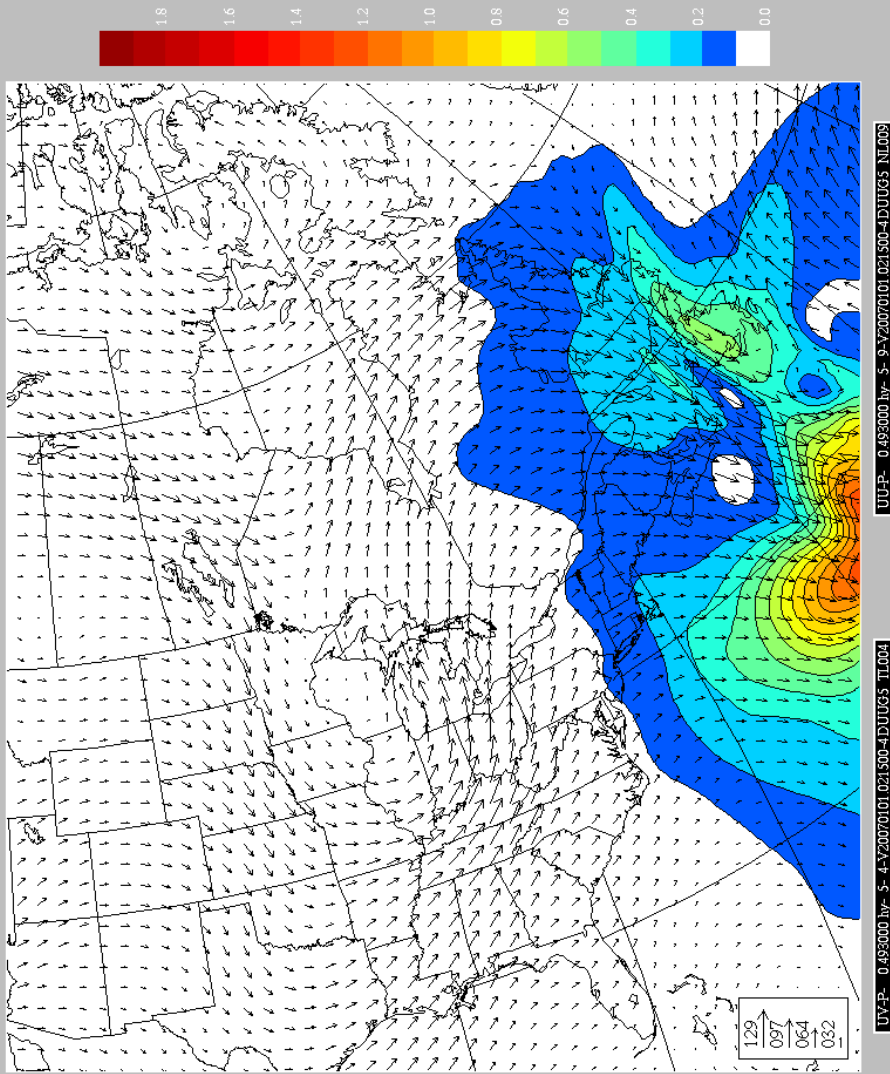
4D-Var GLB 170km



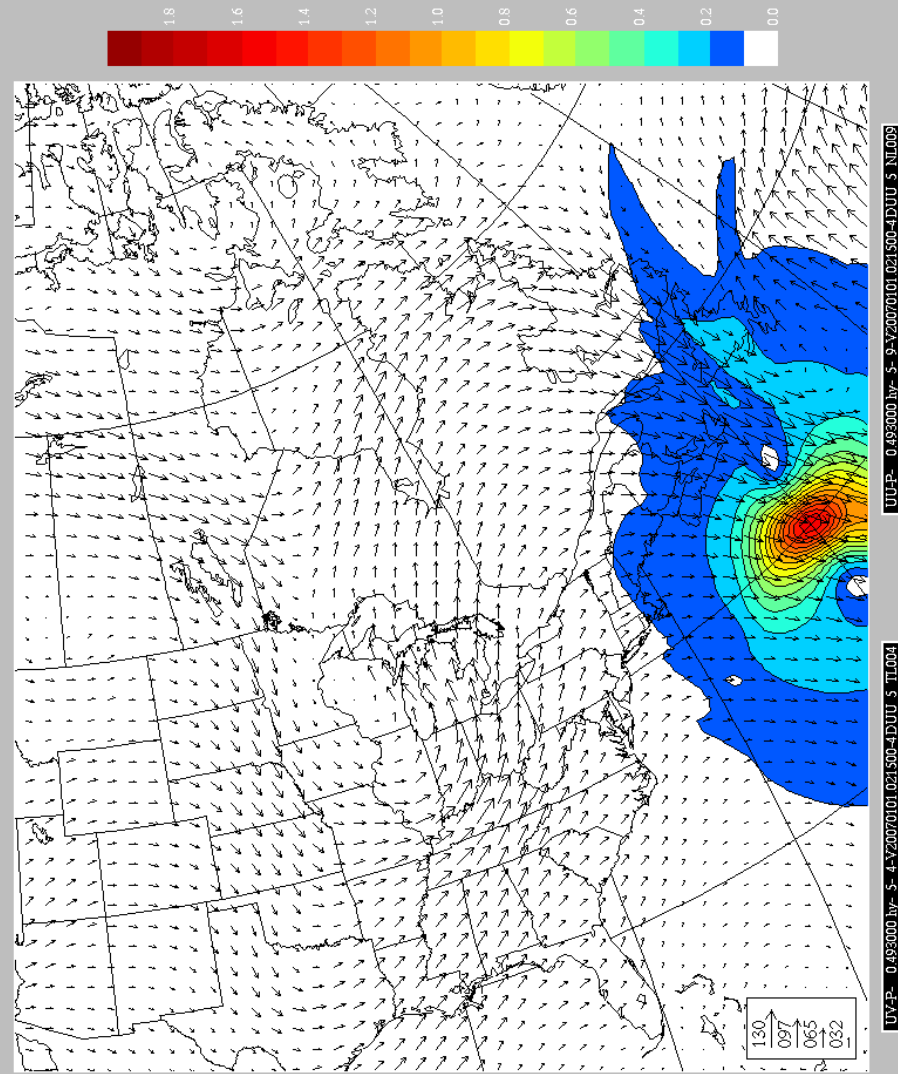
4D-Var LAM 55km

T = +1.30 hr





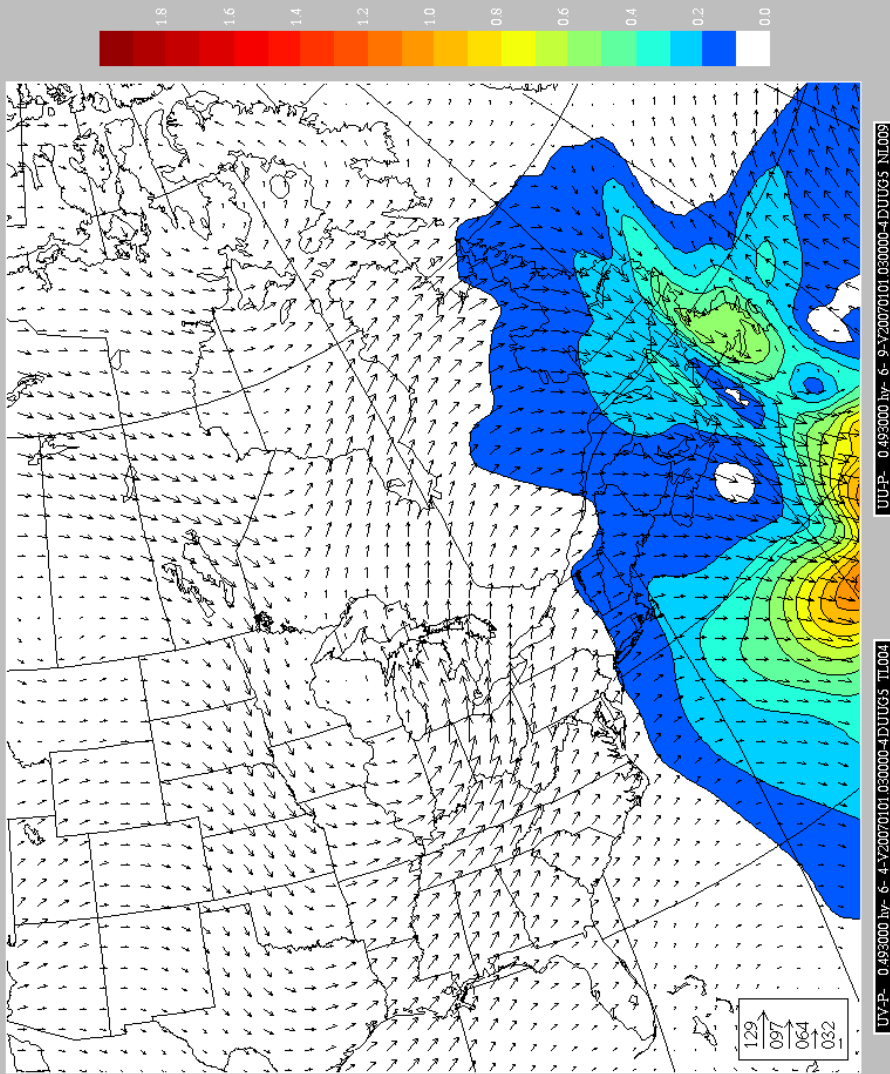
4D-Var GLB 170km



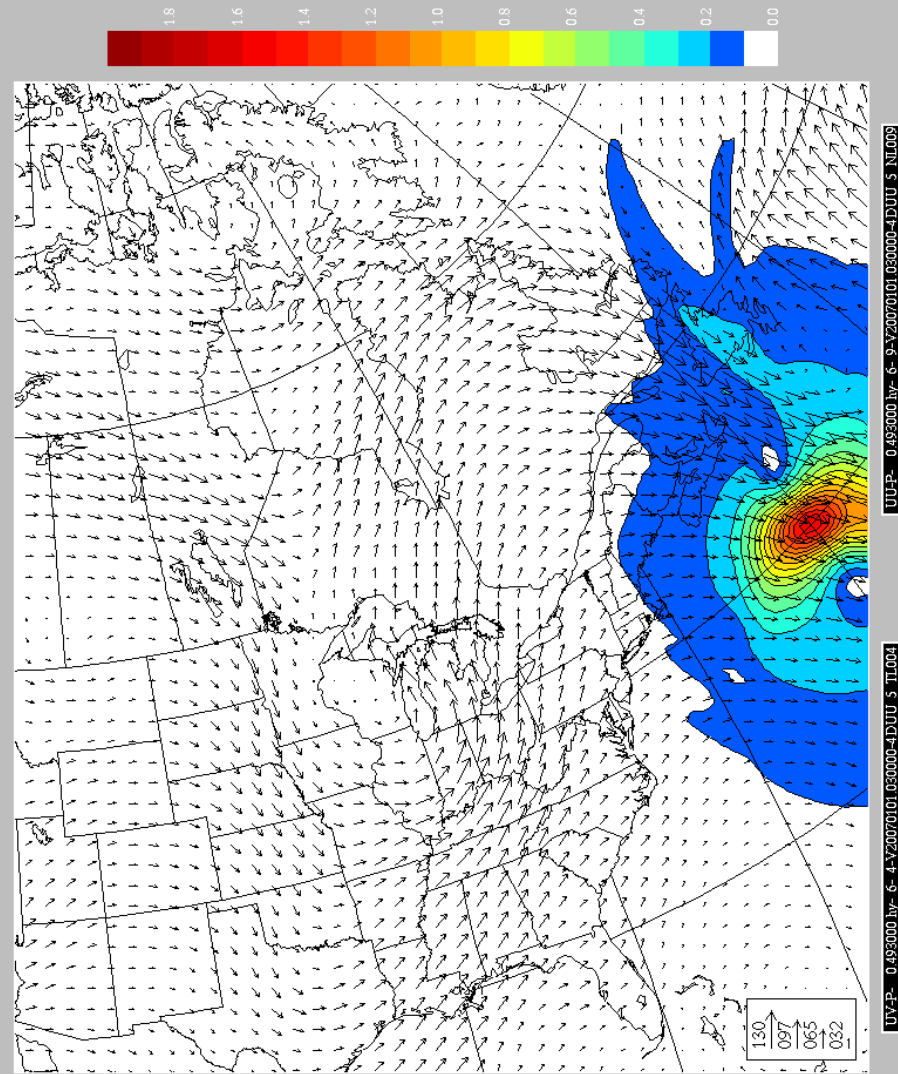
4D-Var LAM 55km

T = +2.15 hr





4D-Var GLB 170km



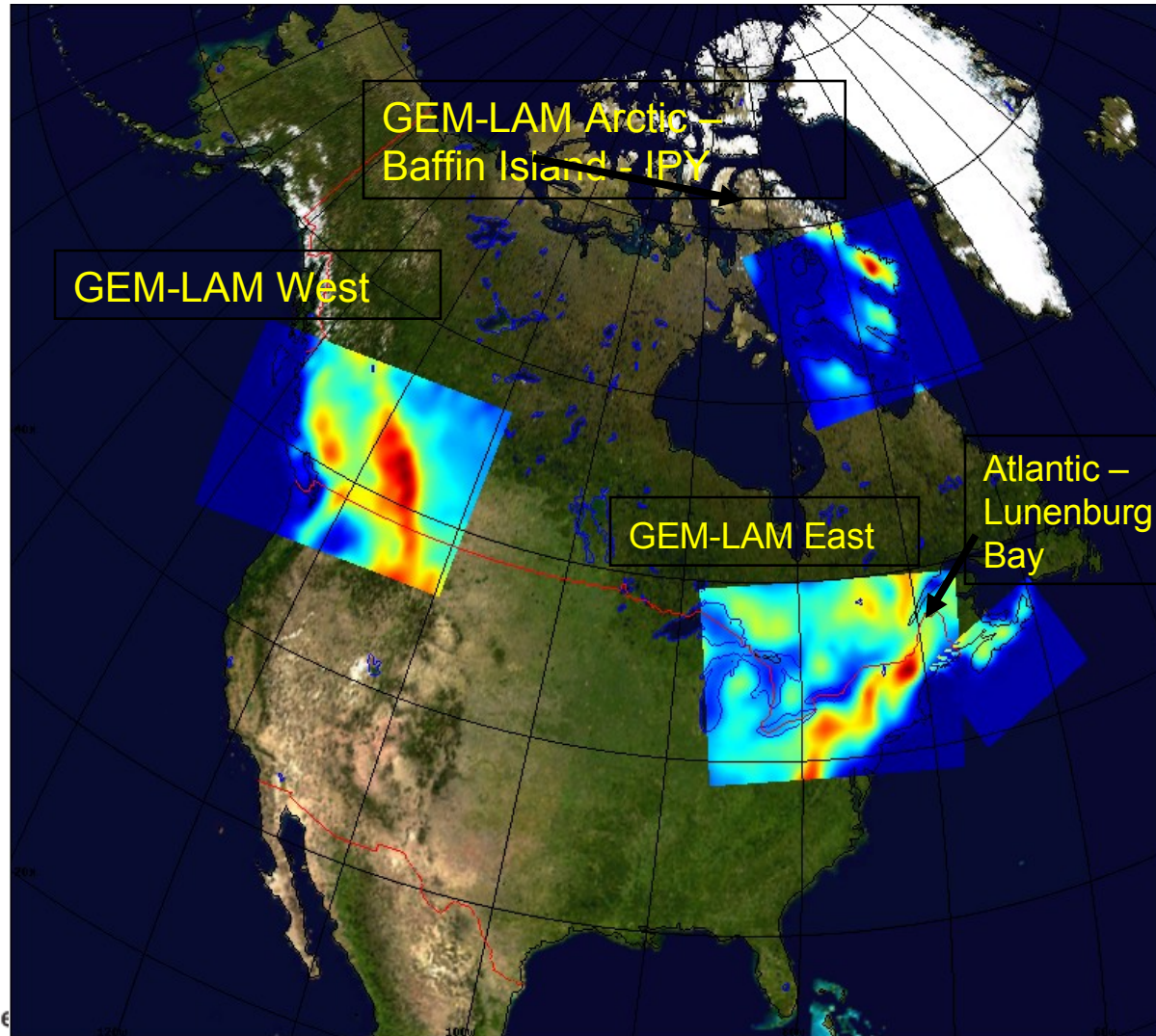
4D-Var LAM 55km

T = +3.00 hr



Current local very high resolution windows

Also 1-km window for 2010 winter Olympics

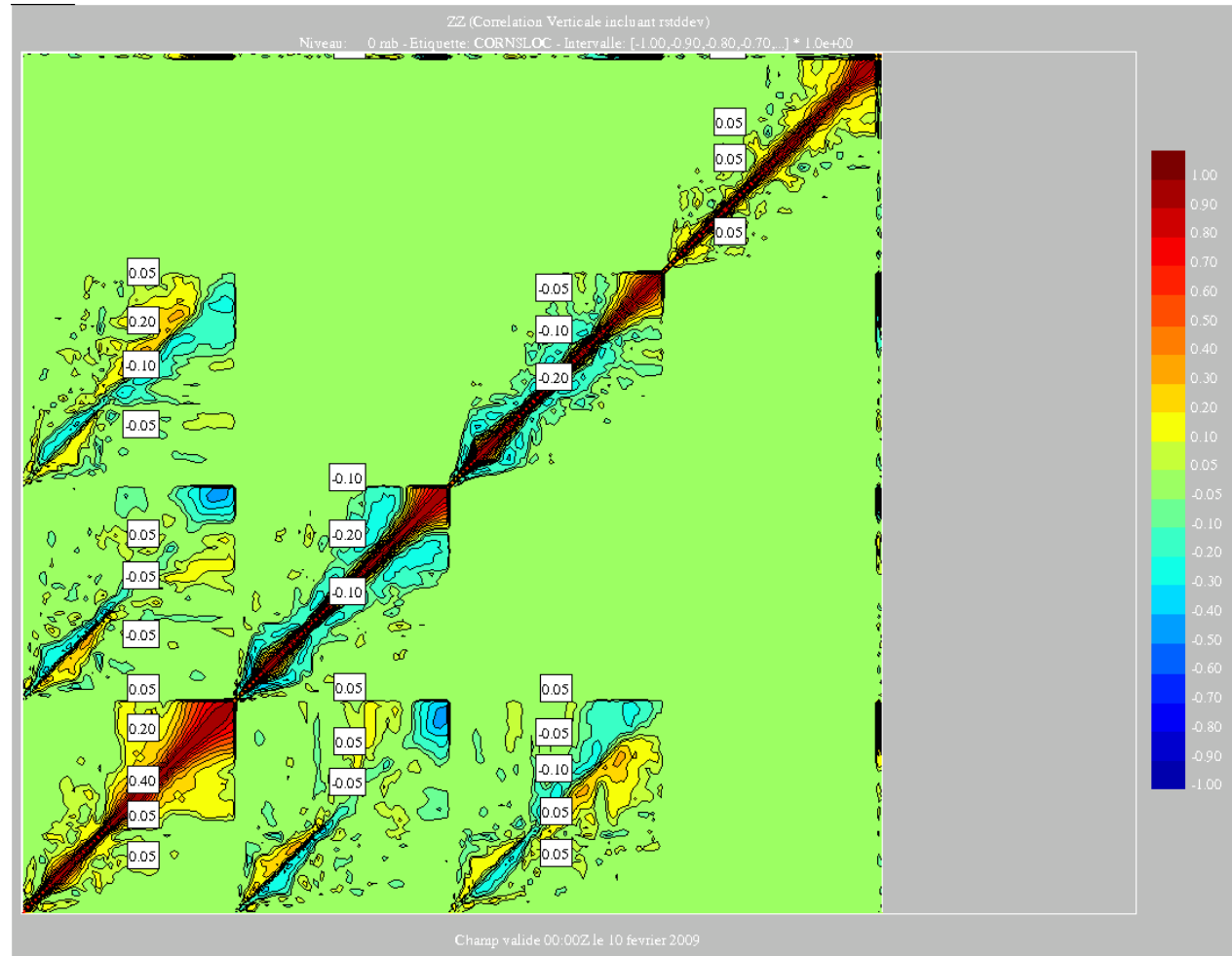


VO-LAM3D-15km

3000 km x 2500 km domain

NMC-12-06h GEM-15km LAM Fcst diff; 150 samples (FEB-Mar 09)

k = 5



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Canada

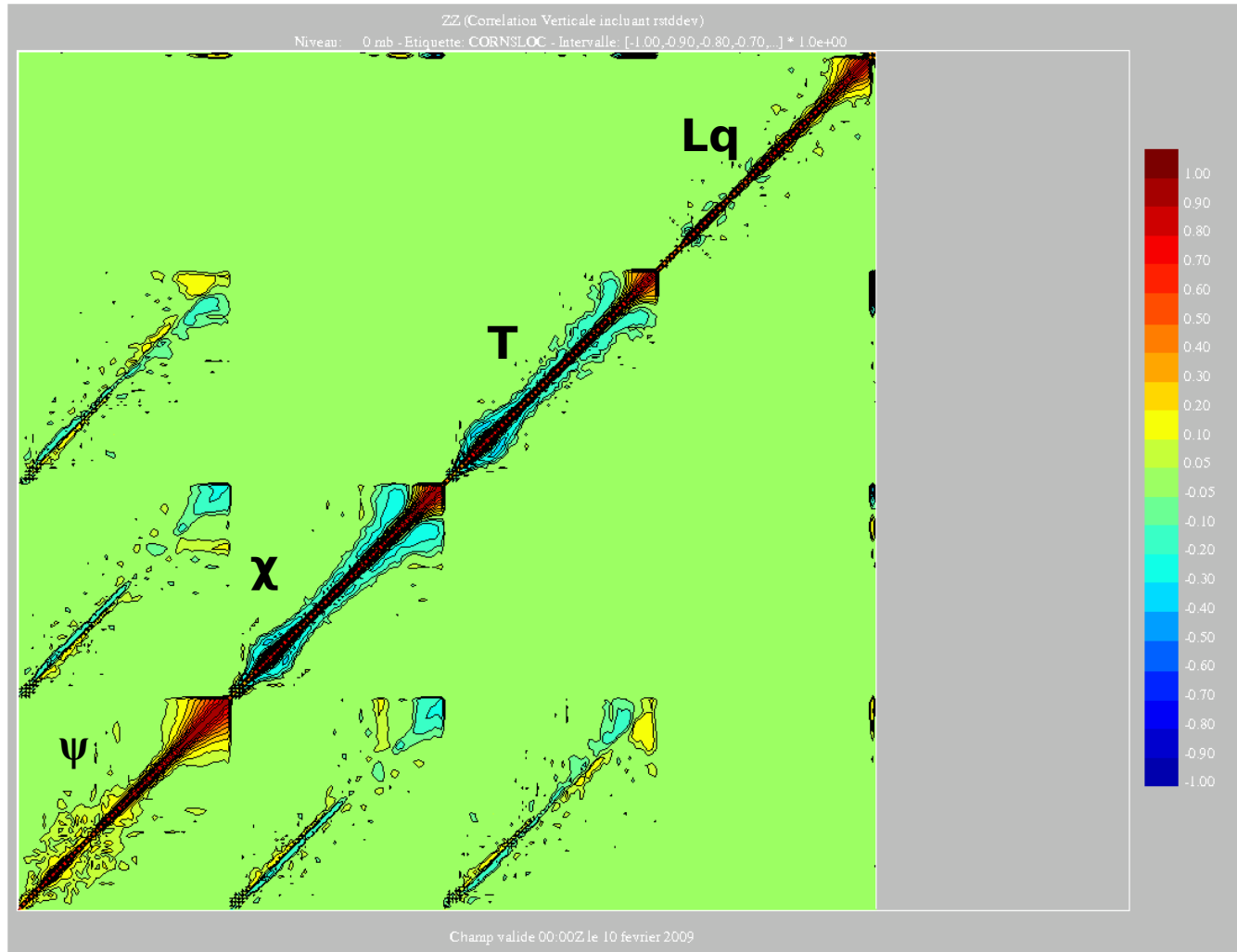
Canada

VO-LAM3D-15km

3000 km x 2500 km domain

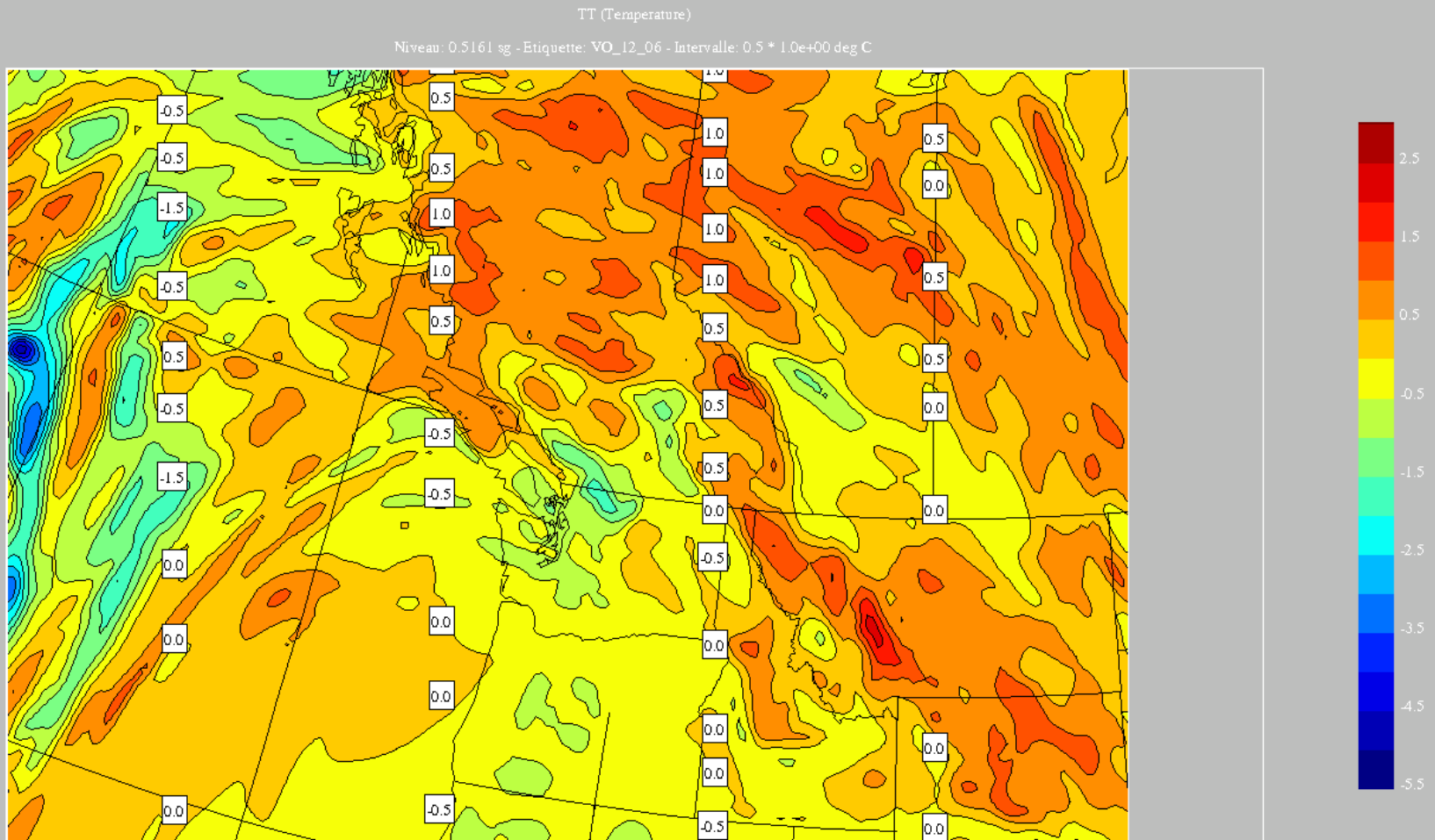
NMC-12-06h GEM-15km LAM Fcst diff; 150 samples (FEB-Mar 09)

k = 25



Temperature forecast error at 500 hPa

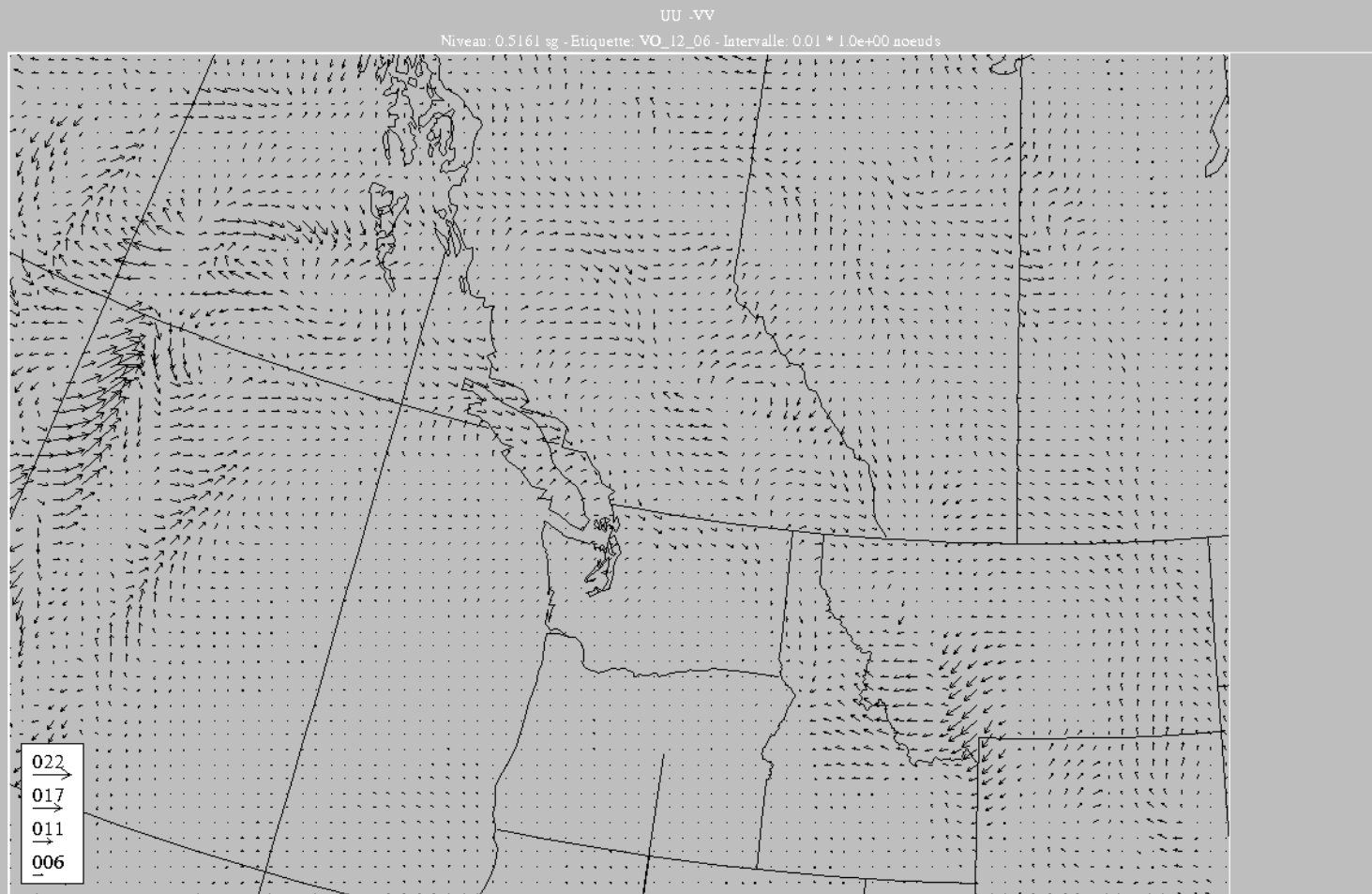
NMC-12-06h GEM-15km LAM Fcst diff; 150 samples (FEB-Mar 09)



Differences a 00 heures valides 12:00Z le 02 fevrier 2009

Wind forecast error at 500 hPa 12h-06h LAM-15km forecasts

NMC-12-06h GEM-15km LAM Fcst diff; 150 samples (FEB-Mar 09)



Differences a 00 heures valides 12:00Z le 02 fevrier 2009

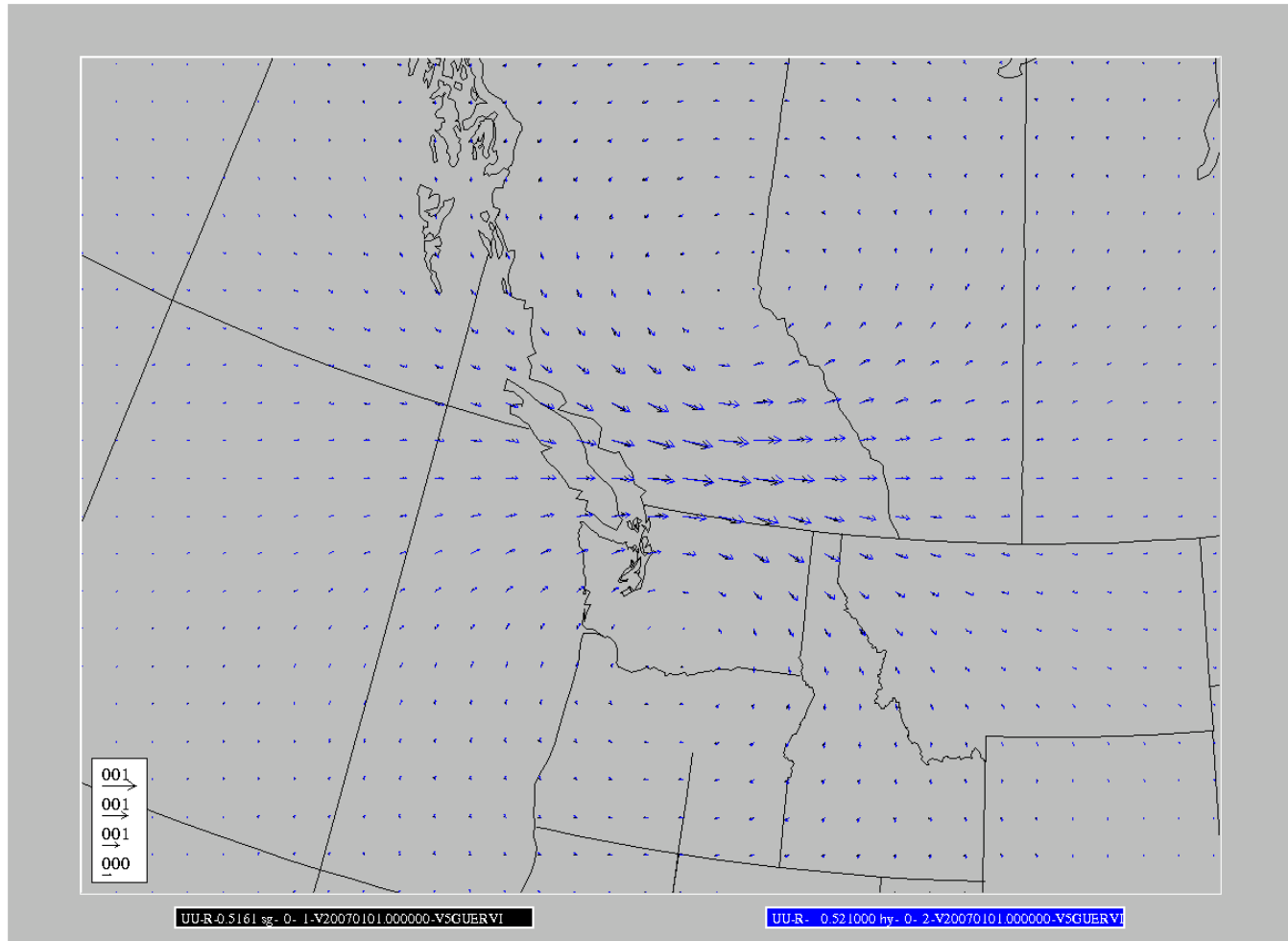


Environment
Canada

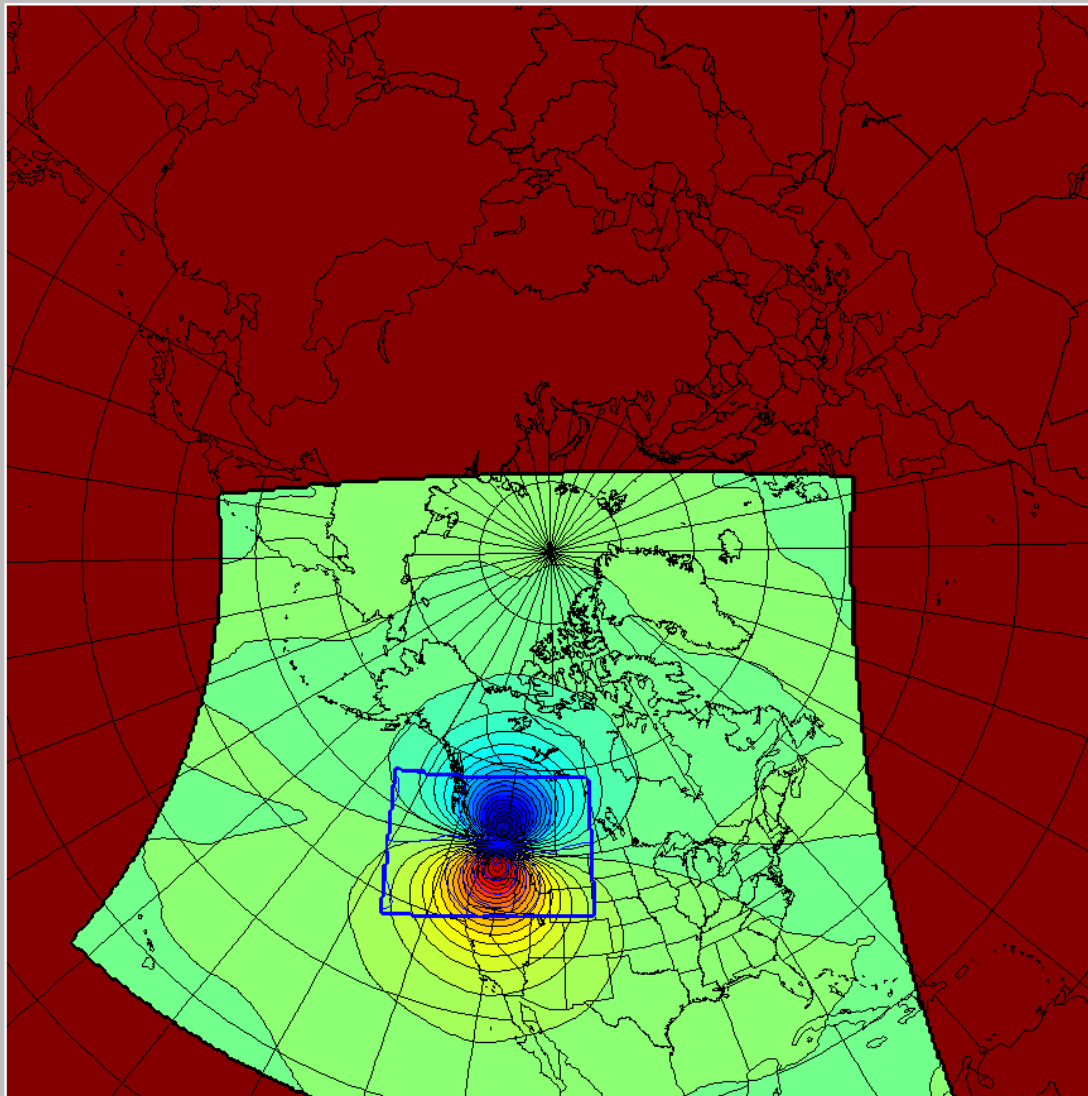
Environnement
Canada

Canada

TT Incr. 700 hPa; 1-Obs-UU-500 hPa LU-15km versus LU-55 km



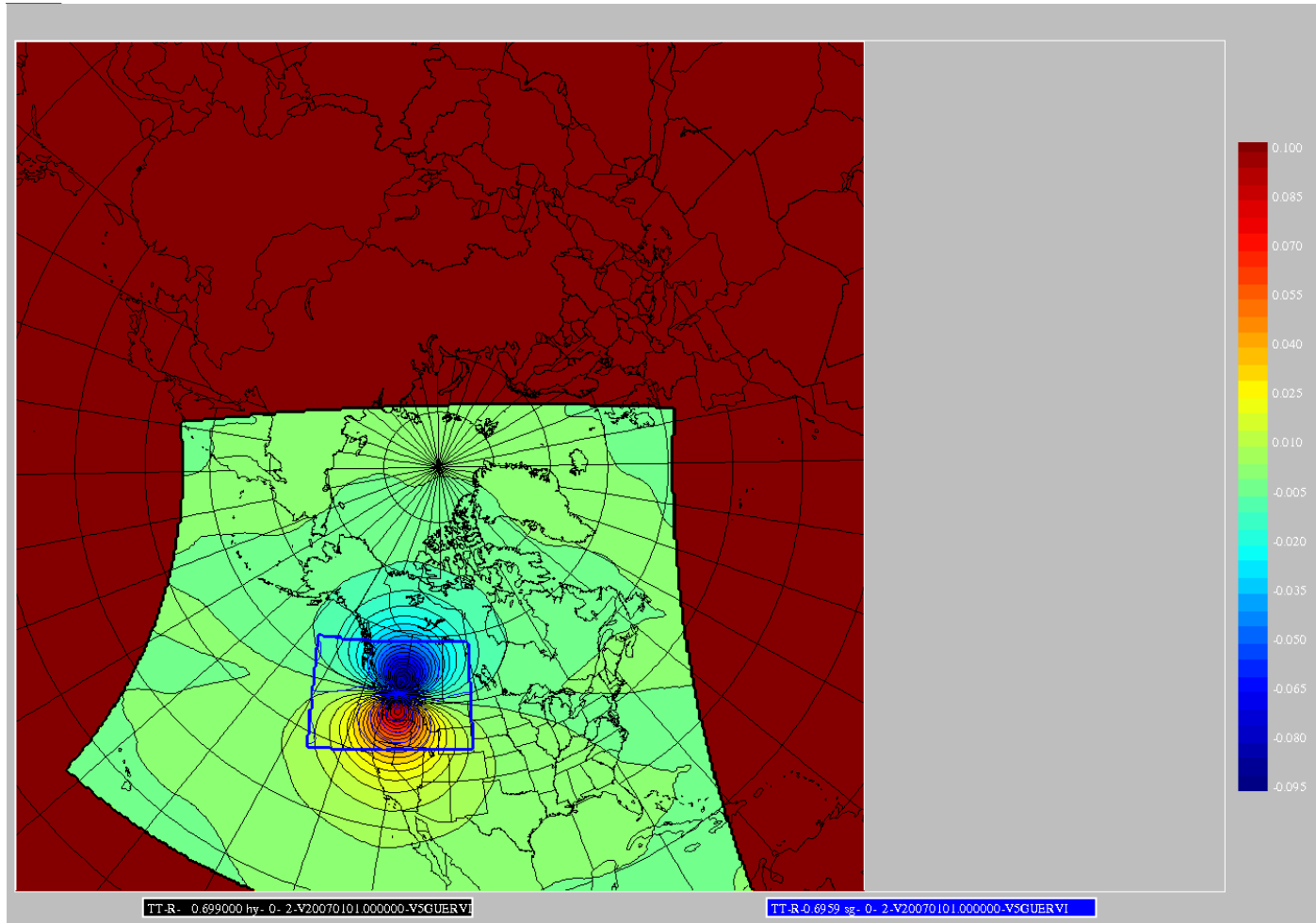
TT Incr. 700 hPa; 1-Obs-UU-500 hPa LU-15km versus LU-55 km



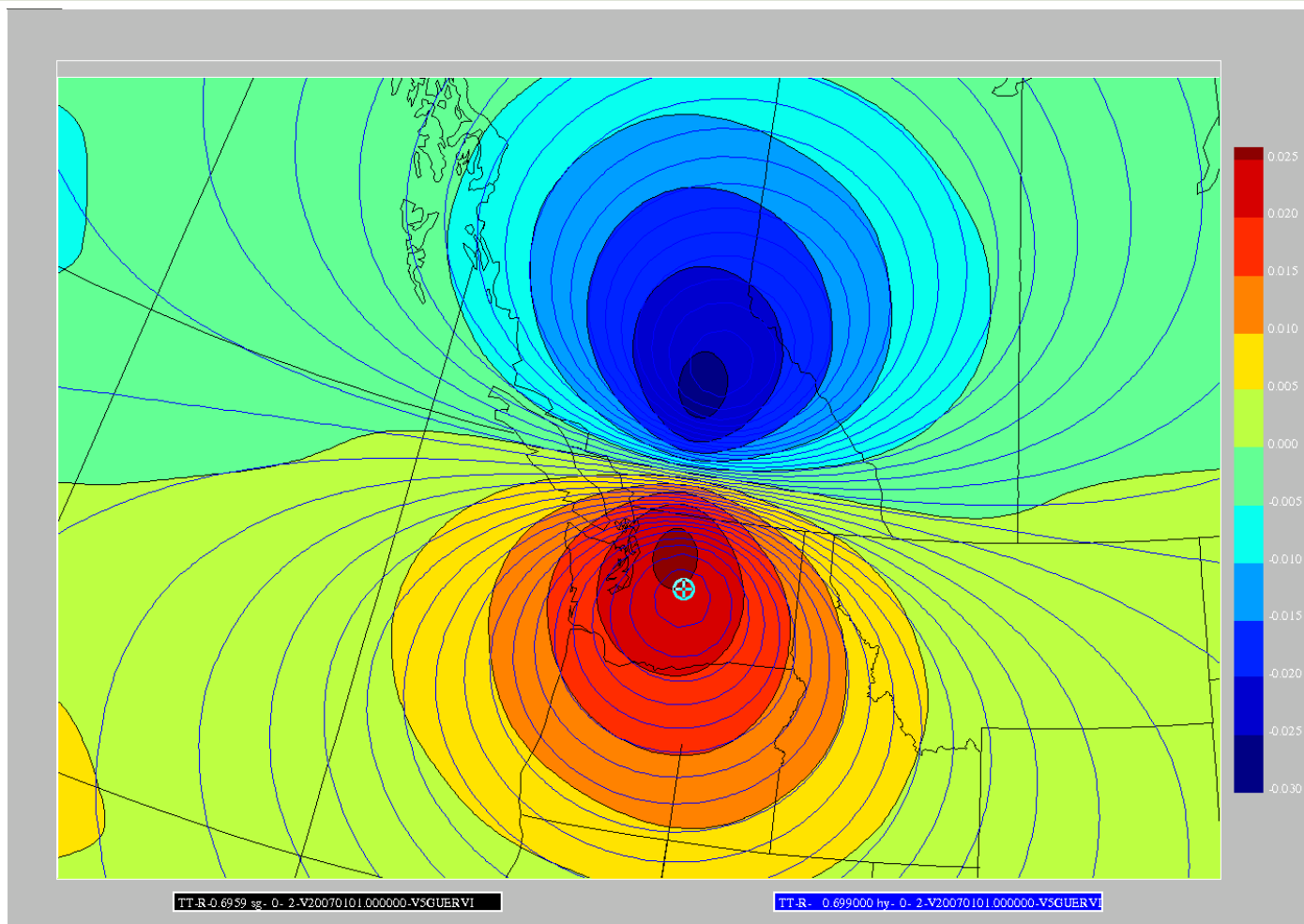
TT-R- 0.699000 hy- 0- 2-V20070101.000000-V5GUERVI

TT-R-0.6959 sg- 0- 2-V20070101.000000-V5GUERVI

TT Incr. 700 hPa; 1-Obs-UU-500 hPa LU-15km versus LU-55 km

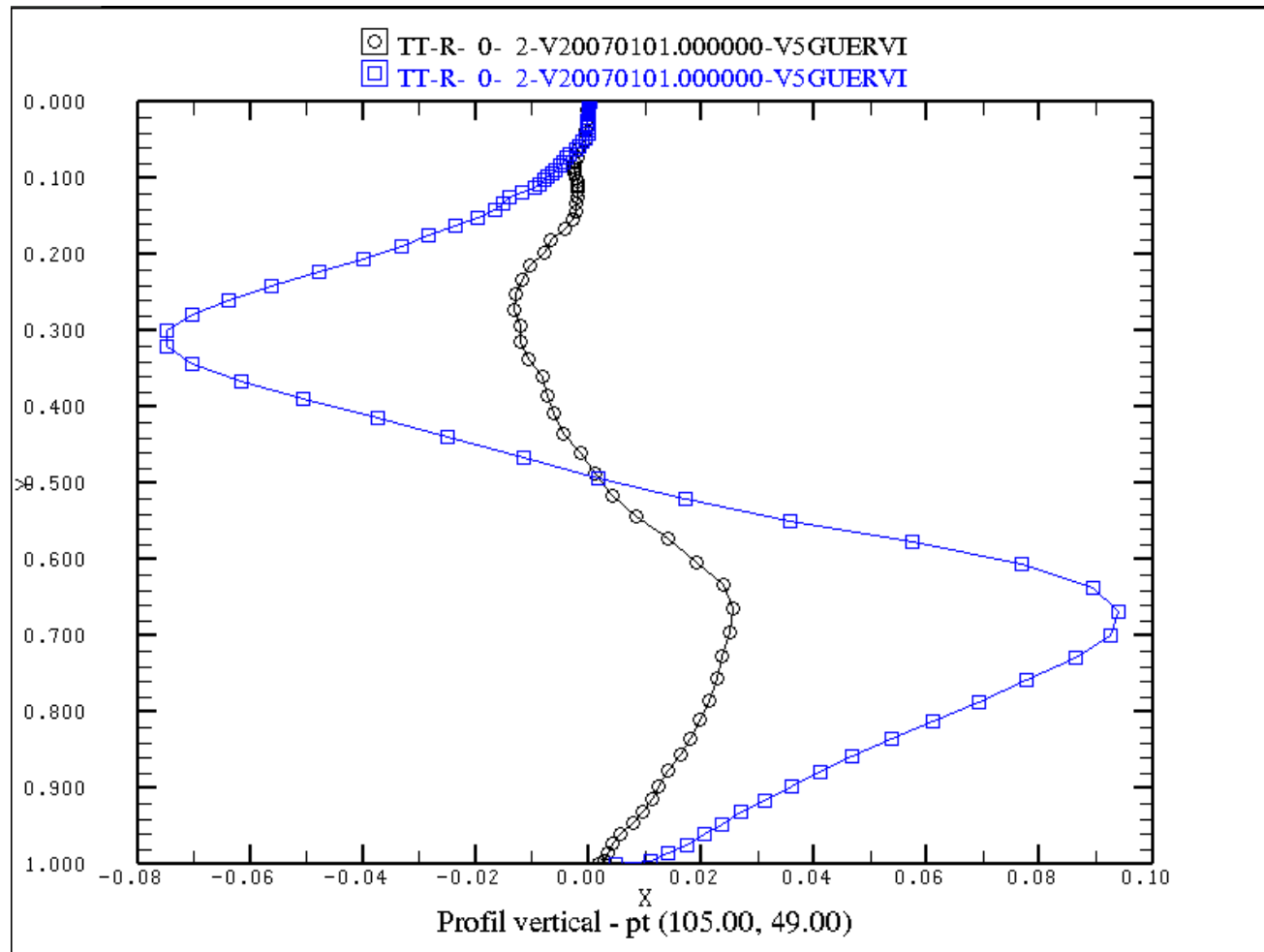


TT Incr. 700 hPa; 1-Obs-UU-500 hPa Lu-15 km versus LU-55 km

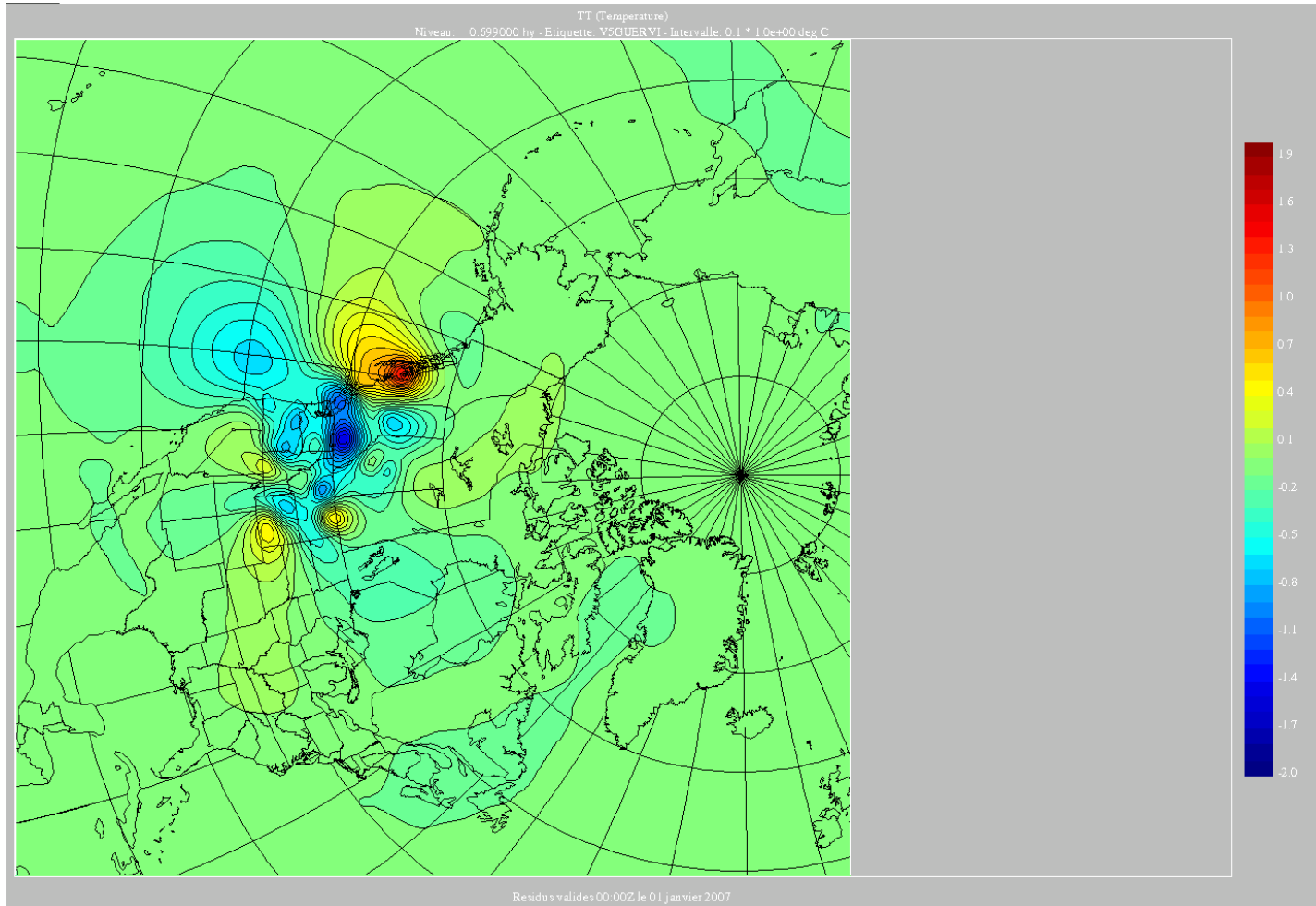


TT Incr. Over Center H

Lu-15 km versus LU-55 km

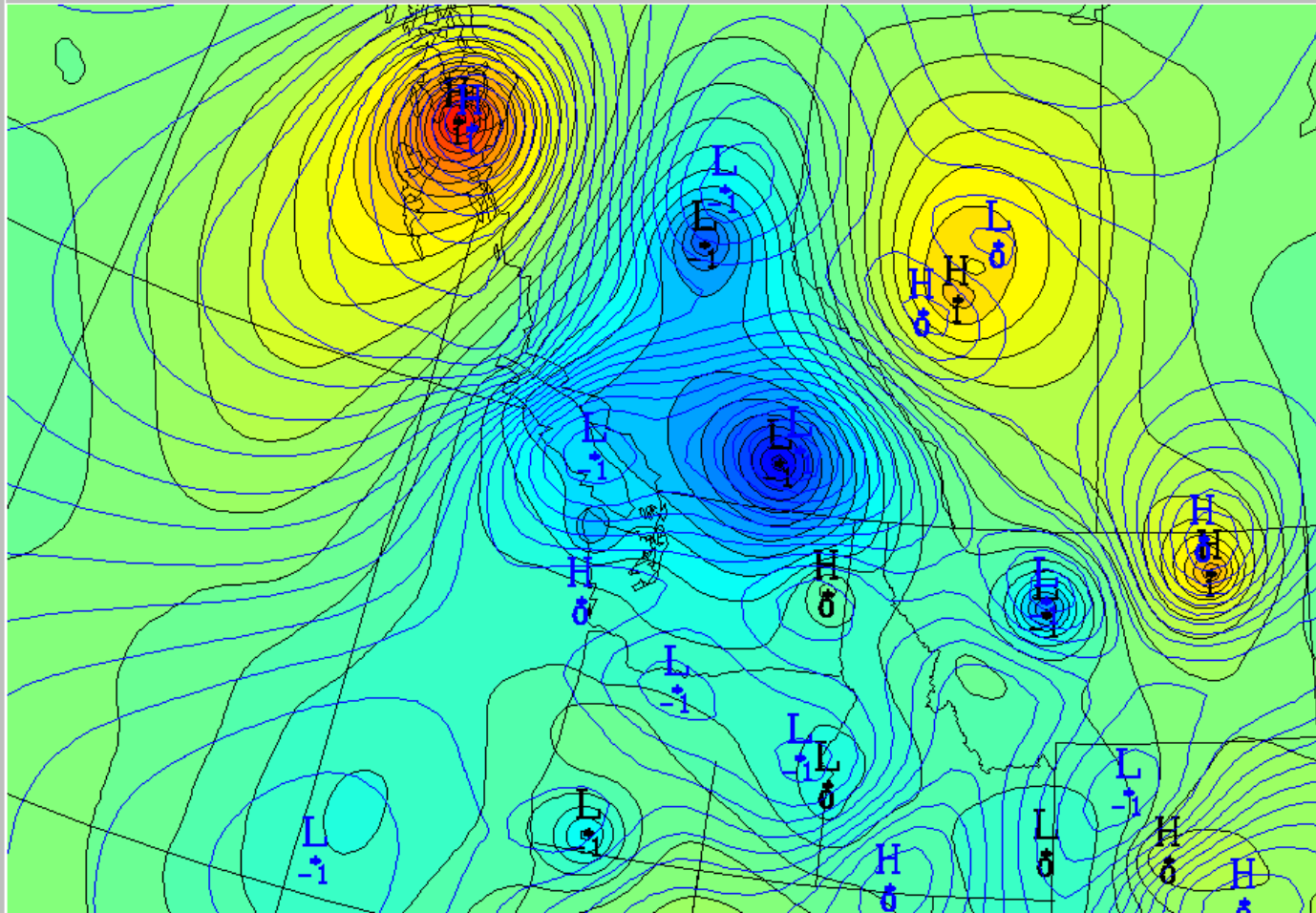


Radiosonde data, TT incr. 500 hPa, LU-55km



Radiosonde data

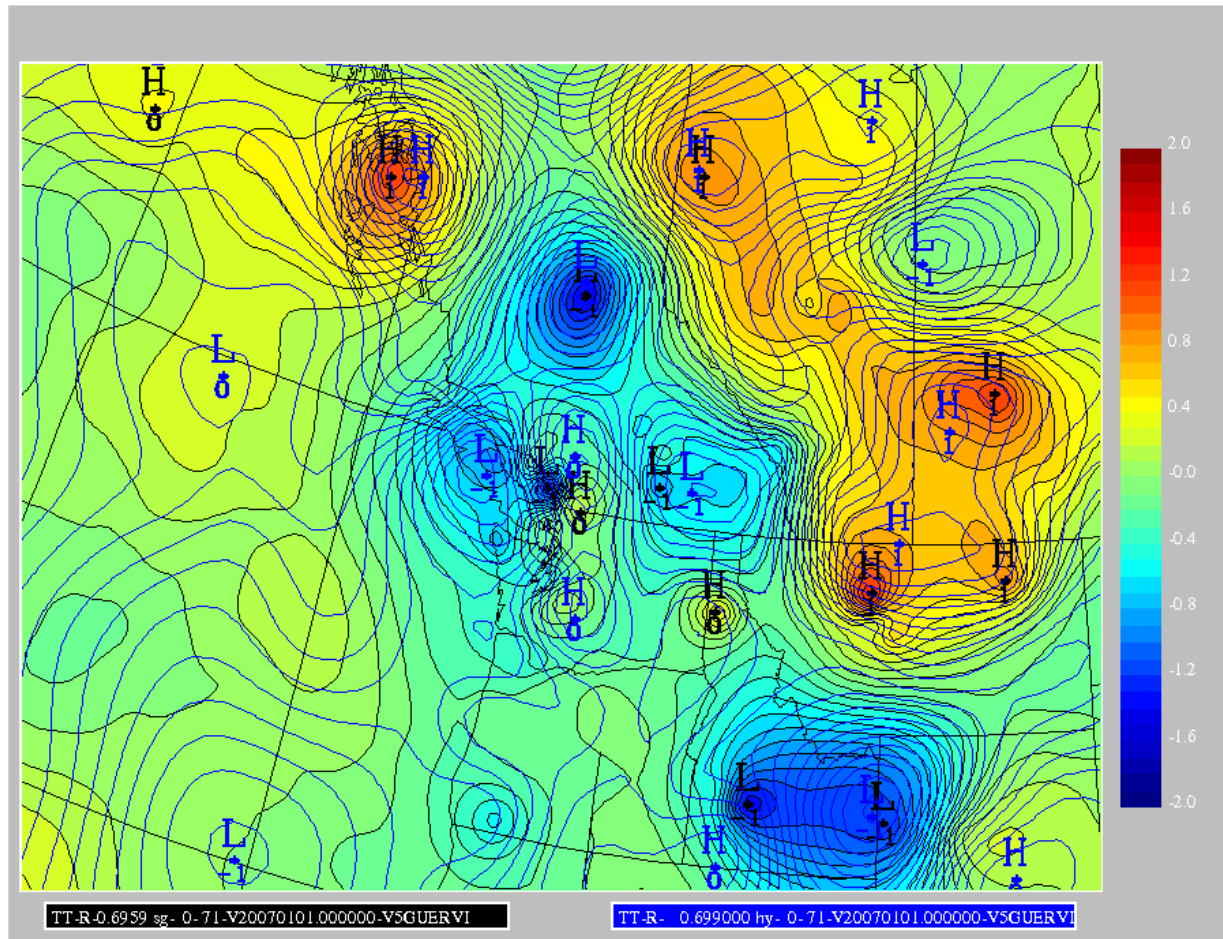
TT incr. 700 hPa, LU-15 versus LU-55km



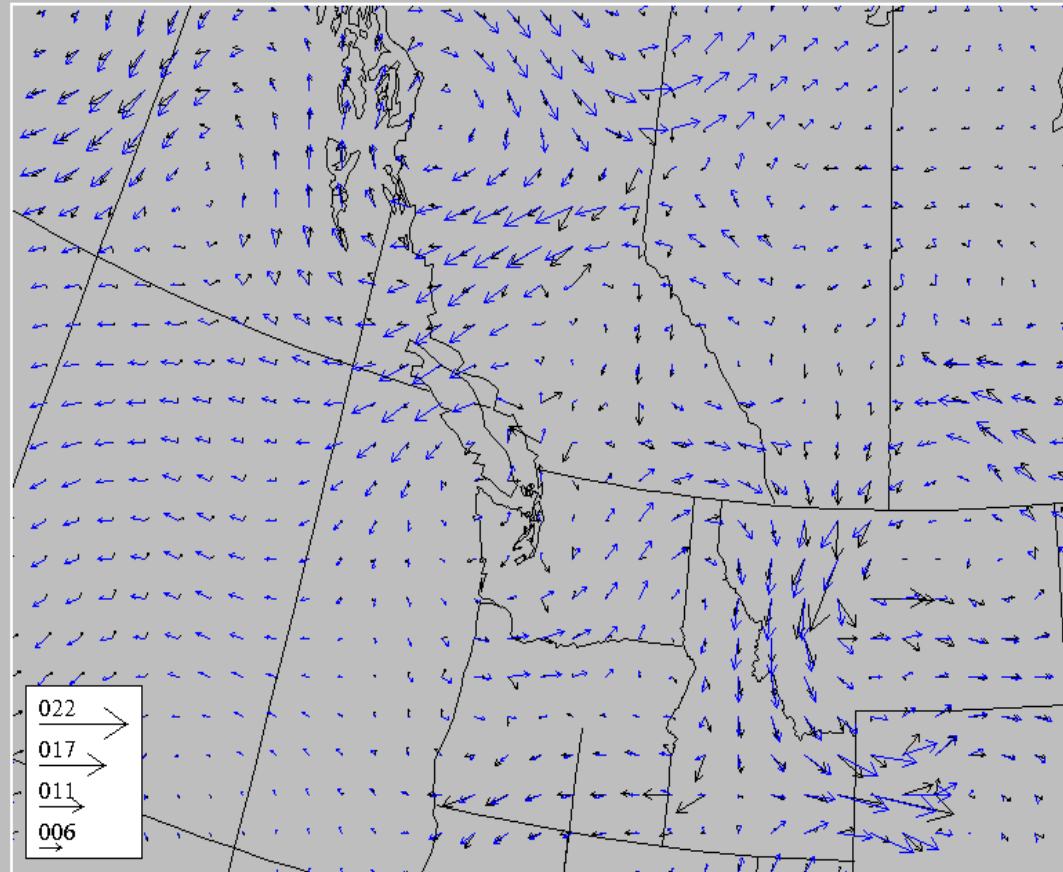
TT-R-0.6959 sg- 0- 31-V20070101.000000-V5GUERVI

TT-R- 0.699000 hy- 0- 71-V20070101.000000-V5GUERVI

TT incr. 700 hPa, LU-15 km versus LU-55 km: Data assimilated: ua, ai, sw, sf, to, bo, go, pr, sc, ro



Wind incr. 700 hPa, LU-15 km versus LU-55 km: Data assimilated: ua, ai, sw, sf, to, bo, go, pr, sc, ro



UU-R-0.6959 sg- 0-71-V20070101.000000-V5GUERV1

UU-R- 0.699000 hy- 0-71-V20070101.000000-V5GUERV1

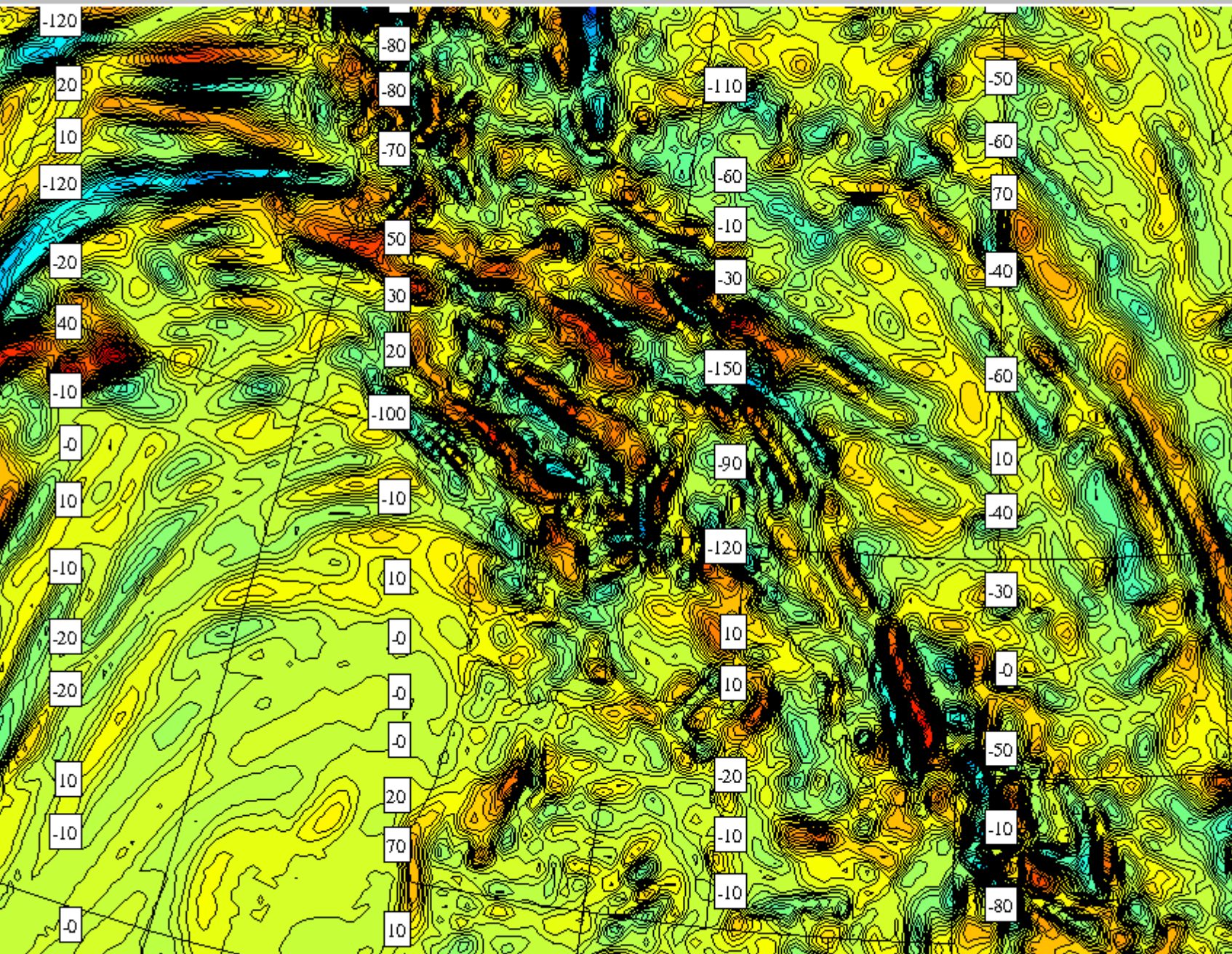


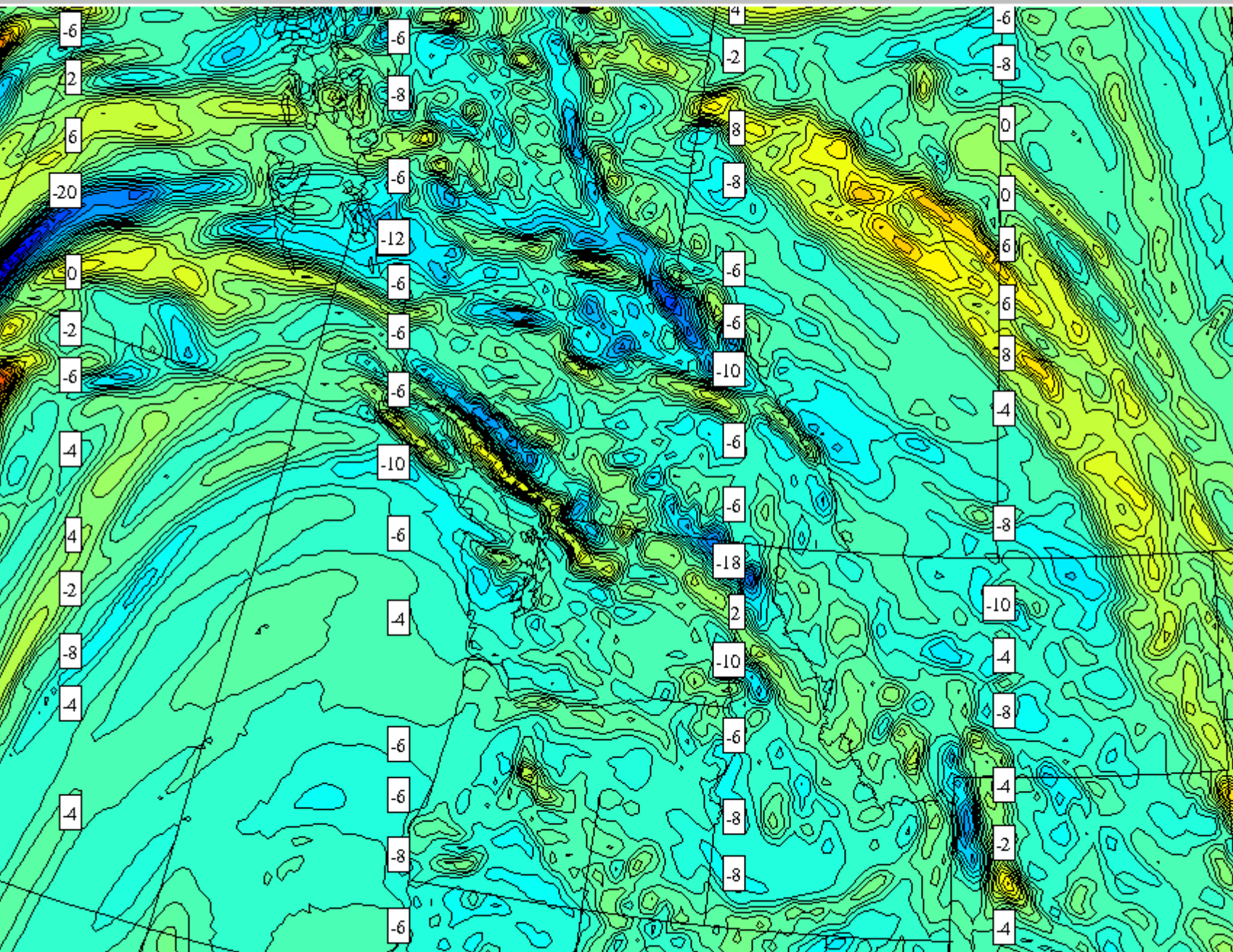
VO-LAM-3D, 2.5km

- Generate 2.5km forecast error samples (Mailhot et al. Sept 2009)
- Compute B statistics, NMC-type at 2.5 km.(Sept. 2009)
- Examine Impact of VO-LAM-3D, 15km & 2.5km on GEM-2.5 forecasts. (CMC collaboration).

QC-VAR-3D-1km: Radar Data Assimilation EC-McGill Collaboration (Zawadzki et al)

- Perform NMC-6h Background error statistics at 2.5 km over QC-Grid. Ensemble approach to be explored also.
 - Implement radial wind observation operator
 - Etc...
 - Work starting Sept. 2009. Kao-Shen Chung PhD. At McGill to assist.
-







Spherical Harmonics

$$\nabla^2 Y_n^m = -\frac{n(n+1)}{a^2} Y_n^m \quad Y_n^m = P_n^m(\mu) e^{im\lambda}$$

Bi-Fourier

$$\nabla^2 = \frac{1}{a^2 \cos^2 \theta} \left\{ \frac{\partial^2}{\partial \lambda^2} + \cos \theta \frac{\partial}{\partial \theta} \left(\cos \theta \frac{\partial}{\partial \theta} \right) \right\} \quad \approx \frac{1}{a^2 \cos^2 \theta} \frac{\partial^2}{\partial \lambda^2} + \frac{1}{a^2} \frac{\partial^2}{\partial \theta^2} \approx \frac{1}{a^2} \frac{\partial^2}{\partial \lambda^2} + \frac{1}{a^2} \frac{\partial^2}{\partial \theta^2} = \frac{1}{a^2} \left(\frac{\partial^2}{\partial \lambda^2} + \frac{\partial^2}{\partial \theta^2} \right)$$

$$\left(\frac{\omega_{j+1,l} - 2\omega_{j,l} + \omega_{j-1,l}}{(\Delta\lambda)^2} \right) = \frac{e^{2\pi i m l / J} + e^{-2\pi i m l / J} - 2}{(\Delta\lambda)^2} = p(m) = \frac{2 \left[\cos \left(\frac{2\pi m}{Nl} - 1 \right) \right]}{(\Delta\lambda)^2}$$

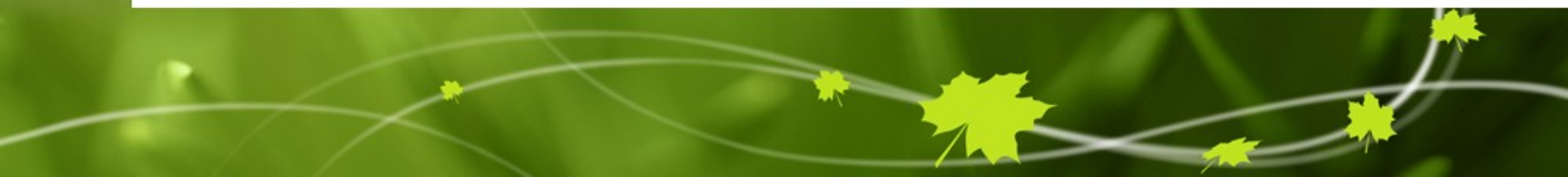
$$\nabla_{m,n}^2 = \frac{1}{a^2} (p(m) + q(n)) \quad q(n) = \frac{2 \left[\cos \left(\frac{2\pi n}{Nj} - 1 \right) \right]}{(\Delta\theta)^2}$$

if $\Delta\lambda = \Delta\theta$

$$\nabla_{m,n}^2 = \frac{2}{a^2 \Delta^2} \left[\cos \left(\frac{2\pi m}{Nl} \right) + \cos \left(\frac{2\pi n}{Nj} \right) - 2 \right]$$

$\text{rlaplam}(m, n)$

$$\nabla_{m,n}^{-2} = \text{rilamlam}(m, n) = 1.0 / \text{rlaplam}(m, n); 0 \text{ for } (m, n) = (0, 0)$$



LAM-Var Arakawa-C Analysis Grid

Ψ_{03}	V_{13}	Ψ_{13}	V_{23}	Ψ_{23}	V_{33}	Ψ_{33}	V_{43}	Ψ_{43}
U_{03}	χ_{13}	U_{13}	χ_{23}	U_{23}	χ_{33}	U_{33}	χ_{43}	U_{43}
Ψ_{02}	V_{12}	Ψ_{12}	V_{22}	Ψ_{22}	V_{32}	Ψ_{32}	V_{42}	Ψ_{42}
χ_{32}	U_{02}	χ_{12}	U_{12}	χ_{22}	U_{22}	χ_{32}	U_{32}	U_{42}
Ψ_{01}	V_{11}	Ψ_{11}	V_{21}	Ψ_{21}	V_{31}	Ψ_{31}	V_{41}	Ψ_{41}
χ_{41}	U_{01}	χ_{11}	U_{11}	χ_{21}	U_{21}	χ_{31}	U_{31}	U_{41}
Ψ_{00}	V_{10}	Ψ_{10}	V_{20}	Ψ_{20}	V_{30}	Ψ_{30}	V_{40}	Ψ_{40}
	χ_{10}		χ_{20}		χ_{30}			



$$(\psi, \chi) \rightarrow (U, V) \rightarrow (\zeta, D) \rightarrow (\psi, \chi)$$

$$\zeta = \frac{1}{a \cos^2 \theta} \left(\frac{\partial V}{\partial \lambda} - \cos \theta \frac{\partial U}{\partial \theta} \right) ; \quad U = u \cos \theta \quad D = \frac{1}{a \cos \theta} \left(\frac{\partial u}{\partial \lambda} + \frac{\partial (v \cos \theta)}{\partial \theta} \right)$$

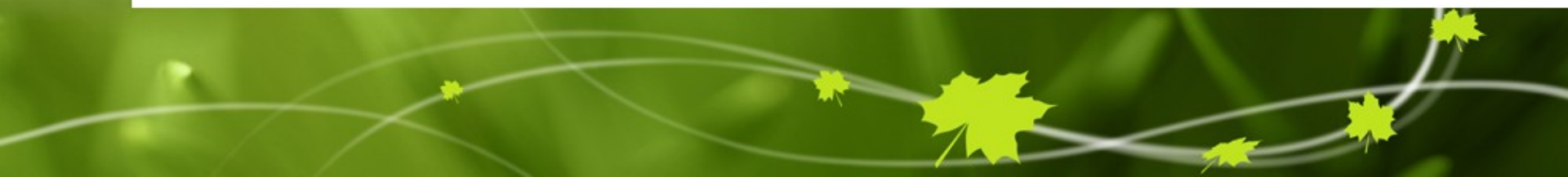
Using wind-images we have:

$$\zeta = \frac{1}{a \cos \theta} \left(\frac{\partial v}{\partial \lambda} - \frac{\partial (u \cos \theta)}{\partial \theta} \right) \quad D = \frac{1}{a \cos^2 \theta} \left(\frac{\partial U}{\partial \lambda} + \cos \theta \frac{\partial V}{\partial \theta} \right) ; \quad V = v \cos \theta$$

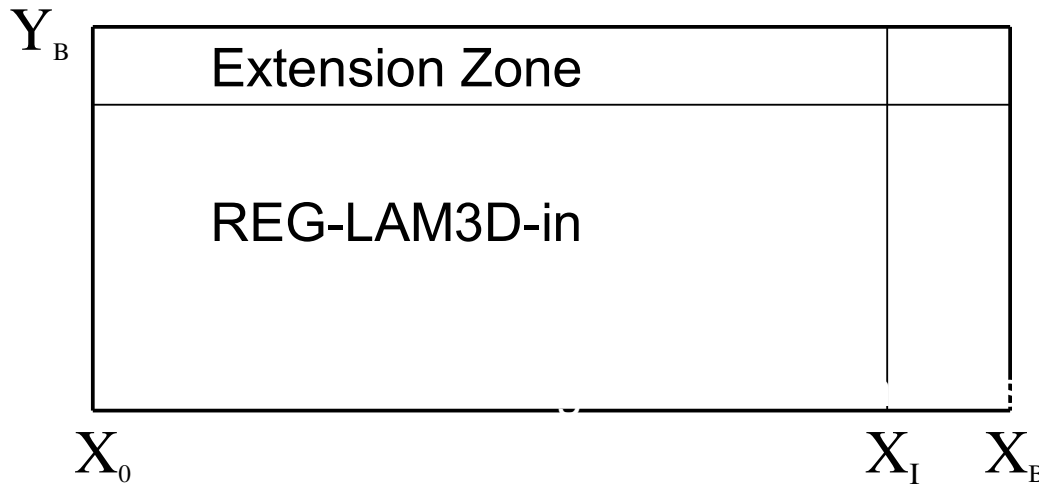
According to the placement of ζ, D variables on the computational grid, we get the discretized version as:

$$D^{i,j} = \frac{1}{a \cos^2 \theta_j} \frac{U^{i+\frac{1}{2},j} - U^{i-\frac{1}{2},j}}{\Delta \lambda_{i+\frac{1}{2}}} + \frac{1}{a} \frac{V^{i,j+\frac{1}{2}} - V^{i,j-\frac{1}{2}}}{\Delta \mu_j}$$

$$\zeta^{i+\frac{1}{2},j+\frac{1}{2}} = \frac{1}{a \cos^2 \theta_{j+\frac{1}{2}}} \frac{V^{i+1,j+\frac{1}{2}} - V^{i,j+\frac{1}{2}}}{\Delta \lambda_{i+\frac{1}{2}}} - \frac{1}{a} \frac{U^{i+\frac{1}{2},j+1} - U^{i+\frac{1}{2},j}}{\Delta \mu_{j+\frac{1}{2}}}$$



Machenhauer's extension's procedure



$$g(x, y) = a_0(y) + a_1(y) \cos x' + b_1(y) \sin x' + b_2(y) \sin 2x'$$

where

$$x' \equiv \pi \frac{(x - x_I)}{(x_B - x_I)}$$

$$a_0 = g(x_I) + g(0)$$

$$a_1 = [g(x_I) - g(x_B)] / 2$$

$$b_1 = [g'(x_I) - g'(0)] / 2\alpha$$

$$b_2 = [g'(x_I) + g'(x_B)] / 4\alpha$$

$$g'(x_I) = (g(x_I) - g(x_I - \Delta x)) / \Delta x$$

$$g'(x_B) = g'(0) = (g(\Delta x) - g(0)) / \Delta x$$

The extension is carried out first in the x-direction and then in the y-direction.



$$\begin{aligned}
 \{ \} &= \frac{a_j}{a^2 \Delta\mu_j \Delta\bar{\mu}_{j-1}} \psi^{i,j-1} - \frac{1}{a^2 \Delta\mu_j} \left[\frac{\cos^2 \theta_j}{\Delta\bar{\mu}_{j-1}} + \frac{\cos^2 \theta_{j+1}}{\Delta\bar{\mu}_j} \right] \psi^{i,j} + \frac{c_j}{a^2 \Delta\mu_j \Delta\bar{\mu}_j} \psi^{i,j+1} \\
 &\quad + \frac{1}{a \cos^2 \bar{\theta}_j} \frac{\partial^2 \psi}{\partial \lambda^2} \\
 &= a_j \psi^{i,j-1} - (a_j + c_j) \psi^{i,j} + c_j \psi^{i,j+1} + \frac{1}{a \cos^2 \bar{\theta}_j} \frac{\partial^2 \psi}{\partial \lambda^2}
 \end{aligned}$$

$$\omega_j(\theta) = \frac{1}{J} \sum_{m=0}^{j-1} \tilde{\omega}_m(\theta) E^{mj} \quad ; \quad E^{mj} \equiv e^{2\pi i jm/J}$$

$$\left(\frac{\omega_{j+1,l} - 2\omega_{j,l} + \omega_{j-1,l}}{(\Delta\lambda)^2} \right) \quad \Delta\lambda_i = \lambda_{i+1} - \lambda_i \quad ; \quad i=1, \dots, NI-1 \quad ; \quad \Delta \sin \theta_j = \sin \theta_{j+1} - \sin \theta_j \quad ; \quad j=1, \dots, NJ-1$$

$$a_l \tilde{\omega}_{m,l-1} + b_l \tilde{\omega}_{m,l} + c_l \tilde{\omega}_{m,l+1} = \tilde{R}_{m,l}$$

$$\mathbf{A}_\theta \equiv \begin{bmatrix} b_1 & c_1 & 0 & \dots & 0 & 0 & \beta \\ a_2 & b_2 & c_2 & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & \dots & a_{L-1} & b_{L-1} & c_{L-1} \\ \alpha & 0 & 0 & \dots & 0 & a_L & b_L \end{bmatrix}$$

Wind-rotations (uvrot2uv.ftn, auvrot2uv.ftn)

Step 1

$$\mathbf{v} = \frac{dr}{dt} = \frac{dx}{dt} \mathbf{i} + \frac{dy}{dt} \mathbf{j} + \frac{dz}{dt} \mathbf{k} = \mu \hat{\lambda} + v \hat{\theta}$$

$$v_x = -\sin \lambda \mu - \cos \lambda \sin \theta v ;$$

$$v_y = \cos \lambda \mu - \sin \lambda \sin \theta v$$

$$v_z = \cos \theta v$$

Step 2

$$\begin{bmatrix} v_x \\ v_y \\ v_z \end{bmatrix} = \mathcal{R}^T \begin{bmatrix} v_x' \\ v_y' \\ v_z \end{bmatrix}$$

DRAFT – Page 94 – May 20, 2009

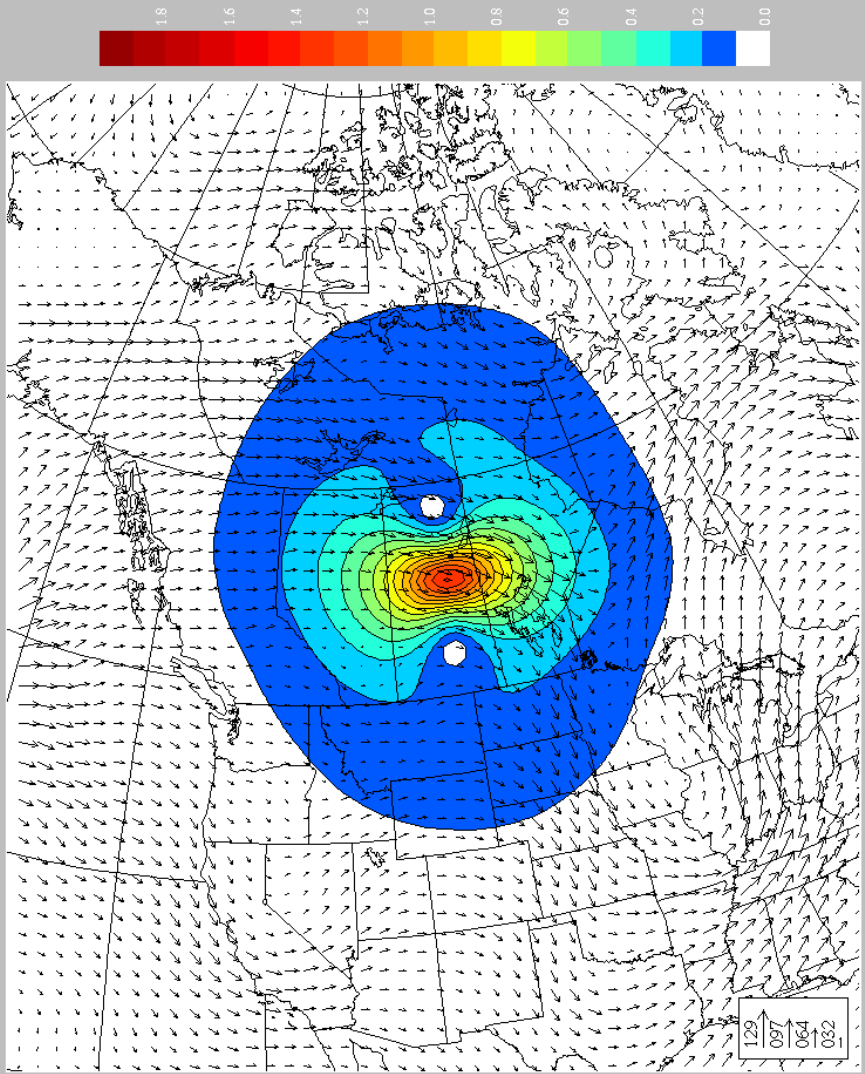


- **Step 3**

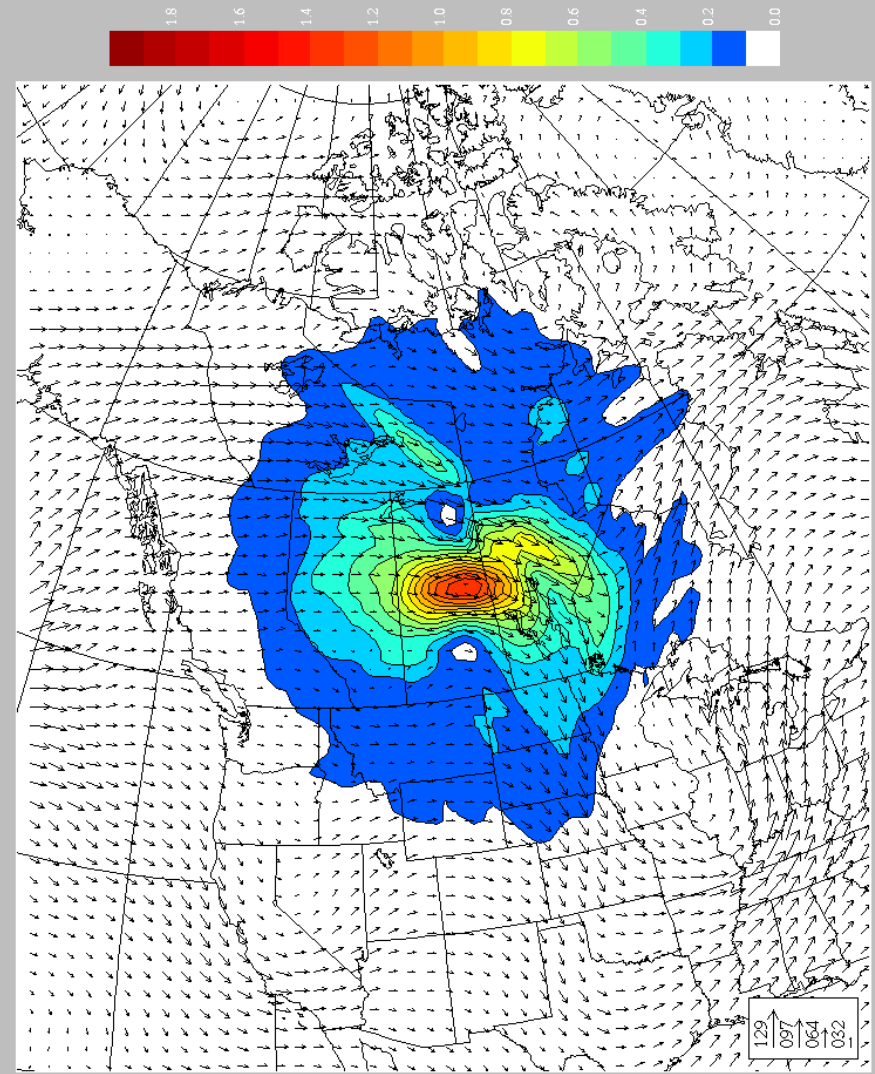
$$\mu = -\sin\lambda v_x + \cos\lambda v_y$$

$$v = -\frac{1}{\sin\theta} (\cos\lambda v_x + \sin\lambda v_y) = v_1$$

$$v = \frac{v_z}{\cos\theta} \equiv v_2$$



3D-Var LAM 55km

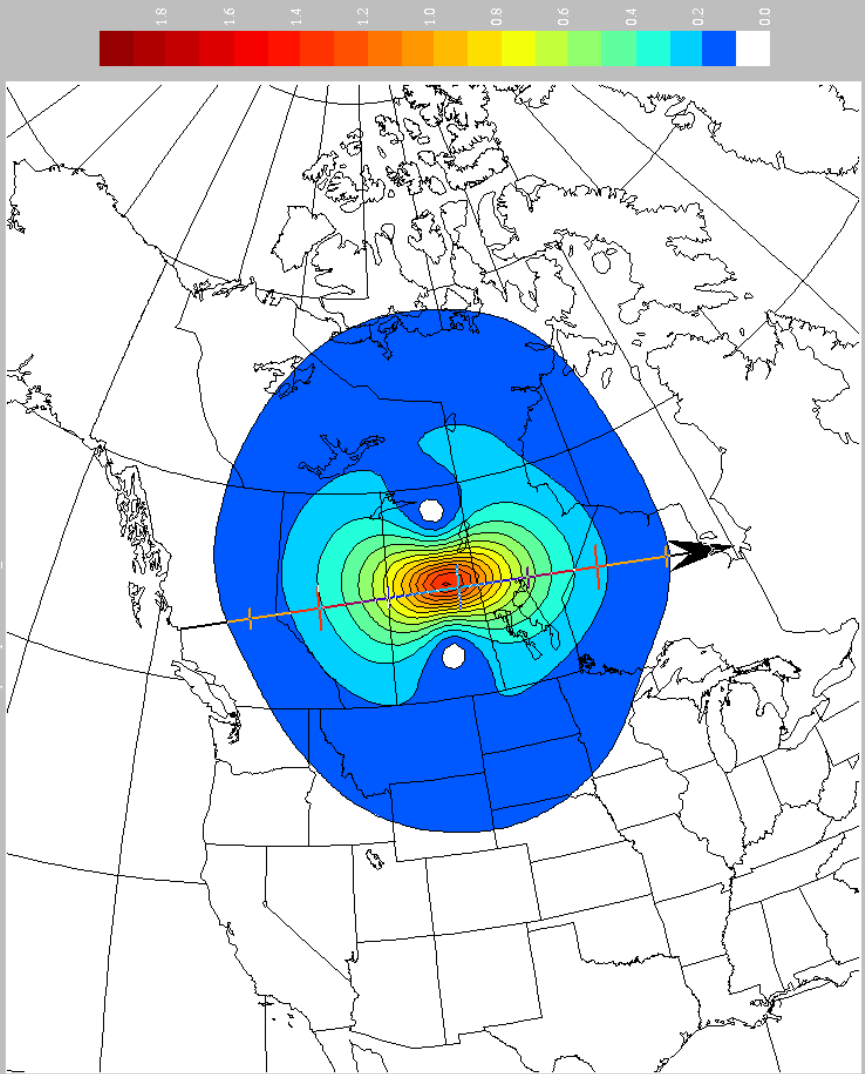


4D-Var LAM 55km

T = +0.00 hr

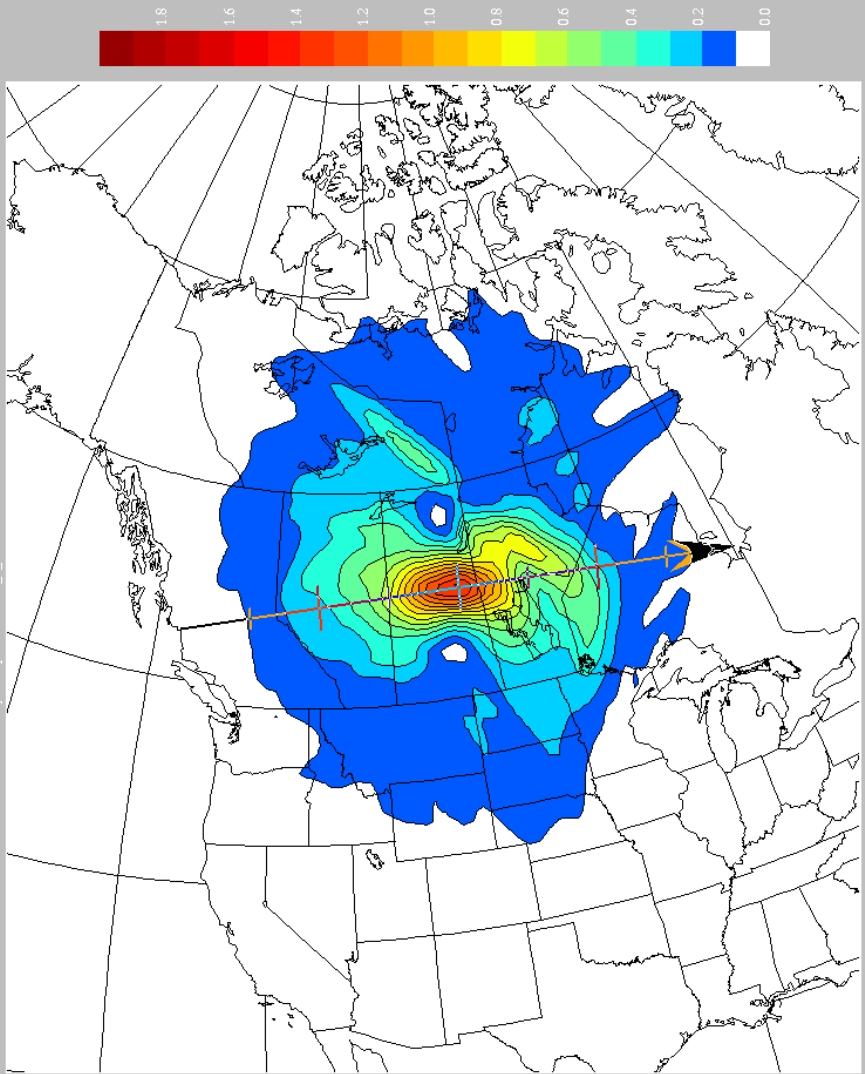


UV (Module du vent)
Niveau: 0.495000 hPa - Etiquette: 3DUU_500 - Intervalle: 0.1 * 1.0e+00 noeuds



Requis validee 00:00Z le 01 janvier 2007

UV (Module du vent)
Niveau: 0.495000 hPa - Etiquette: 4DUU_5_TL004 - Intervalle: 0.1 * 1.0e+00 noeuds



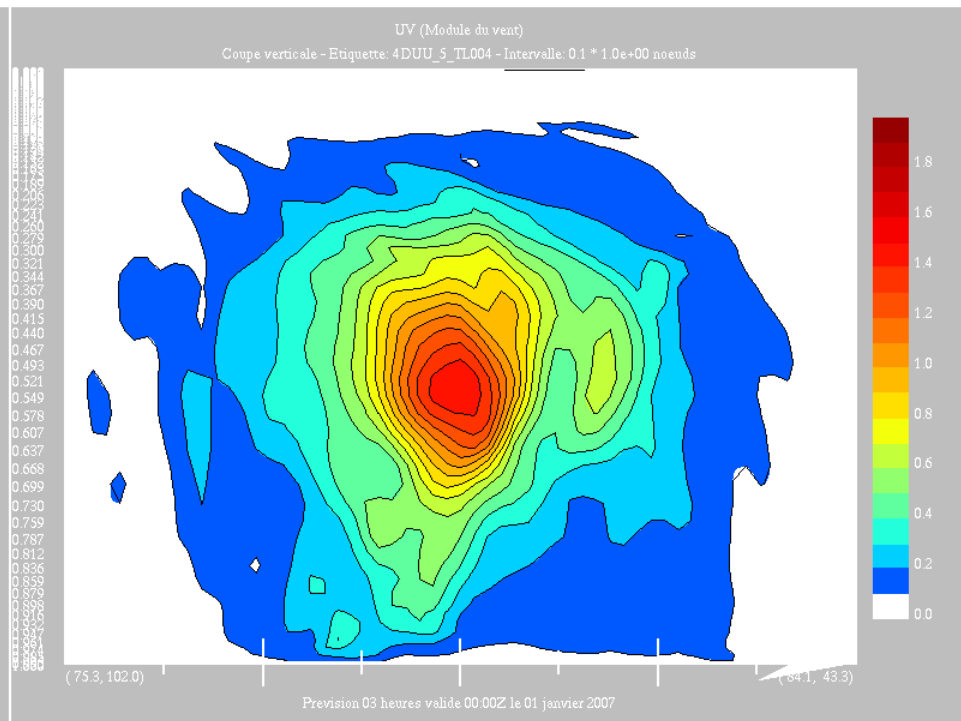
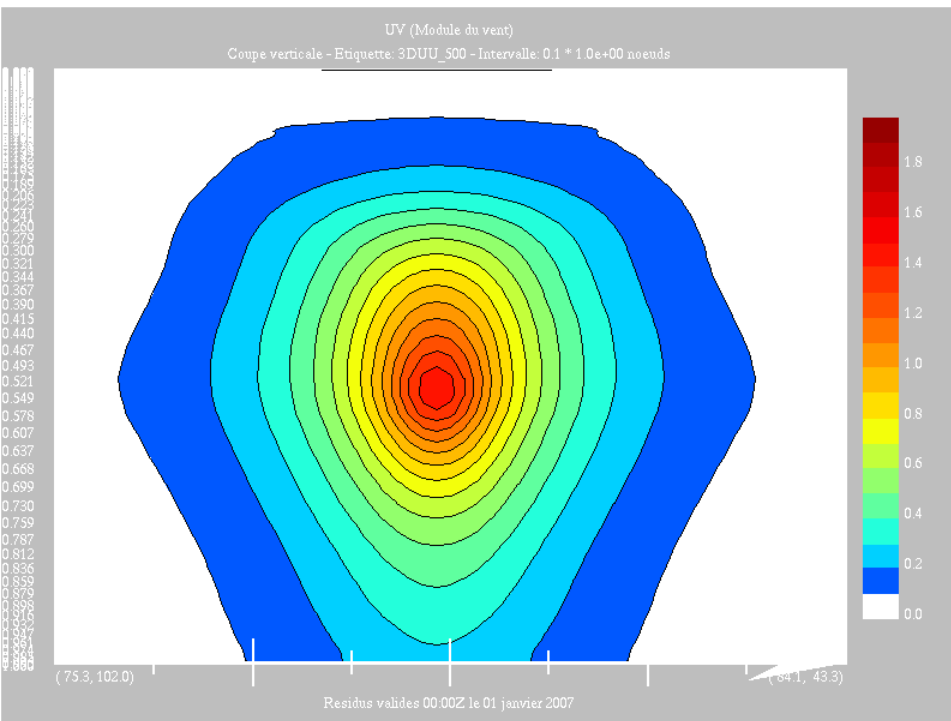
Prevision 03 heures validee 00:00Z le 01 janvier 2007

3D-Var LAM 55km

4D-Var LAM 55km

T = +0.00 hr





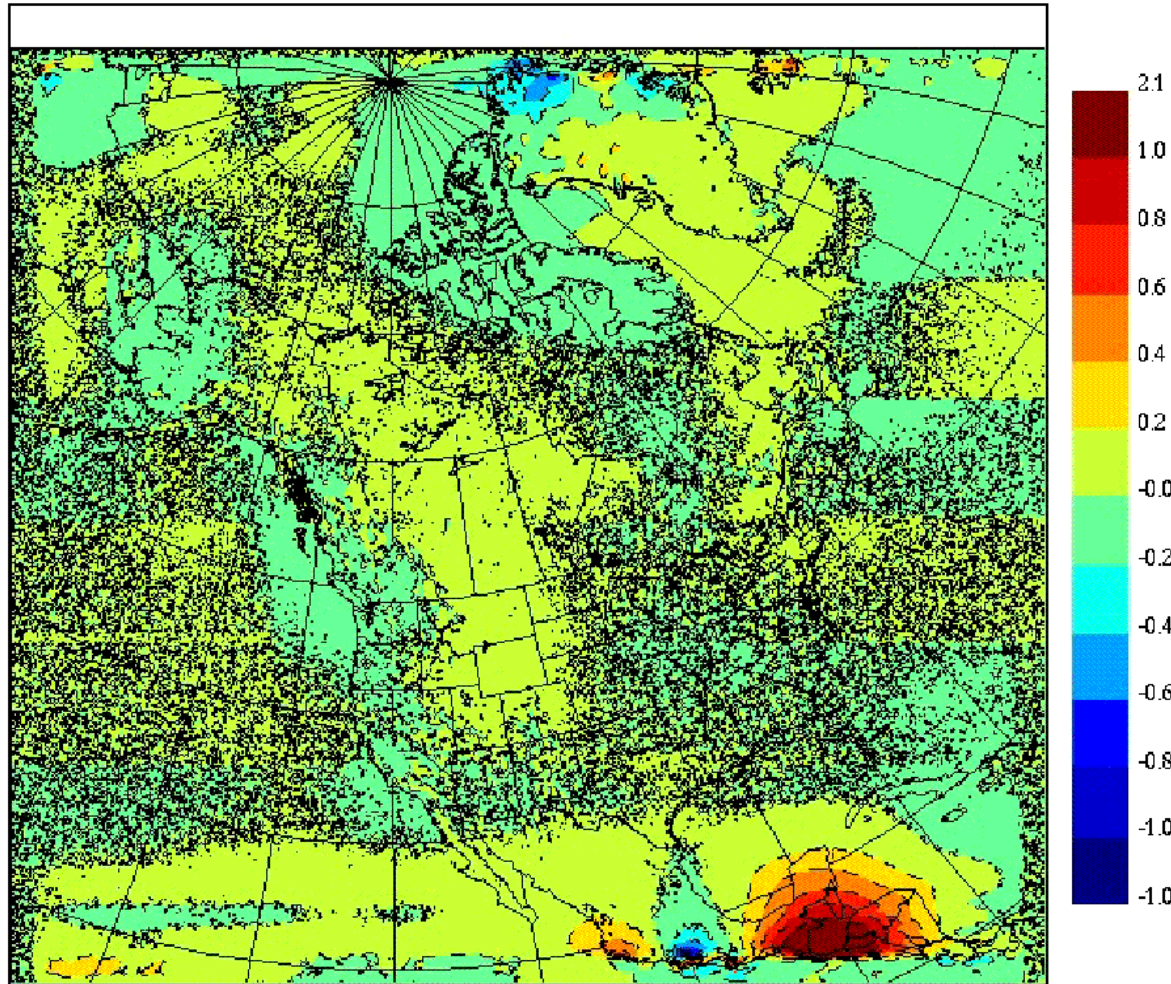
3D-Var LAM 55km

4D-Var LAM 55km

T = +0.00 hr

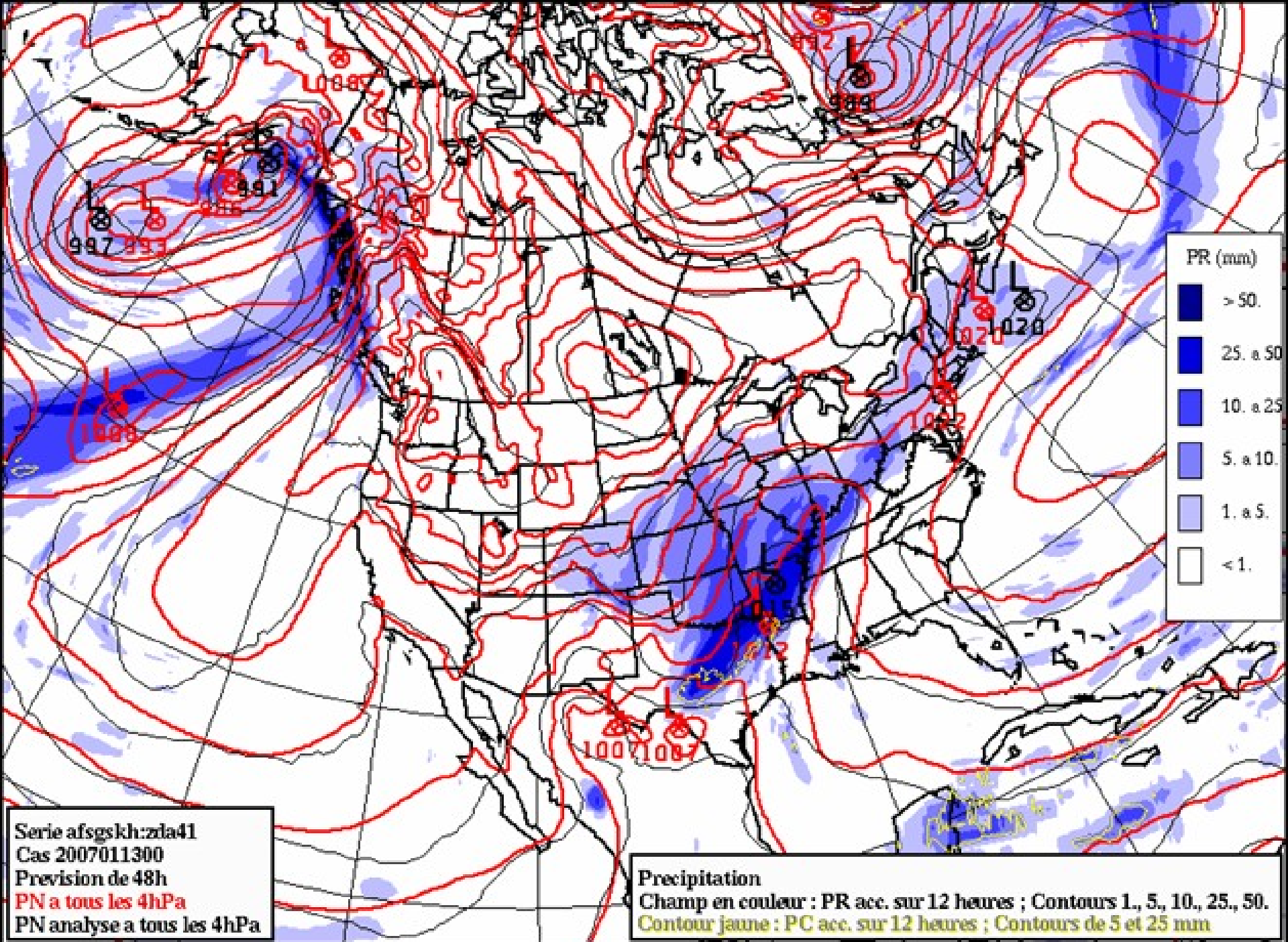


Animation (1 à 48 h) des différences GZ 500 (dam)
Moyenne des 13 cas d'hiver



GZ*P* 500 mb1080* 13* V20050202.010000*[L1EGAT80KM4L1SUD]



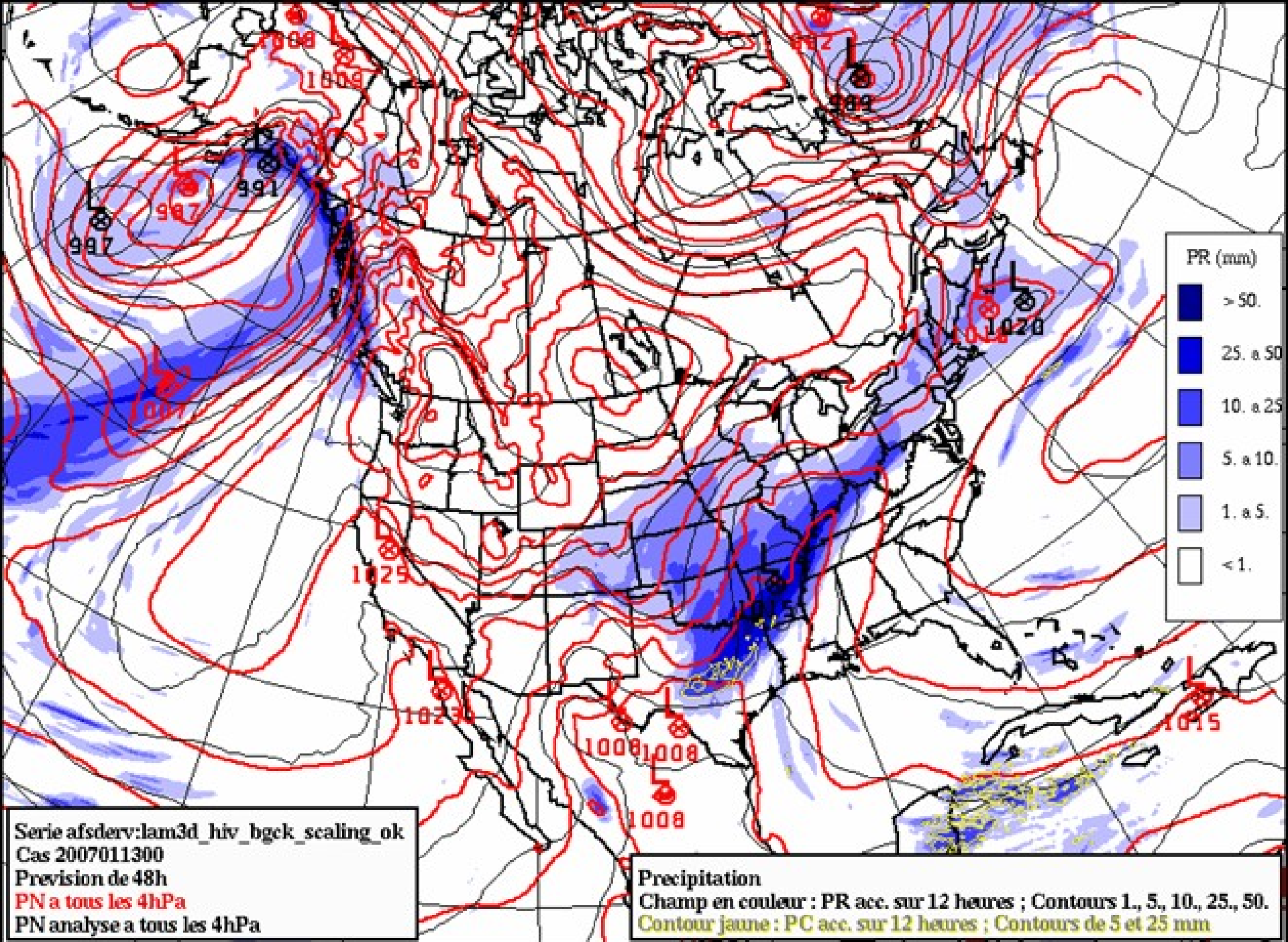


PR (mm)

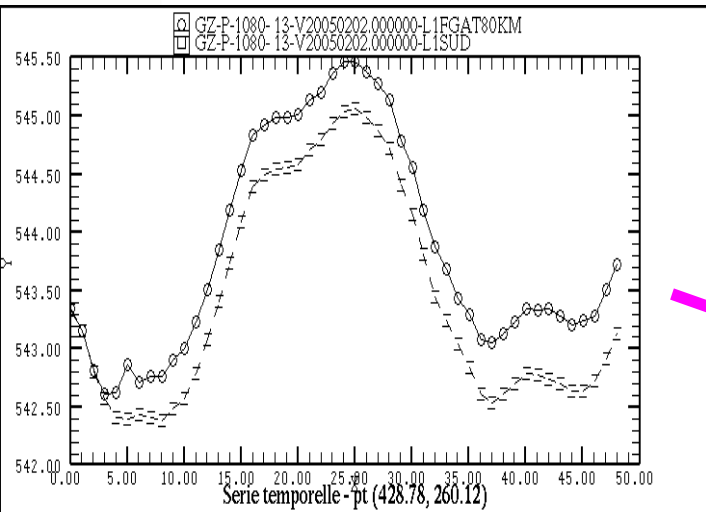
- > 50.
- 25. a 50
- 10. a 25
- 5. a 10.
- 1. a 5.
- < 1.

Serie afsgskh:zda41
 Cas 2007011300
 Prevision de 48h
 PN a tous les 4hPa
 PN analyse a tous les 4hPa

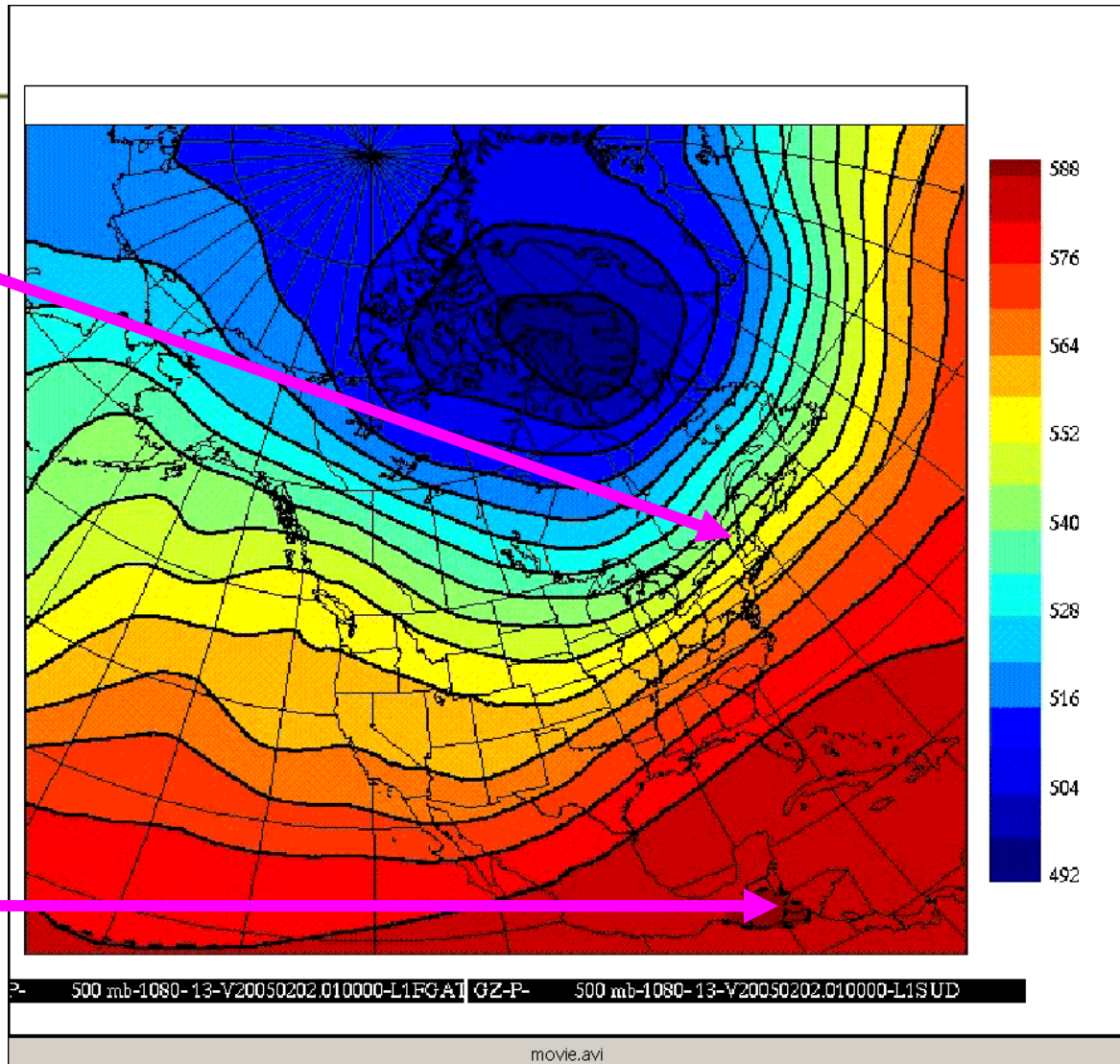
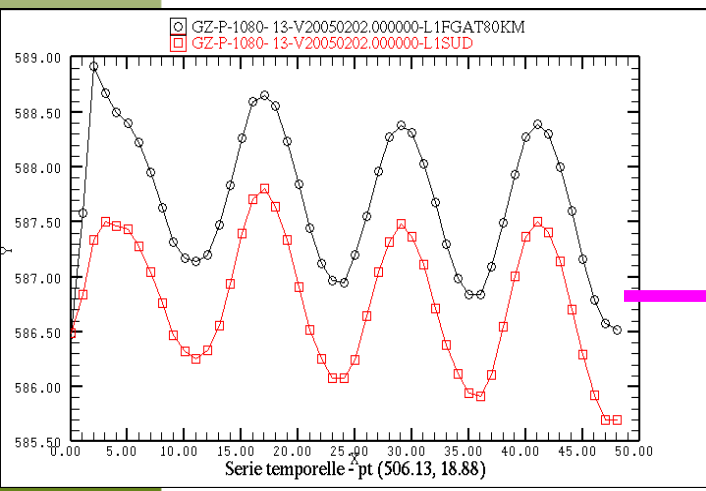
Precipitation
 Champ en couleur : PR acc. sur 12 heures ; Contours 1, 5, 10, 25, 50.
 Contour jaune : PC acc. sur 12 heures ; Contours de 5 et 25 mm



Animation (1 à 48 h) GZ 500 (dam) Moyenne des 13 cas d'hiver



Séries temporelle GZ 500 mb



Replacing GEM-REG with GEM-LAM

- Current GEM-REG is a global model, with a higher resolution central window and variable resolution moving away from this window.
- For assimilation, current approach is tied to Global assimilation and datasets (much coarser resolution).
- Proposed replacement is GEM-LAM on the continental scale at 15-km, including independent 3D-Var at 55-km.
- Initial implementation limits changes to model and assimilation (e.g. same physics, datasets, etc).
- Initial forecast quality to be very similar to that of GEM-REG due to conservative approach taken.
- Much further improvements to be included after 2010 Olympics.



$J_b = \frac{1}{2} \chi^T \chi$ (3.4.2) , we make a change of analysis variables of the form:

$x - x_b = L\chi$ (3.4.3) s.t. $B = \dot{\iota}^T$ (3.4.4)

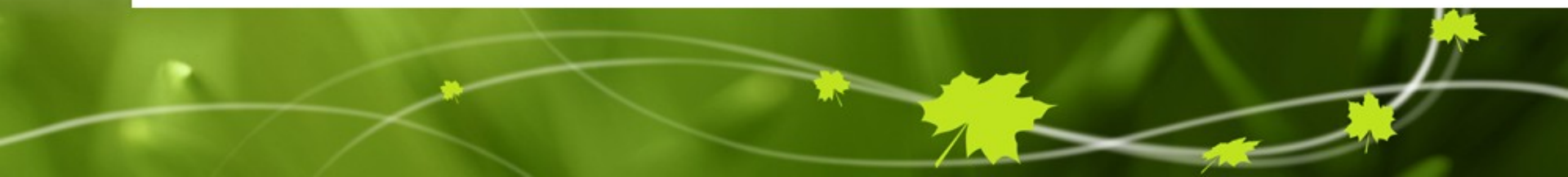
$\Delta\xi \equiv C_V^{-1/2} \Delta\tilde{x}$; $\Delta\tilde{x} = (\Delta\tilde{\psi}, \Delta\tilde{\chi}_u, \Delta\tilde{T}_u, \Delta\tilde{q}, \Delta\tilde{p}_{s_u})^T$ $\Delta\tilde{\psi} = F (\Delta\psi/\sigma_\psi)$

$r_{k_t}(m,n) = EA E^{-1}$ CORNS = $EA^{1/2} E^T$

Min $J = J_b + J_o$
 $= \frac{1}{2} \Delta\xi^T \Delta\xi + \frac{1}{2} (H(x) - y)^T R^{-1} (H(x) - y)^T$

$x_b + \mathbf{RWG} D F^{-1} C_V^{1/2} \Delta\xi$ $D = \text{diag}(\sigma_\psi, \sigma_{\chi_u}, \sigma_{T_u}, \sigma_q, \sigma_{p_{s_u}})$

$\tilde{N}J = \tilde{N}J_b + \tilde{N}J_o = Dx + H^T R^{-1} (H(x) - y)$



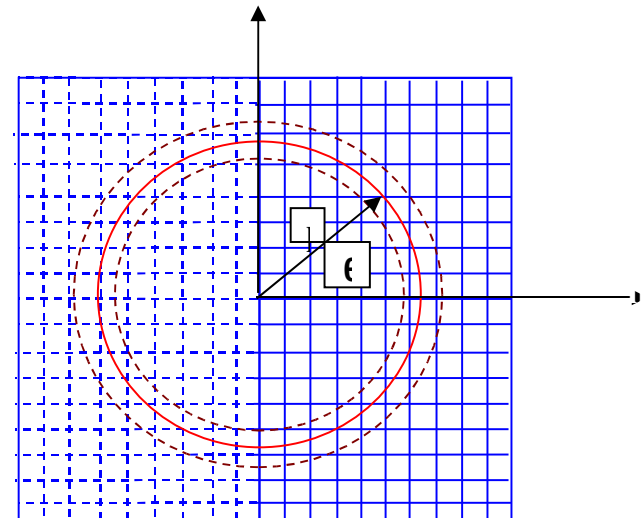


$$\rho(s) = \int_{-M}^M \int_{-N}^N \tilde{f}_{mn} \tilde{f}_{mn}^* \exp \left[2\pi i \left(\frac{ms_x}{L_x} + \frac{ms_y}{L_y} \right) \right] dm dn$$

$$dm dn = \int_{-M}^M \int_{-N}^N |\tilde{f}_{mn}|^2 dm dn = \int_{-M}^M \int_{-N}^N \gamma_{mn} dm dn = 1$$

$$\rho(s) = \frac{2\pi L_x L_y}{D^2} \int_0^{K^*} 2k^* J_0 \left(2\pi i \frac{k^* s}{D} \right) dk^*$$

$$L^2 = -2 \frac{\rho(r)}{\nabla^2 \rho(r)} = \left(\frac{D}{2\pi} \right)^2 \frac{\sum_{k_t=0}^{K_t} |\tilde{\rho}_{k_t}^{mn}|^2 k_t}{\sum_{k_t=0}^{K_t} |\tilde{\rho}_{k_t}^{mn}|^2 k_t^3}$$





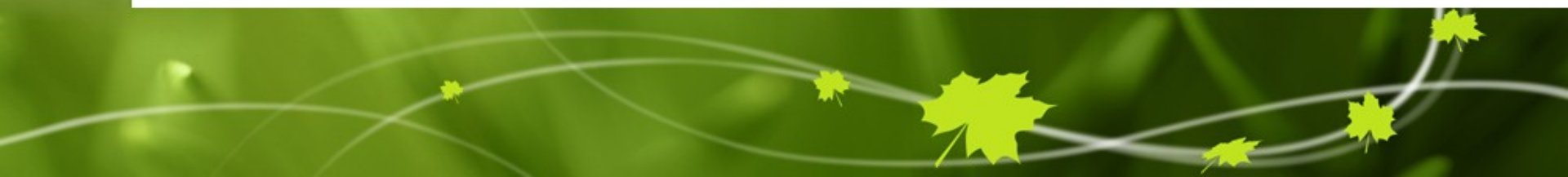
$$B_{klm}^{kln} = \frac{1}{2\pi} \int_0^{2\pi} \tilde{a}_{pqm} \tilde{a}_{pqn}^* d\theta$$

$$B_{klm}^{kln} = \frac{1}{2\pi} \int_0^{2\pi} \tilde{a}_{pqm} \tilde{a}_{pqn}^* d\theta \rightarrow B_{k_t}^{mn} = \frac{1}{m_{ban} \{d'(k_t)\}} \sum_{j_{tot}=1}^{m_{band}(k_t)} \tilde{a}_{k_t,m} \tilde{a}_{k_t,n}^*$$

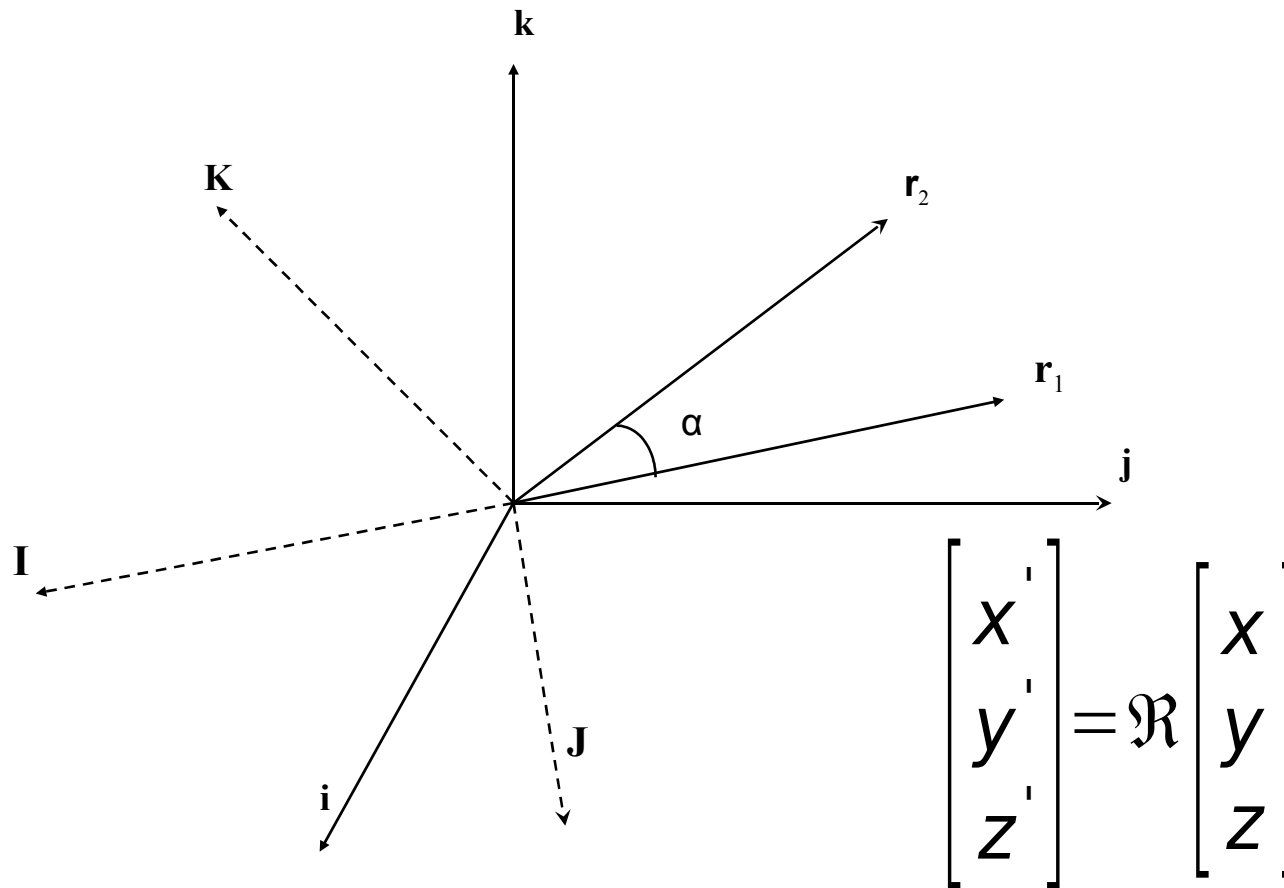
$$m_{ban} \{d'(k_t)\} = 2 m_{band}(k_t) - \alpha$$

$$\sigma_m^2 = \frac{2\pi MN}{N_s^2} \sum_{j=0}^{K_t} B_{k_t}^{mm} k_t^j; \gamma_m(k_t) \equiv \frac{B_{k_t}^{mm}}{\sigma_m^2}$$

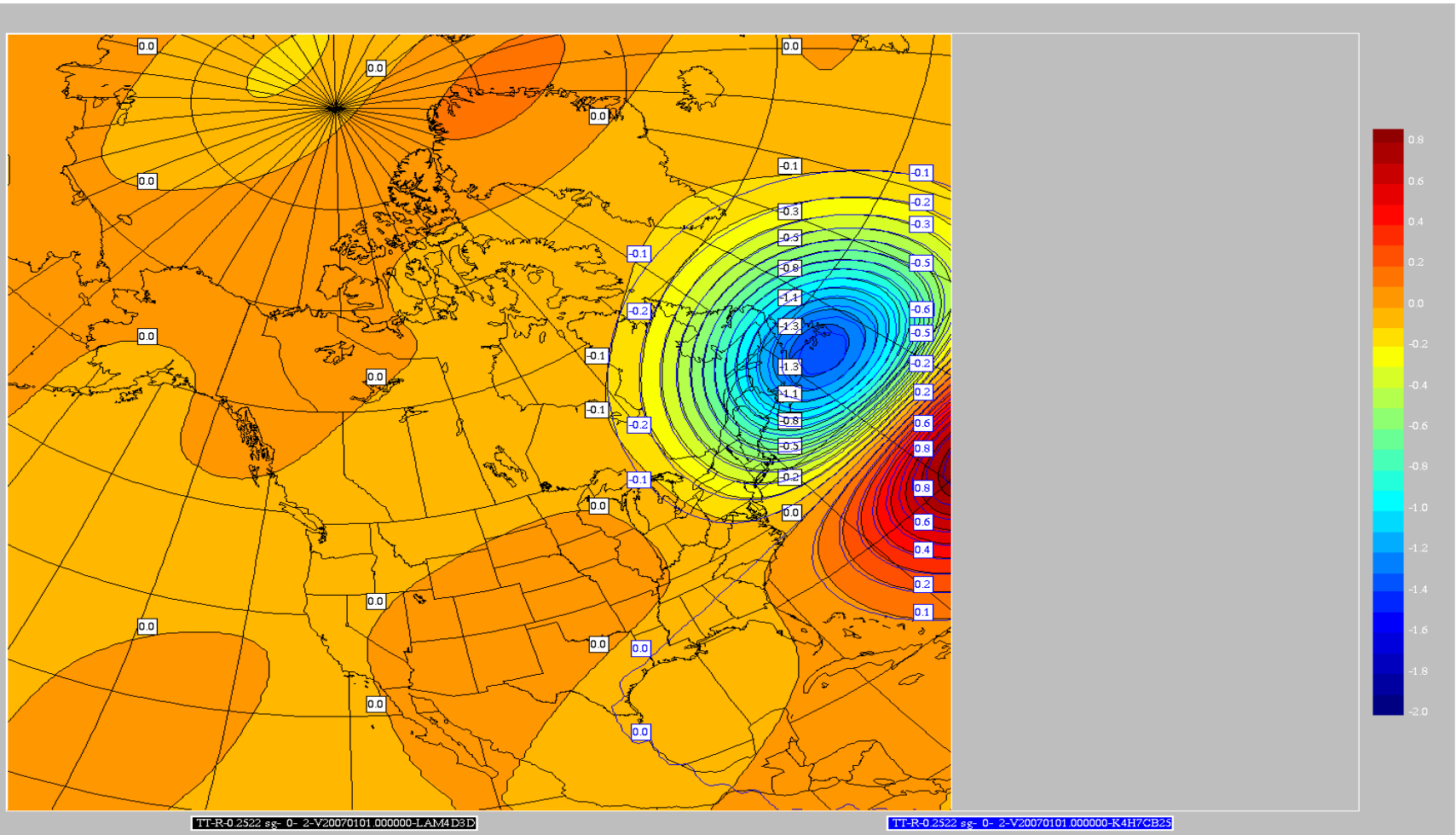
$$r_{k_t}(m, n) = \frac{B_{k_t}^{mn}}{\sigma_m \sigma_n \sqrt{\gamma_m(k_t)} \sqrt{\gamma_n(k_t)}} = \text{CORNS}$$



Rotation Matrix



1-Obs UU-500 hPa: T-increment



LAM-4D

3D-Var 10.2.2 / LAM GEM332

Boucle externe 15 km:

- NL : Analyse = LAM 15km / Pilote = Cubes creux GLB 55km

Boucle interne 55 km:

- LOOP1 = 25 it. LOOP2 = 25 it.

- NL : Analyse = LAM 15km / Pilote = Cubes pleins GLB 55km

- TL : Pilote = Persistence

