Recent Developments to the Milbrandt-Yau Cloud Microphysics Scheme

The Proposed Double-Moment Version for the VO2010 High-Resolution NWP System

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OUTLINE OF PRESENTATION

- 1. Background of the M-Y scheme
- 2. Recent developments
 - changes to snow category
 - new prognostic/diagnostic fields

3. Evaluation of VO2010 tests

4. Current and upcoming research





The Milbrandt-Yau multi-moment scheme:

Six hydrometeor categories

- LIQUID { *cloud* (small droplets) *rain* (drizzle-sized and larger drops) ICE-
PHASE• ice
ice(pristine crystal)
(large crystals and aggregates)
(rimed crystals)
(frozen drops and high-density ice)

Versions:

• Single-Moment

mass:

mass:

mass:

concentration:

concentration:

- QC, QR, QI, QN, QG, QH
- Double-Moment

QC, QR, QI, QN, QG, QH NC, NR, NI, NN, NG, NH

Triple-Moment

QC, QR, QI, QN, QG, QH NC, NR, NI, NN, NG, NH ZR, ZI, ZN, ZG, ZH

prognostic variables (advected)

reflectivity:

History of M-Y scheme

2004:	full multi-moment scheme (v1) developed at McGill University
2007 (Jan.):	single-moment and double-moment versions (v2) implemented into RPN-CMC physics library (v4.4)
2007 (June-Dec.):	single-moment (v2, v3) used for MAP D-PHASE
2007-08 (winter):	single-moment (v3) used in VO2010 practicum 1
2008 (April):	single-moment (v4) implemented into GEM-LAM-2.5
2008 (summer):	double-moment (v4) used in real-time 1-km GEM-LAM in support of UNSTABLE project
2008 (Dec.):	single-moment (v4) and <u>new double-moment (v5)</u> tested in recent high-resolution LAM system for VO2010
2008 (Jan. 8):	To be proposed (CPOP): implementation of double-moment (v5) into VO2010 system for 2009 practicum 2

2. Recent Developments



Developments to Double-Moment Version (v5):

- further optimization of sedimentation
- fine-tuning of *hail* initiation conditions
 - freezing of rain
 - conversion of graupel to hail
- other minor modifications
- modernization of snow category

The SNOW Category (in most bulk schemes, including original M-Y)

- Represents large ice crystals and/or aggregates
- Represented by equivalent spheres
 - Prescribed bulk density ($\rho_s = 100 \text{ kg m}^{-3}$)
 - $m(D) = (\pi/6)\rho_{\rm s}D^3$
 - $V(D) = aD^b$
- Growth rates
 - Diffusion: electrostatic capacitance analogy
 - Accretion: continuous or stochastic collection equation
- Precipitation
 - Mass flux computed from bulk sedimentation velocities

 $\frac{dq_s}{dt} = \frac{1}{\rho} \int_{0}^{\infty} \frac{dm(D)}{dt} N(D) dD$

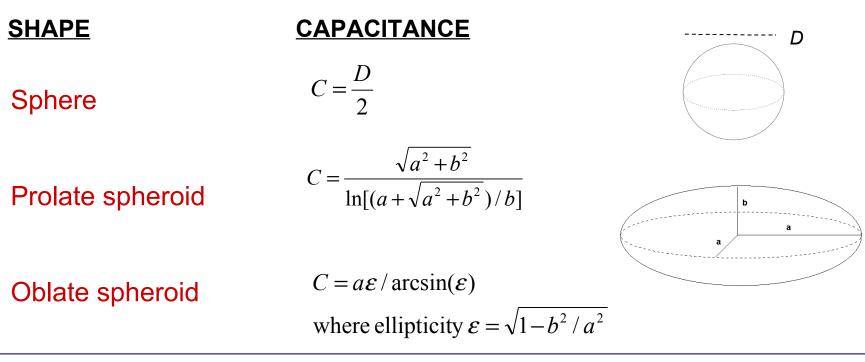
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Electrostatic Analogy for Diffusional Growth of Ice Crystals

$$\frac{dm(D)}{dt} = \frac{4\pi C(S_i - 1)}{AB_i} \quad \text{where} \quad AB_i = \frac{L_s^2}{K_a R_v T^2} + \frac{1}{\rho q_{is} \psi}$$



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Slide 9

Electrostatic Analogy for Diffusional Growth of Ice Crystals

"The electrostatic analogy of the capacitance theory of ice crystal growth is <u>highly flawed</u> and does not produce the observed growth rates of ice crystals.

It severely <u>overpredicts</u> the growth rates in almost all cases [by a factor of 3 to 8+ for plates and 2 to 4 for columns] involving even simple hexagonal shapes."

Bailey and Hallet (2006)



Capacitances of Hexagonal Plates

Theoretical

Measured

Oblate Spheroid Plate Capacitances Measured Capacitances -40 °C 300 mb -20 °C 550 mb -30 °C 400 mb t/D C/D C/D t/D C/D C/D t/D t/D Diameter thickness Capacitance 0.11-23 0.82 0.07-.29 0.730 0.365 0.84 0.27 0.83 0.225 0.112 2.0 0.15 0.36-.62 0.72 0.11-18 0.089 0.698 0.349 0.63 0.73 2.0 0.177 0.16-.28 0.59 0.10-.36 0.664 0.332 0.20 0.10 0.61 20 0.126 0.063 0.09-.26 0.324 0.13 0.02 0.40 0.07-.17 0.45 0.103 0.052 0.648 2.0 0.09-.29 0.08 0.32 0.08-:15 0.043 0.637 0.319 0.12 0.32 20 0.086 0.07 0.20 0.02-.13 0.20 0.02-.13 0.628 0.314 0.072 0.036 0.08 2.0 0.064 0.032 0.622 0.311 0.06 0.03-.13 0.10 0.01-.12 0.08 0.04-.08 2.0 0.02-.04 0.01-.11 0.058 0.029 0.618 0.310 0.04 0.06 0.02-.19 0.04 2.0 Sphere: THEORETICAL **MEASURED** C/D = 0.50.310 0.01 - 0.19Correction factor: 0.03 - 0.38Bailey and Hallet (2006)

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Changes to SNOW Category

2. Modification to diffusional growth

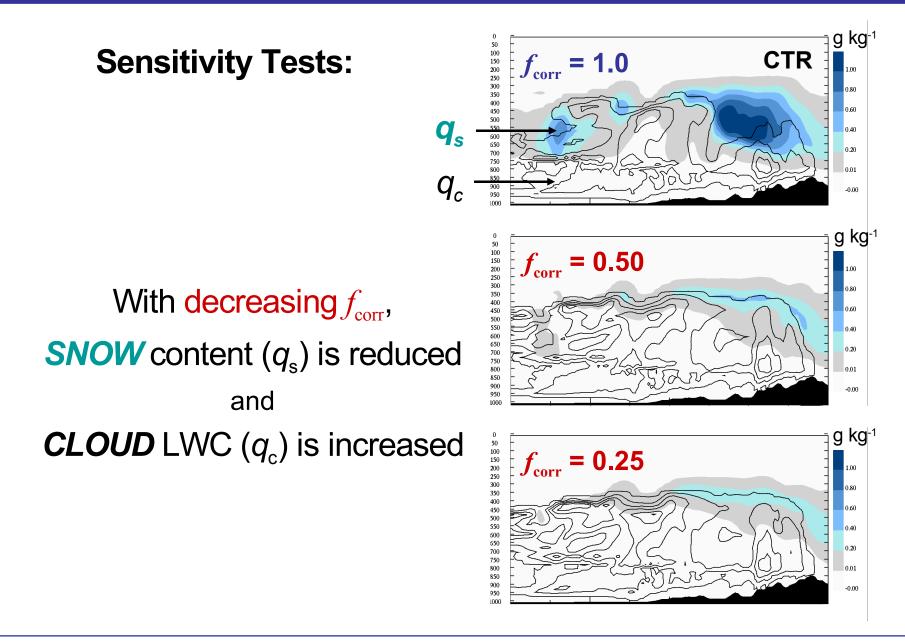
Add **CORRECTION FACTOR** to DIFFUSIONAL GROWTH EQUATION

$$\frac{dm}{dt} = \frac{4\pi C(S_i - 1)}{AB_i} \longrightarrow \frac{dm}{dt} = \frac{4\pi C \cdot f_{corr}}{AB_i} \cdot (S_i - 1)$$

where f_{corr} must be < 1, with value justified by results



2. Recent Developments – Changes to SNOW Category



Riming (growth by collection of cloud water)

Stochastic collection equation: (for category *x* collecting category *y*)

$$CL_{yx} = \frac{1}{\rho} \frac{\pi}{4} \int_{0}^{\infty} \int_{0}^{\infty} |V_x(D_x) - V_y(D_y)| (D_x + D_y)^2 m_y(D_y) E_{xy}(D_x, D_y) N_y(D_y) N_x(D_x) dD_y dD_x$$

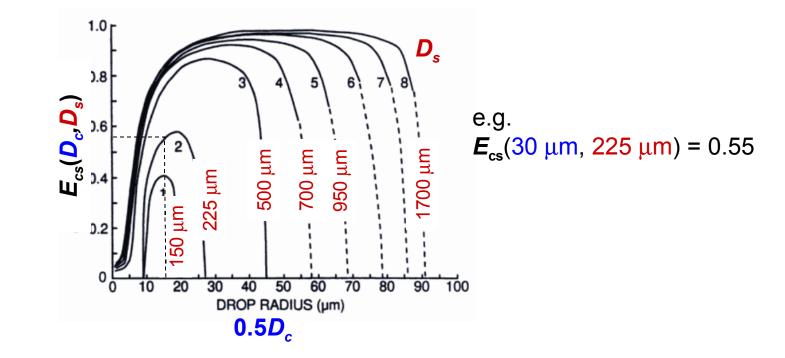
COLLECTION

EFFICIENCY

- Assumptions are made to solve analytically
- For the collection efficiency, $E_{cs} = 1$ is often assumed (for collection of *cloud* water by *snow*)
- If E_{cs} < 1, the snow riming rate will be <u>overestimated</u>

Riming (growth by collection of cloud water)

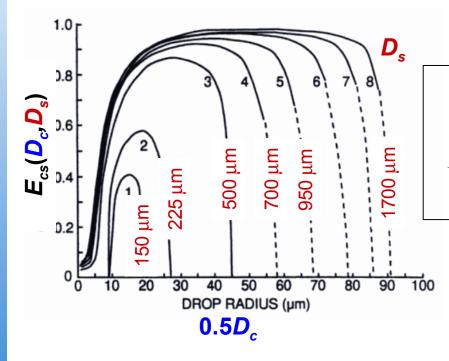
Computed from 3-D simulations* of Navier-Stokes equations:

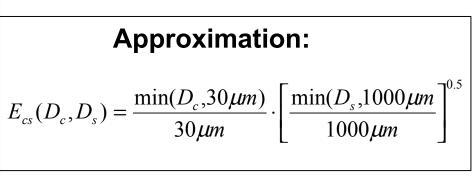


*Wang and Ji, 1992



Riming (growth by collection of cloud water)





- Works for D_c ~ 15-30 μm, and D_s ~ 150-1500 μm
- Reduces riming rate 10-80% (vs. *E*_{cs} = 1)

Note: For *graupel* and *hail*, $E_{cg} = 1$ is a reasonable approximation (Macklin and Bailey, 1966)

Mass-"Diameter" Relation for Snow Particles

Traditional approach:

 $m(D) = (\pi/6)\rho_{\rm s}D^3$

• Based on spheres with constant bulk density, $\rho_{\rm s}$

New approach:*

$$m(D) = cD^d$$
 ($c = 0.062, d = 2$)

- Based on obs of "assemblages of fractal-like aggregated crystals"
- Values of m-*D* parameter (*c*, *d*) directly affect values of size distribution parameters (λ_s , N_{os})
- Thus, all expressions that depend on λ_s, N_{os} are affected
 i.e. <u>all microphysical source/sink terms and sedimentation</u>
 Note: In the new m-D relation, D represents the maximum crystal dimension

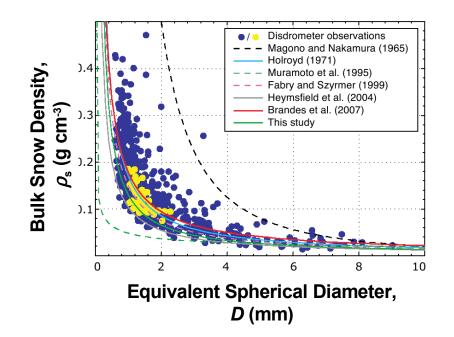
* following Thompson et al. (2008)

2. Recent Developments – Changes to SNOW Category

New approach:*

 $m(D) = cD^d$ (c = 0.062, d = 2)

 Based on obs of "assemblages of fractal-like aggregated crystals"



$$\mathbf{P}_{s} = f(D_{s}^{-1})$$

where
$$D_s = f(Q_s, N_s)$$

(double-moment)

Consistent with distrometer observations*

* Thompson et al. (2008)



Prognostic Density of Precipitating Snow*

(not just bulk density of SNOW category)

* Snow = *ICE* + *SNOW* + *GRAUPEL*

(i.e. ice crystals + snow crystals/aggregates + rimed crystals)

APPROACH:

• use the mass-weighted bulk densities (prescribed or diagnosed) of

ICE, SNOW, and GRAUPEL to obtain the "prognostic" snow density

$$\rho_{snow} = \frac{(q_i \rho_i) + (q_s \rho_s) + (q_g \rho_g)}{q_i + q_s + q_g} \qquad \rho_i = 500 \text{ kg m}^{-3}$$

$$\rho_s = f(D_s)$$

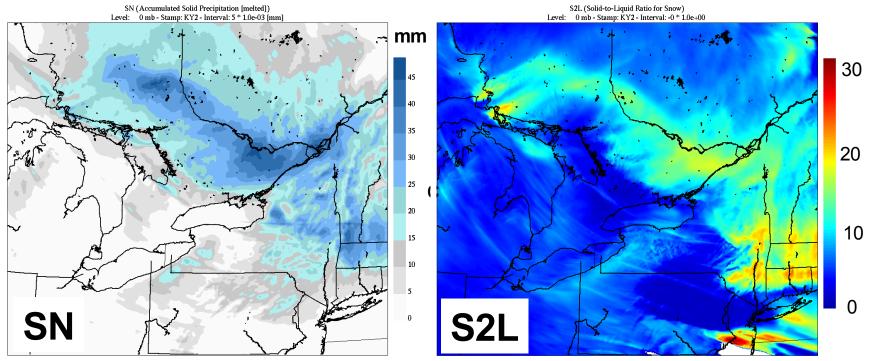
$$\rho_g = 400 \text{ kg m}^{-3}$$

applied to total mass flux (sedimentation rate) of ICE + SNOW +

GRAUPEL to obtain **instantaneous snow rate**, cm s⁻¹ (unmelted)

Accum. Pcp. (liquid-equivalent)

Solid:Liquid Ratio



36 hour fcst valid 00:00Z December 04 2007

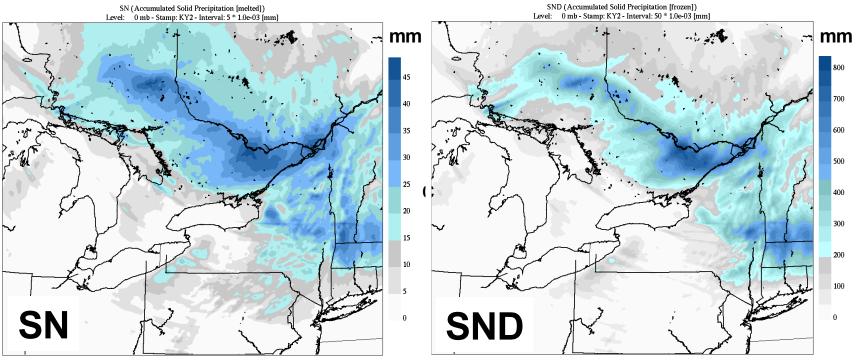
36 hour fcst valid 00:00Z December 04 2007

36-h QPF



Accum. Pcp. (liquid-equivalent)

Accum. Pcp. (unmelted)



36 hour fcst valid 00:00Z December 04 2007

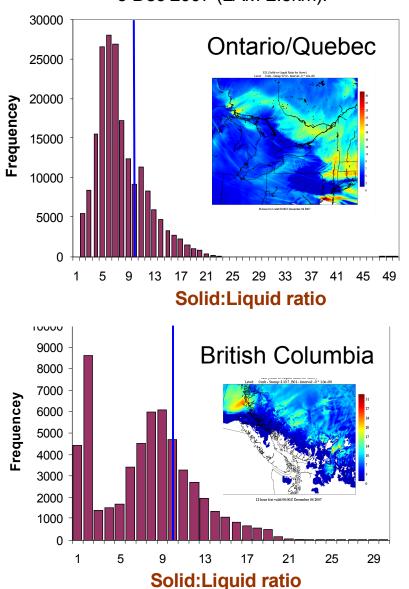
36 hour fcst valid 00:00Z December 04 2007

36-h QPF

NOTE: SND \neq SN \cdot S2L rather, RSND = RSN \cdot RS2L (<u>instantaneous</u>)

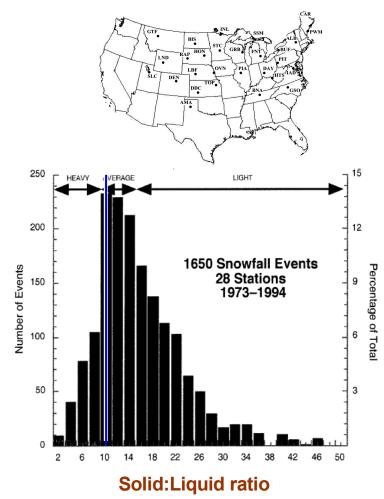


2. Recent Developments – New Diagnostics



3 Dec 2007 (LAM-2.5km):

Climatology (north-east USA):

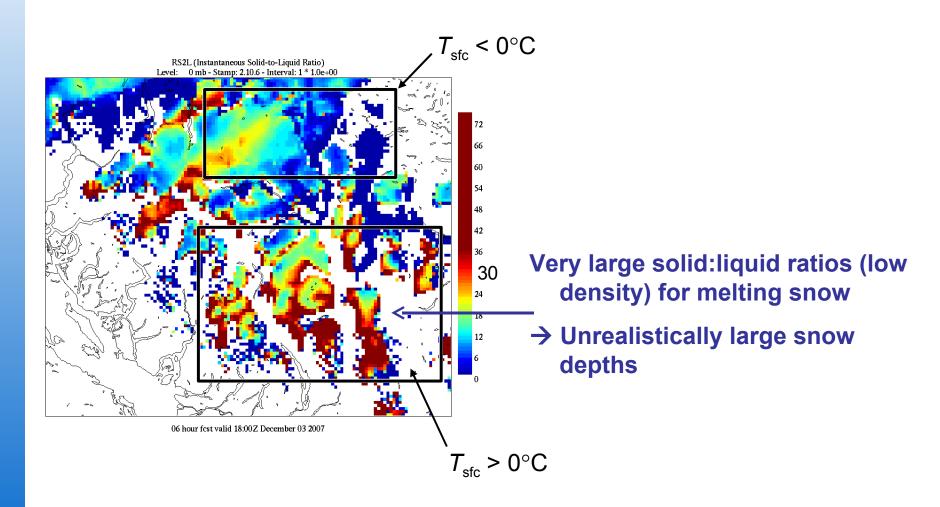


Roebber et al. (2003) Weather and Forecasting



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Solid-to-Liquid Ratio (instantaneous)



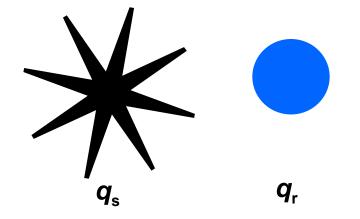
2. Recent Developments – New Diagnostics

Proposed Solution to Treat Melting Snow:

if
$$T > 0^{\circ}$$
C: $\rho_{s_melting} = \frac{q_s \rho_s(D_s) + q_r \rho_L}{q_s + q_r}$

Actual model representation:

 $\rho_{\rm s} = f(D_{\rm s})$ $\rho_{\rm L} = 1000 \text{ kg m}^{-3}$



(where \boldsymbol{q}_{r} originates directly from \boldsymbol{q}_{s} due to melting)

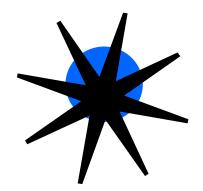
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Approximate view of melting snow:



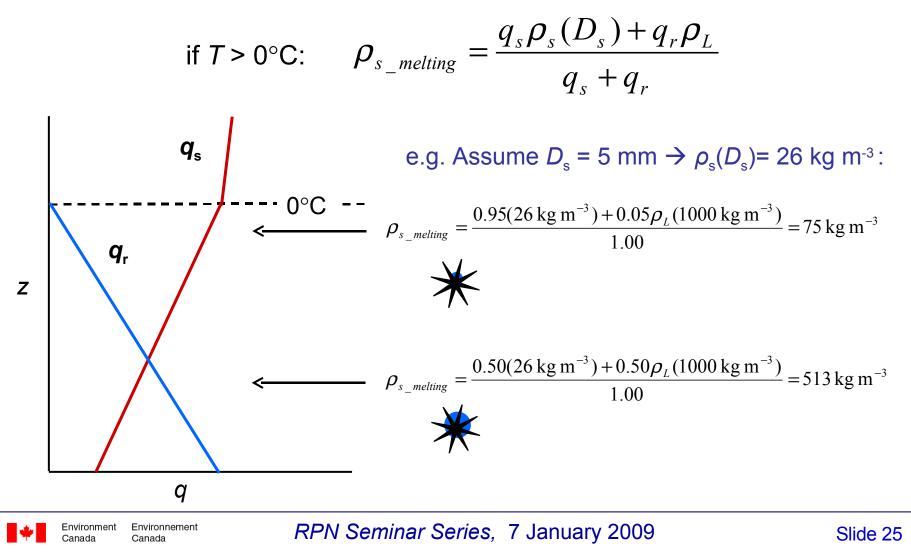


 $\frac{\boldsymbol{q}_{r}}{\boldsymbol{q}_{r}+\boldsymbol{q}_{s}}$ is the liquid fraction of melting snow

2. Recent Developments – New Diagnostics

Proposed Solution:

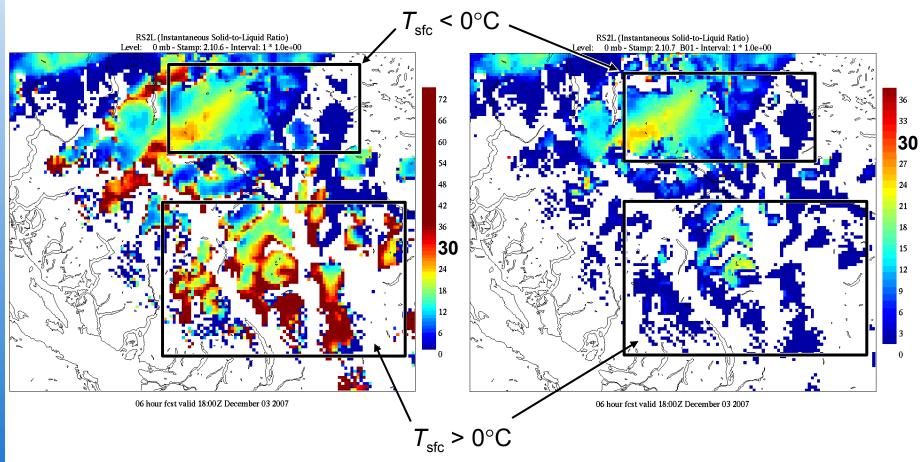
- approximate liquid fraction of melting snow by $q_r / (q_r + q_s)$
- use mass-weighted density to approximate density of melting snow



Solid-to-Liquid Ratio (instantaneous)

Before Correction

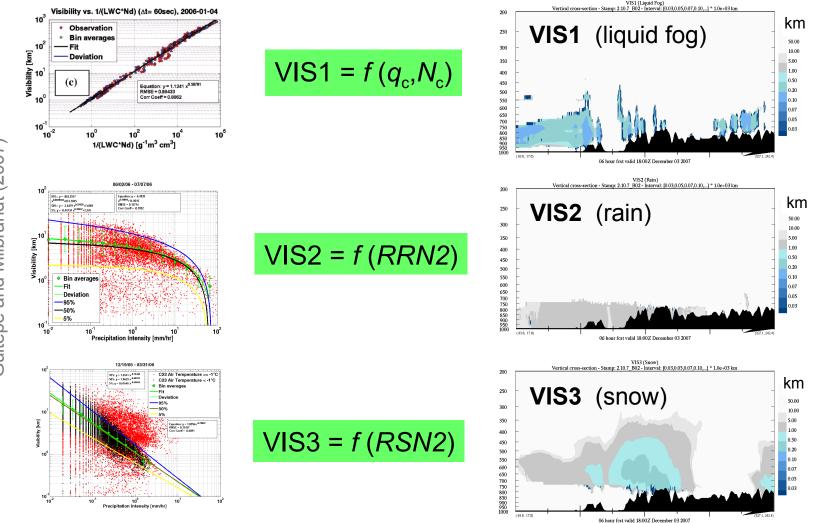
After Correction





3D fields for VISIBILITY due to fog, rain, and snow

(parameterizations* based on observations taken during FRAM)



*Gultepe and Milbrandt (2007)

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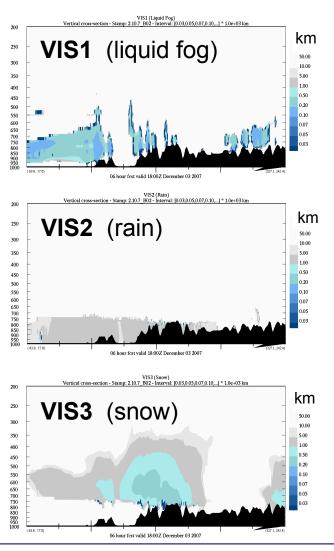
3D fields for **VISIBILITY** due to *fog*, *rain*, and *snow*

(parameterizations* based on observations taken during FRAM)

VISIBILITY due to the <u>combined effects</u> of liquid FOG, RAIN, and SNOW:

$$VIS = -\ln(\varepsilon)\beta_{ext}^{-1}$$

$$\longrightarrow$$
 VIS = $\left(\frac{1}{VIS1} + \frac{1}{VIS2} + \frac{1}{VIS3}\right)^{-1}$



3D fields for **VISIBILITY** due to *fog*, *rain*, and *snow* (parameterizations based on observations taken during **FRAM**)

200

250

300

350

400

450 500

550 600

650

200

250

300

350

400

450 500

550

200

250

300

350

400

450 500

550 600

650

VIS1

VIS1 (Liquid Fog) Stamp: 2.10.7 B02 - Interval: [0.03,0.05,0.07,0.10,...] * 1.0e+03 km

(liquid fog)

06 hour fcst valid 18:00Z December 03 2007

06 hour fest valid 18:00Z December 03 2007

06 hour fcst valid 18:00Z December 03 2007

VIS3 (Snow) Stamp: 2.10.7 B02 - Interval: [0.03.0.05.0.07.0.10....] * 1.0e+03 k

VIS2 (rain)

VIS3 (snow)

VIS2 (Rain) ection - Stamp: 2.10.7 B02 - Interval: [0.03,0.05,0.07,0.10,...] * 1.0e+03 km km

50.00

10.00

5.00

1.00

0.50

km

50.00

10.00

5.00

1.00

0.50

0.20

n 10

0.05

km

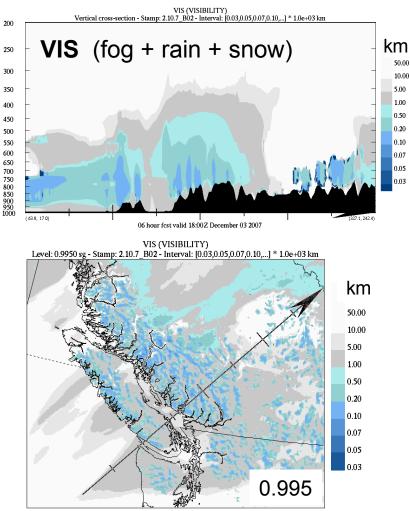
50.00

10.00 5.00

1.00

0.50

07



06 hour fcst valid 18:00Z December 03 2007

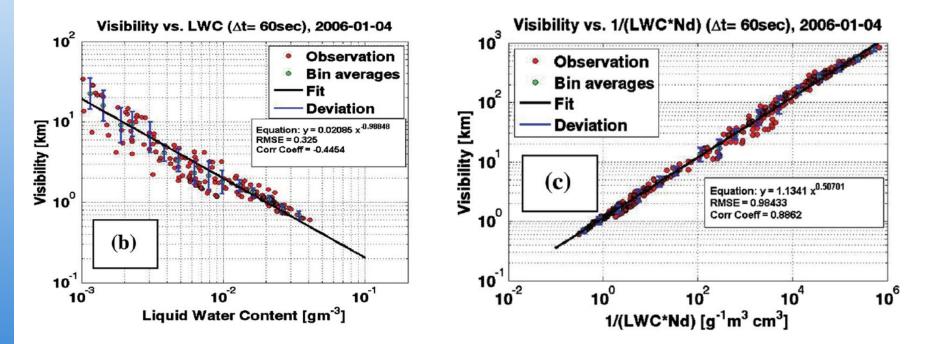


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VIS1 (liquid fog)

Single-Moment: VIS1 = f(QC)

Double-Moment: VIS1 = f(QC, NC)



- VIS1 is parameterized better for double-moment,
- BUT low-level LWC (QC) is the weakest link (not NC)

Gultepe and Milbrandt (2007)

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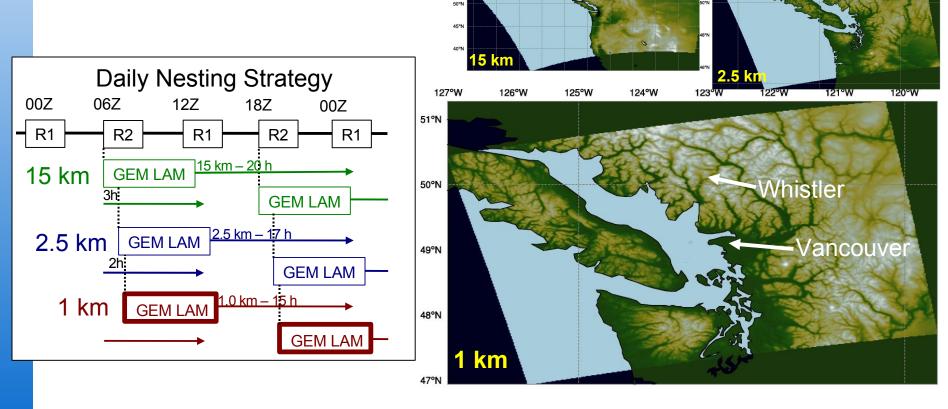
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3. Evaluation of VO2010 Tests



VO2010 High-Resolution Forecast System

- Triple-nested LAM integrations twice daily from 0600 and 1800 UTC GEM Regional forecasts:
 - LAM-15km \rightarrow 2.5km \rightarrow 1km



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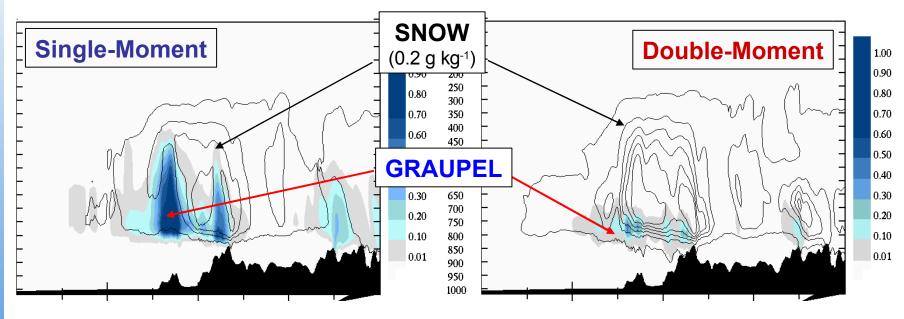
- 10 winter cases (2007-2008) selected
- New features: evaluation in 3 steps
 - 1. geophysical fields using GenPhysX and new database at 90-m res
 - 2. CCCmarad radiation scheme (single-moment M-Y, v4)
 - 3. Milbrandt-Yau double-moment bulk microphysics scheme (v5)

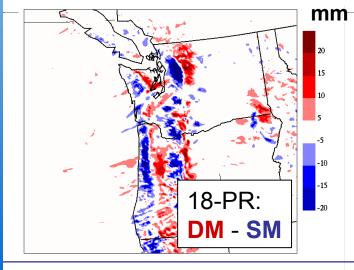
Following Comparison: Step 2 vs. Step 3 i.e. SINGLE-MOMENT vs. DOUBLE-MOMENT



3. Evaluation

New SNOW-GRAUPEL mass balance \rightarrow modifies precipitation



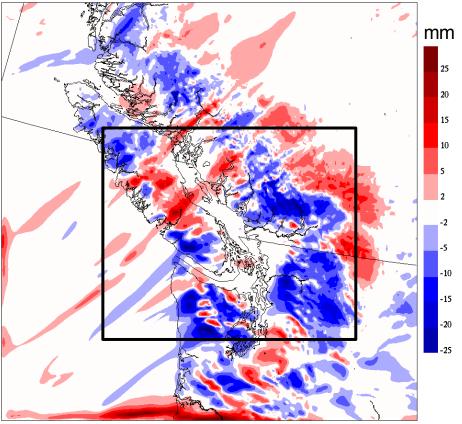


- ↑SNOW ↓GRAUPEL in **Double-Moment**
- downwind shift in surface pcp
- general reduction in pcp along coast and upwind side of mountains

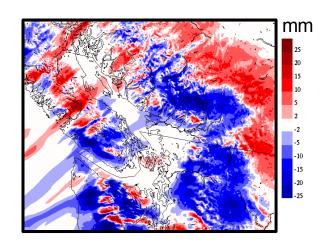
Environment Environnement Canada Canada 6-h PR 2007-12-03: 12-18 UTC

DOUBLE-MOMENT - SINGLE-MOMENT

2.5-km run:

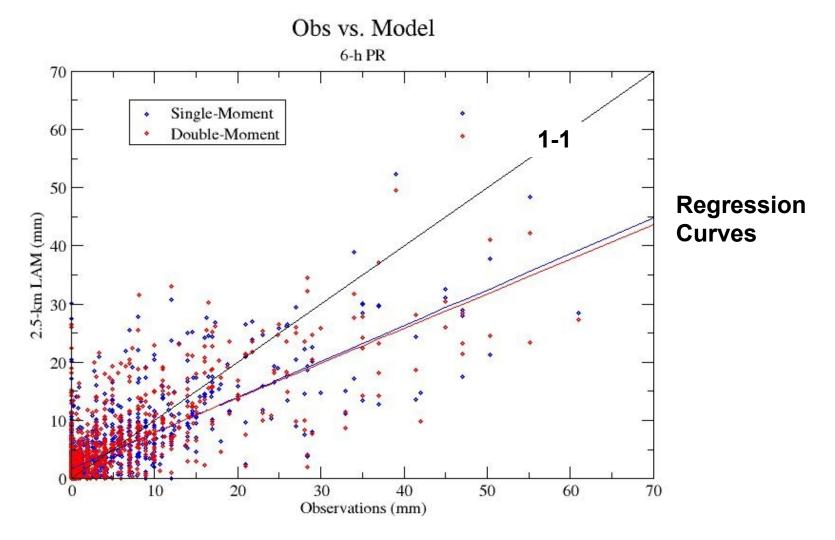


1-km run:

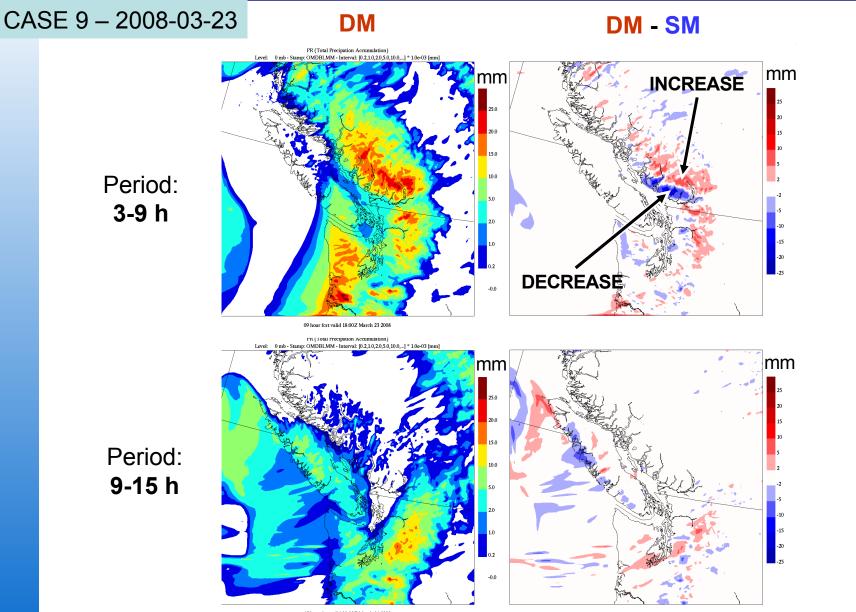


Similar response to schemes →Focus analysis on 2.5-km grid (larger grid, more rain gauges)

10 Winter Cases, 20 6-h periods, 50-70 obs. points per period: 1335 gauge vs. model (2.5-km) points



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15 hour fest valid 00:00Z March 24 2008



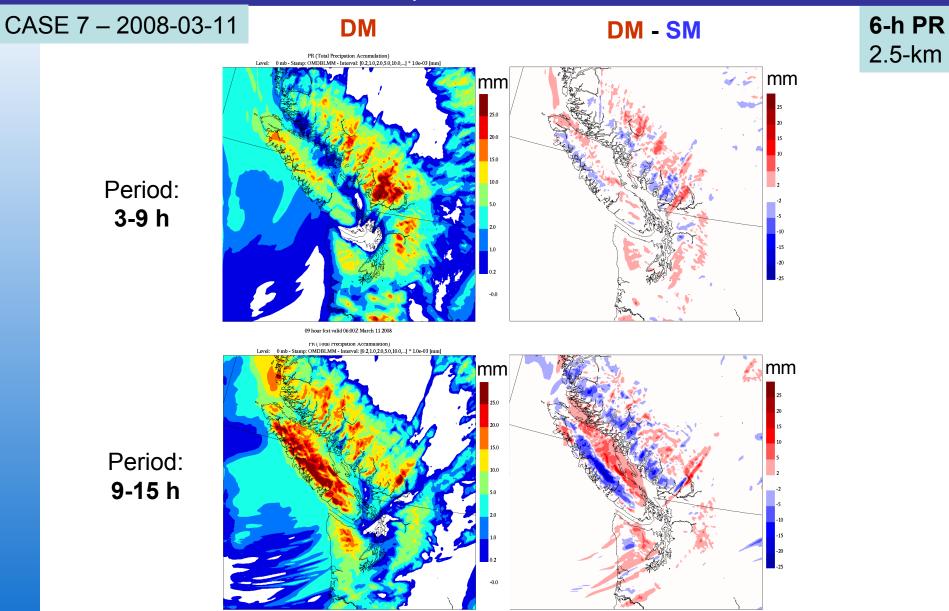
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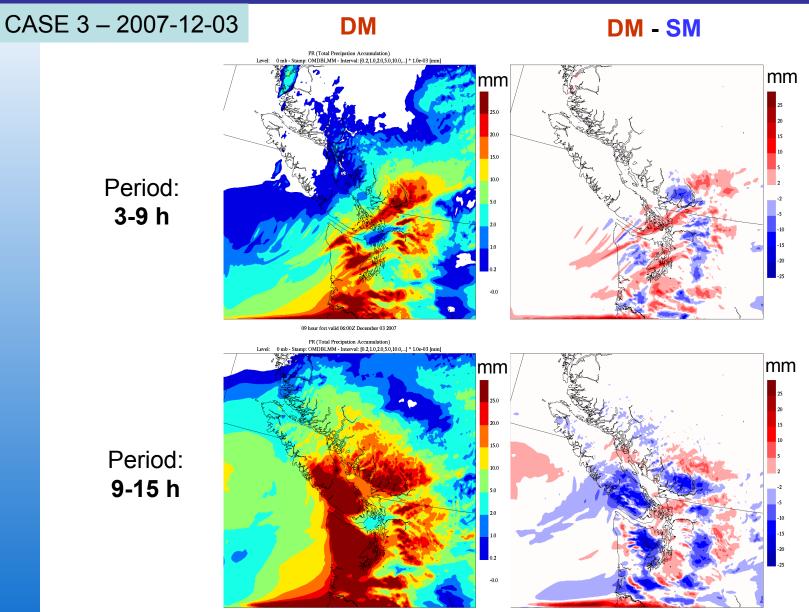
6-h PR

2.5-km



15 hour fcst valid 12:00Z March 11 2008





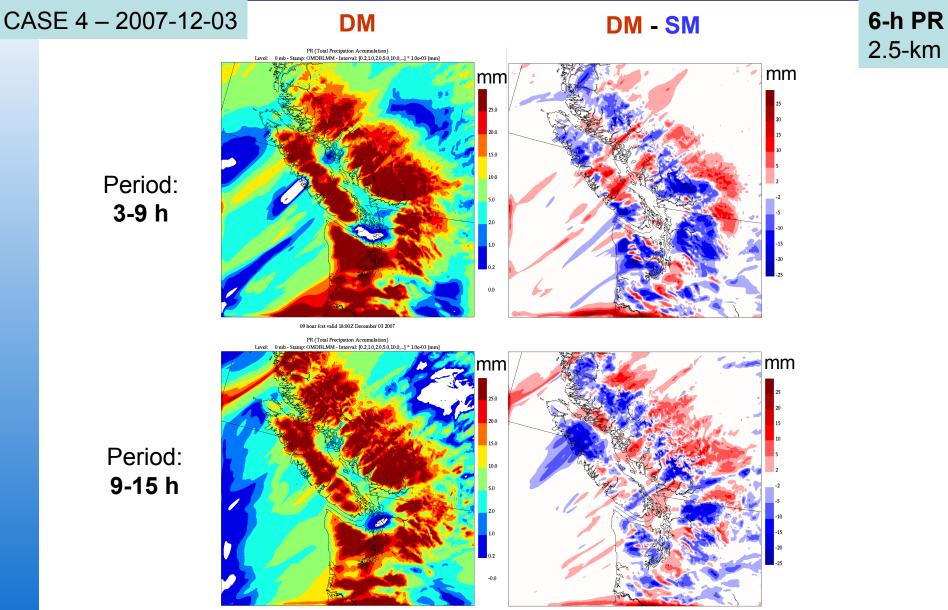
15 hour fcst valid 12:00Z December 03 2007



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6-h PR

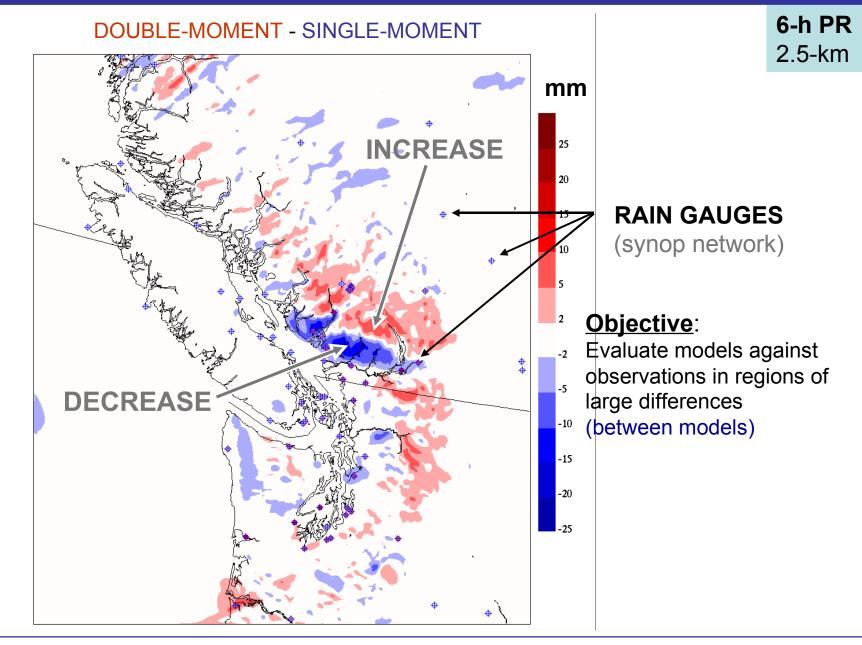
2.5-km

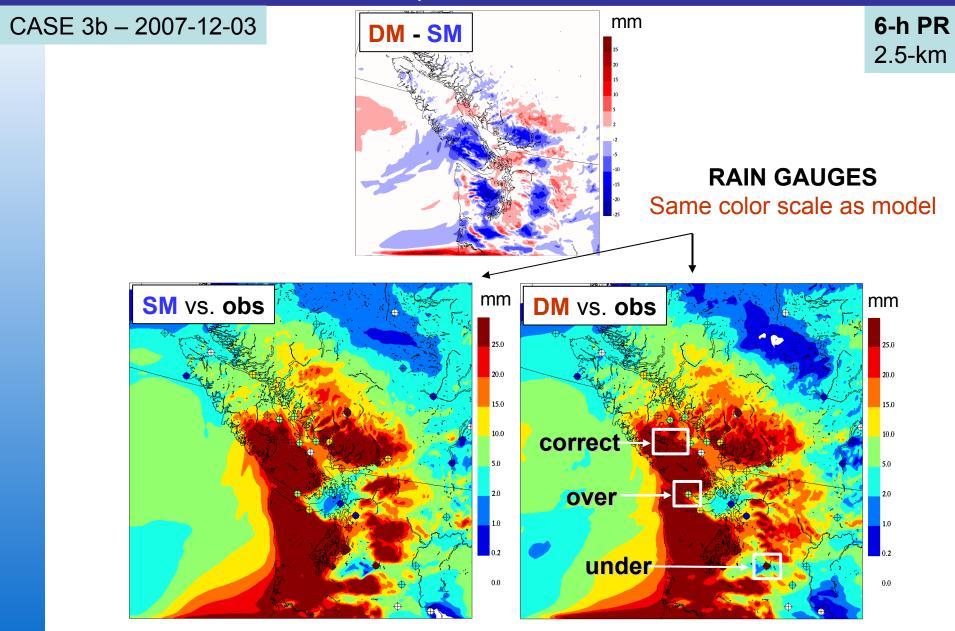


15 hour fcst valid 00:00Z December 04 2007

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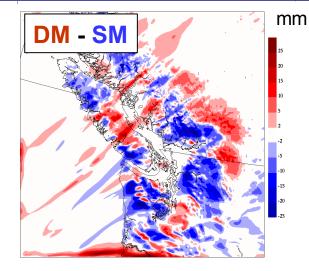




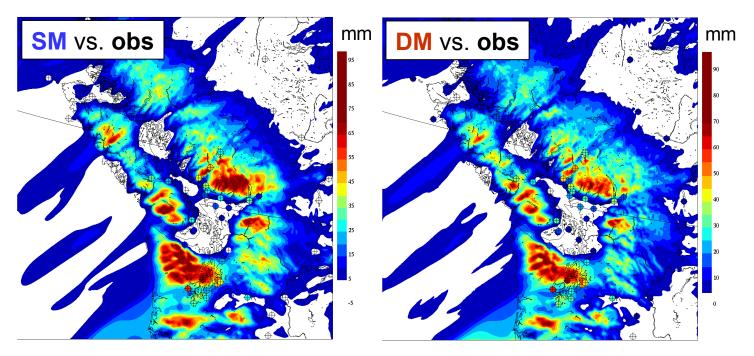
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CASE 4a – 2007-12-03

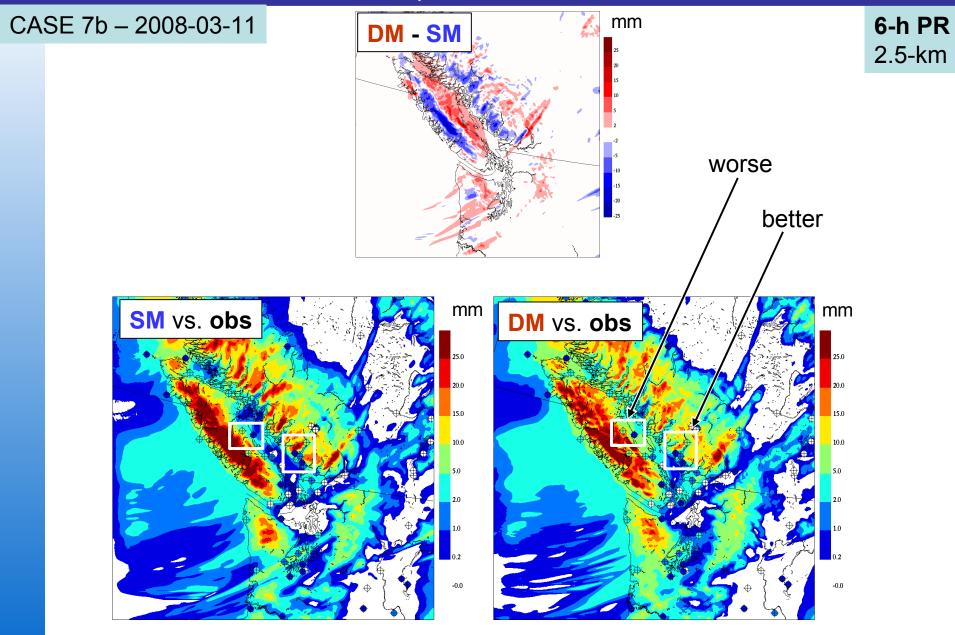






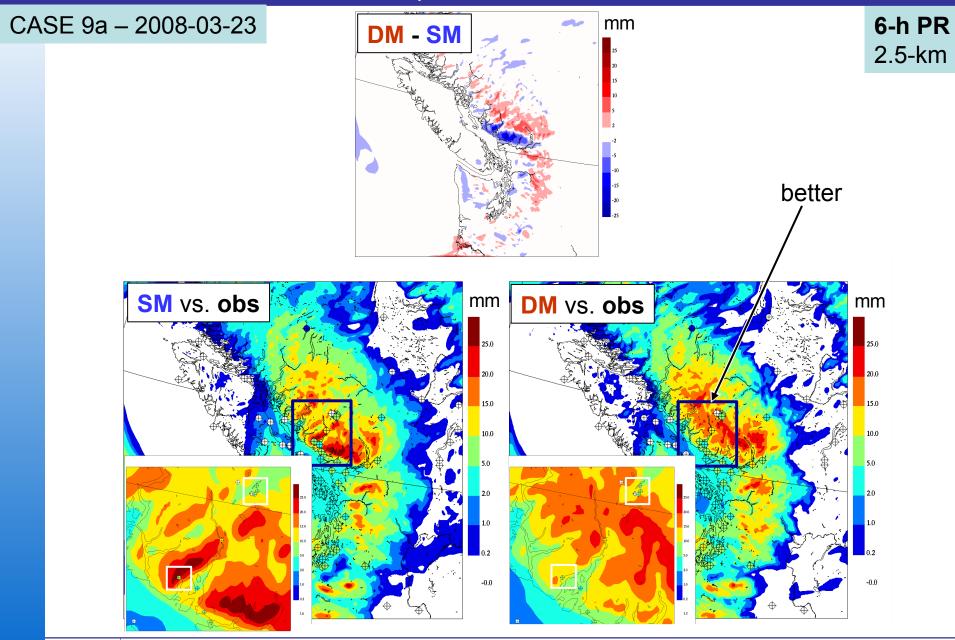


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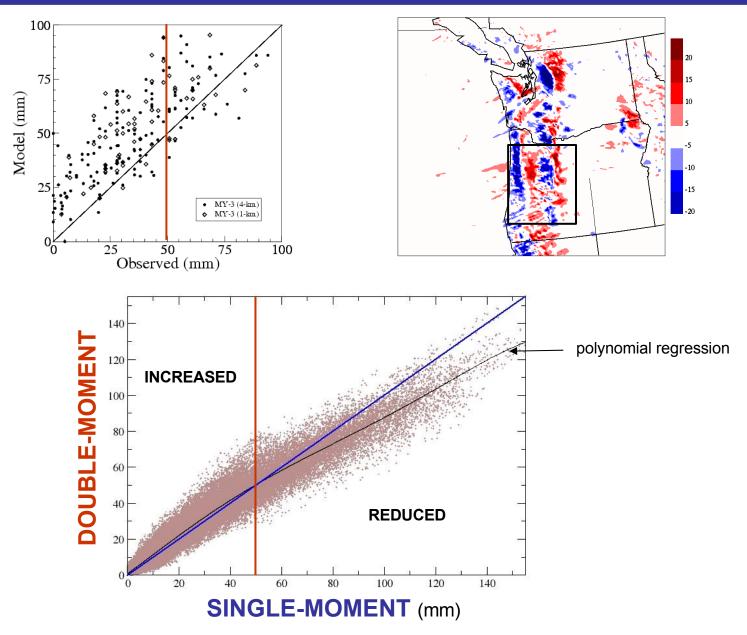
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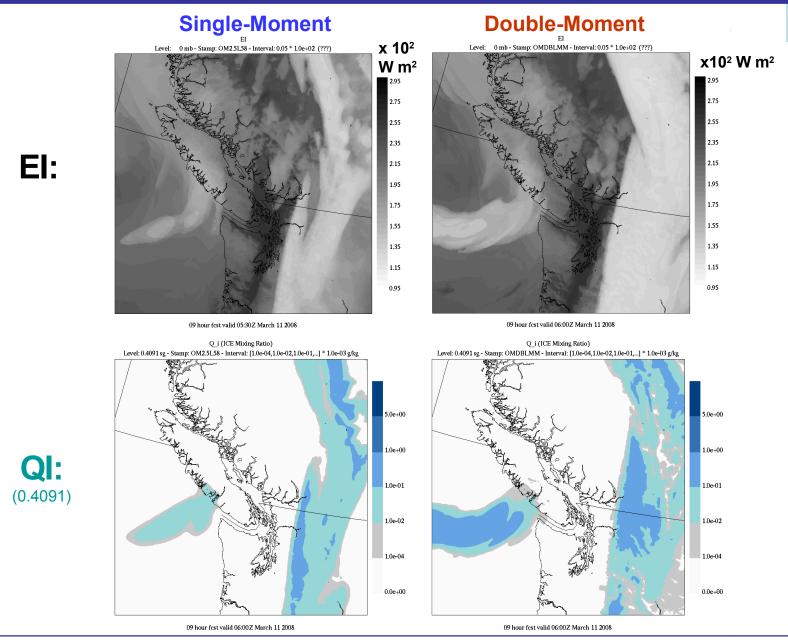
From 10 Cases, 20 6-h periods, 50-70 obs. points per period: (1335 gauges vs. model (2.5-km) points)

- Insufficient data to compute meaningful statistics
- Subjective evaluation indicates:
 - general tendency of reduced QPF (for large amounts)
 - systematic downwind shift in location (along coast and mountains)
 - location of gauges makes evaluation difficult

 \rightarrow but this appears to be a general improvement (consistent with change in snow-graupel mass balance)



3. Evaluation – Microphysical Fields and Outgoing Longwave Radiation

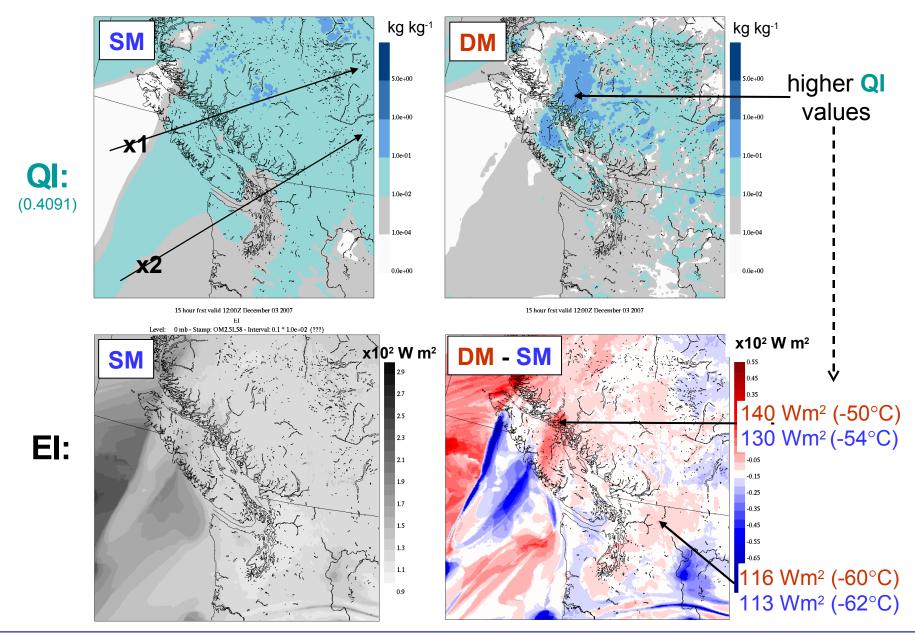


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2.5-km

3. Evaluation – Microphysical Fields and Outgoing Longwave Radiation

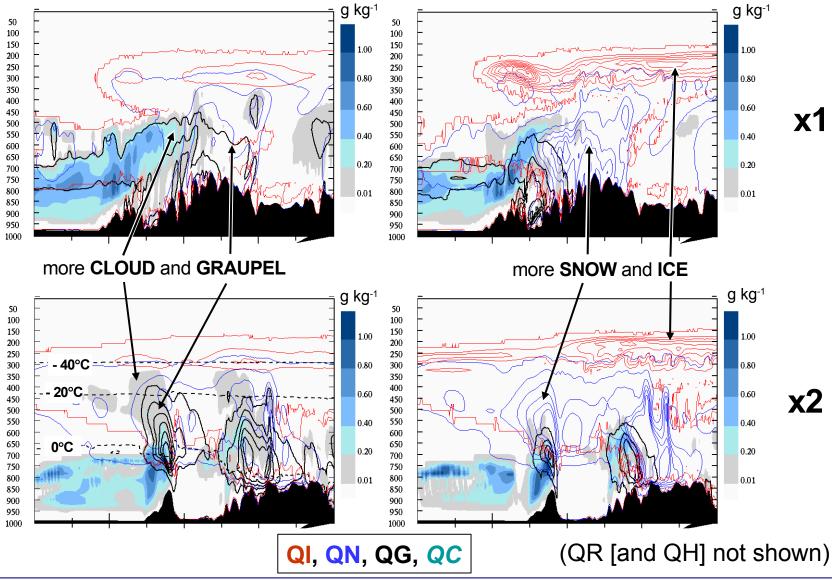


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Single-Moment





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OVERALL DIFFERENCES:

- Broader and brighter OLR patterns (in DM) associated with larger quantities of upper-level ICE
- Improvement in *CLOUD* at high levels (no unrealistic large LWC at very cold temperatures)
- More ICE and SNOW ↔ less CLOUD and GRAUPEL (consistent with downwind shift in precipitation)

MORE REALISTIC?

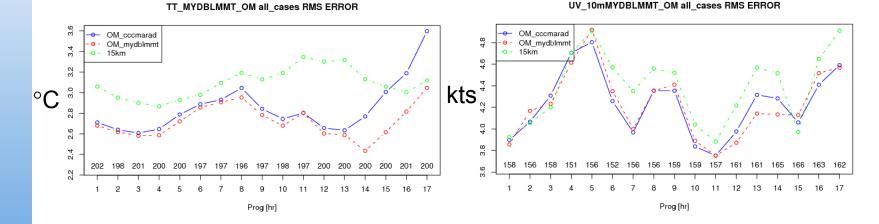
- yes and no (probably more yes than no)
- tunable, given more understanding of biases

2.5 km

Average of 10 Cases

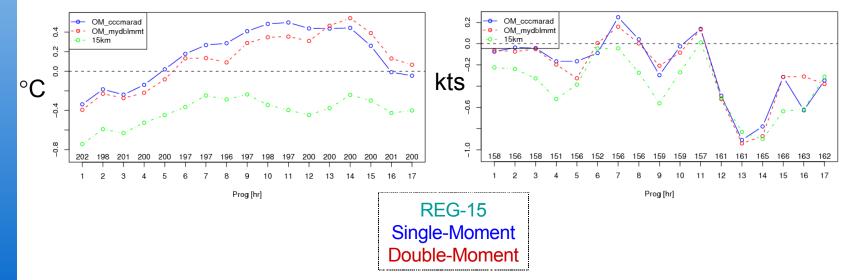
Temperature (2 m)

Wind Speeds (10 m)



TT_MYDBLMMT_OM all_cases BIAS

UV_10mMYDBLMMT_OM all_cases BIAS

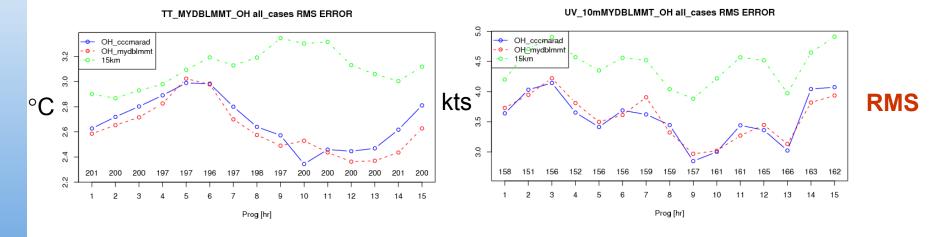


1 km

Average of 10 Cases

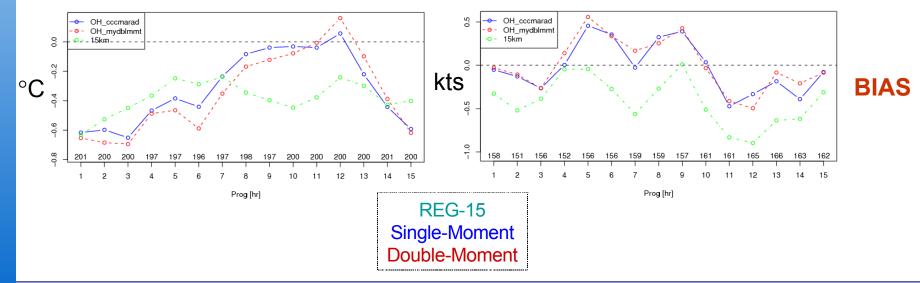
Temperature (2 m)

Wind Speeds (10 m)



TT_MYDBLMMT_OH all_cases BIAS

UV_10mMYDBLMMT_OH all_cases BIAS



Computational Cost:

10% additional total CPU time

With Double-Moment vs. Single-Moment (ave. of 10 runs)



4. Current and Upcoming Research



1. Snow Density

- Collaboration with Severe Weather National Laboratory (Denis Jacob)
- Verification against observations (regular GEM-LAM-2.5 grids)
- Comparison to other techniques (e.g. Dubé method)



2. Summer Convection

 Comparative study (against other microphysics schemes) on the ability to simulate the cold pool in a mid-latitude squall line



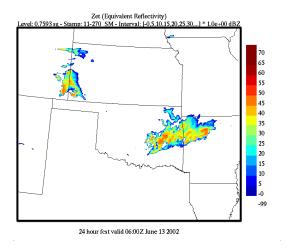
WMO 2008 International Cloud Modeling Workshop CASE 3:

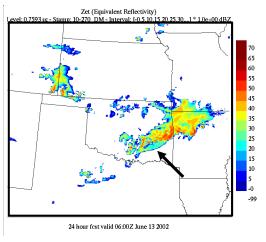
Reflectivity at 2 km AGL, 0600 UTC 13 June 2002 (36-h fcst)

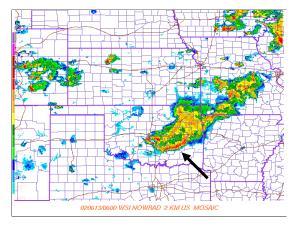
SINGLE-Moment

DOUBLE-Moment

WSI RADAR







2.5-km GEM-LAM simulations

- Initialized from 0000 UTC 12 June 2002 CMC analysis
- operational "regional" configuration (global-variable, $\Delta x \sim 15$ -km over North America)
- Nested to $\Delta x \sim 2.5$ -km grid at 1200 UTC (using Milbrandt-Yau cloud scheme)

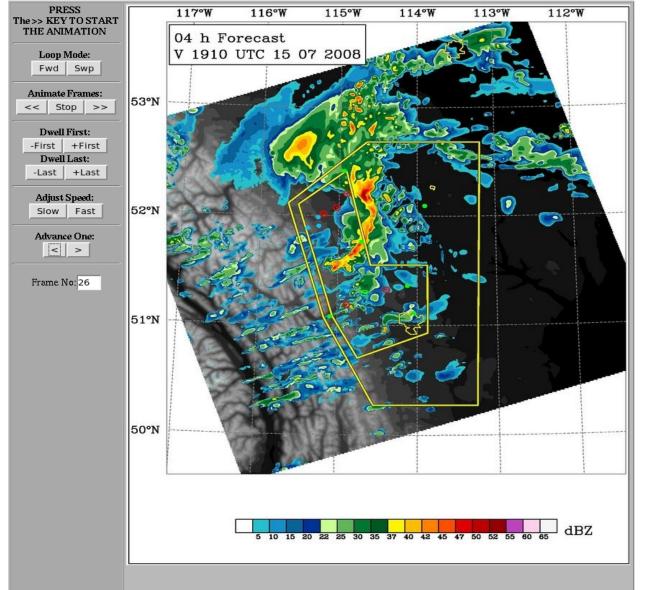
2. Summer Convection

- Comparative study (against other microphysics schemes) on the ability to simulate the cold pool in a mid-latitude squall line
- Performance of double-moment scheme for UNSTABLE





4. Current and Upcoming Research



Website snapshot for GEM-LAM-1km run (using double-moment M-Y)

Environment Environnement Canada Canada RPN Seminar Series, January 2009

2. Summer Convection

- Comparative study (against other microphysics schemes) on the ability to simulate the cold pool in a mid-latitude squall line
- Performance of double-moment scheme for UNSTABLE
 - a) 3 months of summer 2008 runs (archived)
 - b) 8 cases during IOP to be examined in detail

3. Large-scale ($\Delta x \ge 10$ km) version of M-Y scheme

- Introduction of subgrid-scale cloud fraction
 → for application in GEM-REG or meso-Global configurations
- Proper interaction of double-moment variables with radiation scheme (Polar-GEM, Frederick Chosson)



4. Other research projects (using M-Y scheme)

- Xue / Dawson University of Oklahoma: using triple-moment scheme to simulate tornadic supercells
- Benoit / Gayraud Université de Montréal: using double-moment (v5) scheme to simulate icing events in Gaspé region
- Yau / Naishi McGill University: using multi-moment scheme to simulate squall lines
- etc.

CONCLUSION

- The <u>double-moment version</u> of the M-Y scheme has been further optimized and developed, with emphasis on improving the <u>snow</u> category
- Several new fields are now available, including a prognostic snow density (giving an instantaneous solid-to-liquid ratio)
- Comparison to single-moment runs for 10 winter cases on the new VO2010 high-res forecast system reveal <u>systematic differences</u> in the new doublemoment version
 - Increased ice and snow and reduced cloud and graupel masses
 - corresponding <u>downwind shift</u> in the location of <u>precipitation</u>



CONCLUSION

The improvements to the proposed double-moment scheme are scientifically valid

While objective verification of high-resolution models remains difficult, our subjective evaluation indicates an overall improvement



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