1	Impacts of Predicted Liquid Fraction and Multiple Ice-Phase Categories
2	on the Simulation of Hail in the Predicted Particle Properties (P3)
3	Microphysics Scheme
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17	Key Points:
18 19	• Predicting the liquid fraction improves the parameterization of melting and results in reduced hail sizes.
20 21	• The use of multiple free ice-phase categories reduces the dilution of bulk physical properties of ice and increases hail sizes.
22 23 24 25	• With recent updates, the Predicted Particle Properties bulk microphysics scheme is well- suited for modeling hailstorms.

26 Abstract

Since its inception in 2015, the Predicted Particle Properties (P3) bulk microphysics scheme 27 has undergone several major developments. Ice is now represented by a user-specified number of 28 freely-evolving (non-prescribed) categories; the liquid fraction of particles is predicted, thereby 29 allowing for mixed-phase particles and improved process rates; and the scheme is triple-moment, 30 which allows the size spectral width to vary independently. As such, P3 is now capable of 31 representing key properties and microphysical processes that are important for hail. In this study, 32 the impacts of some new capabilities of P3 on the simulation of hail amounts and sizes are 33 examined in the context of quasi-idealized, high-resolution (200-m isotropic grid spacing) 34 simulations using a cloud-resolving model. Two hailstorm cases are simulated, one from 35 Oklahoma (US) and the other from Alberta (Canada), each initialized from qualitatively different 36 37 soundings. For each case, sensitivity tests are conducted to examine the impacts of 1) the 38 predicted liquid fraction, and 2) the number of free ice-phase categories (varied between one and four). Predicted liquid fraction leads to a more realistic treatment of melting and shedding, which 39 decreases mean ice (hail) sizes during melting compared to the original P3 scheme. In contrast, 40 with an increasing number of ice-phase categories, the problem of property dilution is mitigated, 41 resulting in greater quantities and larger sizes of hail reaching the surface. It is argued that the 42 43 latest version of the P3 scheme is now capable of realistically representing the major

44 microphysical processes involved in the initiation, growth, and decay of hail.

45

46 Plain Language Summary

The Predicted Particle Properties (P3) scheme is a piece of computer code, used in atmospheric 47 numerical models, that calculates the bulk effects of cloud processes that ultimately lead to 48 49 precipitation. Since its inception in 2015, the P3 scheme has undergone several major 50 developments. Ice-phase particles are now represented by a user-specified number of freely evolving generic categories; P3 now predicts the liquid fraction which allows for mixed-phase 51 particles and more accurate calculations of physical processes; and there is flexibility in 52 53 representing the distribution of ice particle sizes. With these features, P3 is now capable of simulating the physical processes related to the growth and decay of hail. In this study, the 54 impacts of the new features on the simulation of hail were examined using a fine-scale, detailed 55 numerical model capable of simulating individual storms. Two hailstorm cases were simulated, 56 each with different pre-storm environments in order to illustrate the robustness of the 57 conclusions. The predicted liquid fraction was shown to improve the simulation of hail melting 58 and resulted in smaller hail at the surface. In contrast, the use of two or more ice-phase 59 categories allowed for the simulation of larger hail sizes. 60

61

63 **1 Introduction**

A major component of an atmospheric model is the bulk microphysics scheme (BMS), which 64 parameterizes the effects of grid-scale clouds and precipitation. Despite the existence of more 65 detailed approaches, bin-resolving and Lagrangian super-particles schemes, BMSs continue to 66 play important roles in research and are ubiquitous in operational numerical weather and climate 67 prediction models. This is expected to continue into the foreseeable future. Since ice was 68 introduced into single-moment schemes decades ago (e.g., Rutledge & Hobbs, 1983), the 69 treatment of ice-phase microphysics has become increasingly sophisticated. Over the years, more 70 categories were added to expand the range of properties of frozen particles represented in 71 72 models, in particular terminal fall speeds (e.g. Lin et al., 1983). Detailed two-moment schemes later become popular (e.g. Ziegler, 1985; Murakami et al., 1990; Ferrier, 1994; Meyers et al., 73 74 1997; Reisner et al., 1998; Seifert & Beheng, 2006; Morrison et al., 2005; Morrison et al., 2009). Three-moment schemes then followed (Milbrandt & Yau, 2005a,b; Yang & Yau, 2008; Dawson 75 et al., 2014; Loftus et al., 2014; Chen & Tsai, 2016). More recently, the prognostic volume 76 mixing ratio for rimed ice categories (graupel and hail) was included in some schemes, which 77 allows for the prediction of the bulk particle density (Mansell et al., 2010; Milbrandt & 78 79 Morrison, 2013; Jensen et al., 2023; Park et al., 2024). Tsai & Chen (2020) developed a BMS 80 which, in addition to bulk density, predicts the shape evolution of the ice-phase categories. Thompson & Eidhammer (2014) included prognostic aerosols, which ultimately is important in 81 82 determining droplet sizes; this in turn impacts the rime density in the most recent version of this scheme, which now includes prognostic graupel density. With all of these predictive aspects, 83 84 BMSs are now capable of simulating the key microphysical processes involved in the production

and growth of hail.

Despite many advances, most BMS are still constructed around the original approach of using 86 87 pre-defined ice-phase categories (e.g. "snow", "graupel", etc.) usually with fixed parameters to define or diagnose the values of bulk physical properties. This traditional approach has some 88 inherent and insurmountable weaknesses. First, the properties of natural ice particles vary 89 considerably. This is in contrast with liquid drops and droplets, whose density is constant and 90 91 with spherical shape (except for large drops). Perhaps most importantly, the traditional approach requires the parameterized process of conversion between categories; this process is unphysical 92 and is purely a necessary artifact of the construction of the scheme. It is therefore unconstrained 93 by observations or theory and its closure assumptions introduce model sensitivity (Morrison et 94 al., 2020). Note that these problems are equally inherent to most bin microphysics schemes, 95 96 which is illustrated clearly in Xue et al. (2017).

An alternative to traditional, pre-defined ice category-based schemes is the property-based
approach, which uses one or more ice-phase categories that do not correspond a priori to a
particular ice type. That is, categories are not assigned a type with corresponding fixed
parameters, but rather each category includes a set of prognostic variables from which physical
properties can be derived and vary continuously in time and space. The first property-based

- 102 microphysics scheme can probably be credited to Hashino & Tripoli (2007), though this was a
- 103 bin scheme. The Predicted Particle Properties (P3) scheme was introduced by Morrison &
- 104 Milbrandt (2015), who proposed the concept of a "free" (freely evolving) bulk ice-phase
- 105 category. Jensen et al. (2017) also constructed a property-based bulk scheme called Ice-
- 106 Spheroids Habit Model with Aspect-Ratio Evolution (ISHMAEL), with a unique capacity to
- 107 predict the evolution of the aspect ratios of ice crystals. To our knowledge, these are the two only
- 108 property-based BMSs that have been developed that completely eschew traditional ice
- 109 categories.
- Although the P3 scheme was originally constructed as a proof of concept, it initially performed
- 111 well against detailed, mature, well-calibrated, traditional BMSs. This was true for both historic
- 112 case studies (Morrison et al., 2015) and in a real-time experimental numerical weather prediction
- 113 (NWP) context (see Milbrandt et al., 2021). It was (and is) also computationally efficient due in
- 114 part to its extensive use of pre-computed lookup tables during run time (Morrison et al., 2015). It
- has since been interfaced with several mesoscale and large-eddy simulation (LES) models; it has
- been used operationally since 2018 in the 2.5-km deterministic NWP system of Environment and
- 117 Climate Change Canada (ECCC) (Milbrandt et al., 2016; Milbrandt et al., 2018) and it is
- available in the Weather Research and Forecasting model (WRF; Skamarock et al., 2008) and the
- 119 Energy Exascale Earth System Model (E3SM) climate model (Wang et al., 2021). Since its
- 120 inception, P3 has undergone several major developments. This includes the generalization to
- 121 multiple ice-phase categories (Milbrandt & Morrison, 2016), prognostic liquid fraction of
- particles (Cholette et al., 2019), a triple-moment representation of ice (Milbrandt et al., 2021),
- and a diagnostic subgrid-scale cloud fraction (Jouan et al., 2020). A triple-moment rain version
- 124 was also developed (Paukert et al., 2019) though this was not incorporated into the main P3 code
- 125 stream.
- 126 Although the P3 scheme is now quite mature and its representation of ice is highly versatile,
- some aspects have not yet been examined with regards to their impacts on the simulation of hail.
- In a study using idealized supercell simulations, Johnson et al. (2019) compared the performance
- of P3 to that of two detailed traditional BMSs and found P3 to perform poorly in comparison for
- 130 the simulation of dual-polarization radar signatures for hail. These deficiencies were alleviated
- by the introduction of triple-moment ice (and also improved for a modified double-moment ice
- 132 configuration) in Milbrandt et al. (2021), which relaxed the restriction of mean ice sizes by
- varying the particle size spectral width and controlling gravitational size sorting. The impacts of
- 134 other potentially important recent innovations to P3 have not yet been explored.
- 135 The goal of this study, therefore, is to examine the following question: What are the impacts on
- the simulation of hail from 1) the predicted liquid fraction, and 2) multiple free ice categories?
- 137 This is examined using quasi-idealized high-resolution (200-m grid spacing) cloud model
- 138 simulations using the latest version (v5) of P3 for two deep convective hail-producing storms in
- 139 different environments.

140 The remainder of the paper is organized as follows: Section 2 describes the experimental

design, including the cloud model configuration and the two idealized hailstorm cases. Section 3

summarizes the control simulations for the two cases. Section 4 presents the results of two sets of

- sensitivity experiments, one looking at the effects of liquid fraction and the other on using
- different numbers of ice categories. Discussion is provided in section 5 with concluding remarks
- in section 6.

146 2 Experimental design

147 2.1 Overview of the P3 scheme

A complete description of the original single-category version of the P3 scheme is provided in 148 Morrison & Milbrandt (2015) and an overview of the most recent version (at the time of 149 writing), with details on how triple-moment ice and predicted liquid fraction were combined, is 150 given in Cholette et al. (2023). The liquid-phase component of P3 is a standard two-category 151 ("cloud droplets" and "rain"), two-moment (prognostic mass and number) formulation, with a 152 gamma particle size distribution (PSD) for each category. Ice is represented with a user-specified 153 number (nCat; all symbols are defined in Table A1) of free ice-phase categories. The PSD of 154 each ice category is also represented by a gamma function. For all hydrometeor categories, the 155 PSD is of the form 156

$$N(D) = N_0 D^{\mu} e^{-\lambda D}, \tag{1}$$

where N(D) is the number of particles between D and D + dD, D is the equivalent diameter, and 158 N_0 , λ , and μ are the intercept, slope, and shape parameters, respectively (see Table 1 for units). 159 There are between four and six prognostic mixing ratio variables per ice category: the total mass 160 $(Q_{i,tot})$, rime mass $(Q_{i,rim})$, total number $(N_{i,tot})$, rime volume $(B_{i,rim})$, and optionally the sixth 161 moment (Z_i) and liquid mass accumulated on ice $(Q_{i,liq})$. Since all of these quantities are mixing 162 ratios, they are conserved and can be advected and diffused appropriately. Note, $Q_{i,tot}$ is the total 163 mass of a given ice (in general, mixed-phase) category, n, equal to the sum of $Q_{i,lia}$, $Q_{i,rim}$, and the 164 deposition mass (which can be computed but is not actually a prognostic variable) for the 165 category. The actual total mass of ice- or mixed-phase particles (e.g. in a grid element) is the sum 166 of all $Q_{i,tot}(n)$ for *n* from 1 to *nCat*. 167

168 From these prognostic variables, various bulk physical properties can be computed, including

169 the rime fraction (F_{rim}), liquid fraction (F_{liq}), density (ρ_i), mass-weighted mean terminal fall

speed (V_m) (and also the number-weighted and sixth moment-weighted fall speeds, for the

sedimentation of $N_{i,tot}$ and $Z_{i,tot}$, respectively), and mass-weighted mean diameter (D_m). In this

study, we also examine the maximum hail size, $D_{h,max}$, which can be diagnosed from the tail of

the PSD following the method described in Milbrandt et al. (2021).

174 An overview of the representation of ice (and mixed-phase particles) and the major

175 growth/decay processes is depicted in Fig. 1. Pristine crystals can be initiated from either

176 primary nucleation, homogeneous freezing of cloud droplets, or secondary ice production (SIP).

- 177 Currently the only SIP mechanism included is rime splintering, but in the near future other
- modes will be added, such as the fragmentation of freezing drops, which was shown to be
- important for tropical convection (see Qu et al., 2022). Ice can grow (or decay) from deposition
- 180 (sublimation), undergo aggregation, both within a given ice category and between categories,
- and grow gradually from riming. With the predicted liquid fraction, liquid can remain on the
- particles during wet growth and possibly re-freeze before being shed as rain. During melting, the small ice sizes in the PSD melt instantly to rain while the remaining ice mass is retained as
- small ice sizes in the PSD melt instantly to rain while the remaining ice mass is retained as partially-melted mixed-phase particles. Shedding during melting and wet growth is computed
- explicitly with the prediction of liquid fraction. Mixed-phase particles can also re-freeze if they
- fall or are transported into subfreezing air. As in the original scheme, rain can freeze to solid
- 187 (maximum-density) ice via either immersion freezing or through collisions with existing ice.
- 188 Thus, hail embryos can originate from either graupel or frozen drops, and since freezing has a
- 189 drop-size dependence there is an indirect dependence on aerosols for the origin of hail embryos.
- 190 (Currently P3 does not have prognostic aerosol concentrations, though this will be implemented
- in the near future.)

193 **Table 1.** List of simulation configurations. Runs are named with the convention *case-*

194 *configuration*. The *case* is either "OK" or "AB" to denote the Oklahoma [date] or Alberta [date]

case, respectively. The control ("CTR") configuration has predicted liquid fraction off and uses

one ice category. "LF" denotes liquid fraction on. For multi-ice-category runs, (x) in "(x)CAT"

¹⁹⁷ indicates the number of ice categories, which is implicitly 1 if not indicated. "MOD" denotes

198 modified; see main text for details. All simulations use 3-moment-ice.

Run name	Liq-Frac	nCat
OK-CTR	off	1
OK-LF	on	1
OK-CTR-MOD	off	1
OK-LF-MOD	on	1
OK-LF-2CAT	on	2
OK-LF-3CAT	on	3
OK-LF-4CAT	on	4
AB-CTR	off	1
AB-LF	on	1
AB-LF-2CAT	on	2
AB-LF-3CAT	on	3
AB-LF-4CAT	on	4



Representation of Ice/Mixed-Phase Hydrometeors in P3

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Figure 1. Depiction of the representation of ice-phase and mixed-phase hydrometeors and the main microphysical processes related to ice in P3.

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205 2.2 Summary of idealized simulations

In order to establish robustness of the results, this study examined two hailstorm cases, each 206 with different geographical locations and pre-storm environments. The first is from Oklahoma, 207 USA on 1 June 2008. The observed storm had a warm cloud base, implying an increased 208 209 likelihood of predominantly frozen-drop hail embryos (Young 1993), high CAPE, and was observed to produce hail sizes at the surface up to 10 cm. This was also the case used in 210 Milbrandt et al. (2021). The second case was from Alberta, Canada on 13 June 2020. This case 211 had a colder cloud base, implying more likelihood of graupel embryos, relatively lower CAPE, 212 yet the observed storm produced a prolific quantity of large hail. The initial sounding for the 213 Alberta case also had stronger mid-to-upper-level vertical shear. The two cases are hereafter 214

referred to as the OK (Oklahoma) and AB (Alberta) cases.

This study is done through examination of quasi-idealized cloud-resolving numerical 216 217 simulations using the Cloud Model 1 (CM1) model (Bryan & Fritsch, 2002). CM1 is a nonhydrostatic fluid flow model, commonly used to simulate various atmospheric phenomena. 218 We used the compressible dynamics option with sub-time steps for acoustic modes and 5th order 219 advection of scalars using the Weighted Essential Non-Oscillatory scheme (Balsara & Shu, 220 2000). All simulations used a 200-m isotropic grid spacing and open lateral boundary conditions. 221 222 The domain sizes were 1000 x 1000 horizontal grid points for OK and 1250 x 1250 for AB, both with 100 vertical levels. The model time step was 2 s. A Rayleigh damping layer was applied to 223 the uppermost 5 km of the model with a damping timescale of $1/300 \text{ s}^{-1}$ toward the base state 224 225 sounding. The upper and lower boundaries were free slip and surface heat fluxes were zero. 226 Horizontally homogeneous initial conditions were used, based on a single sounding for each case (see below). Subgrid-scale mixing used the 1.5 order prognostic turbulent kinetic energy method 227 similar to Deardorff (1980). Radiation and all other physical processes besides microphysics 228 were neglected. Convection was initiated using the vertical motion nudging method of Naylor & 229 Gilmore (2012), with an ellipsoidal region (with a horizontal radius of 15 km and a vertical 230 radius of 1500 m) of vertical motion (peaking at 10 m s⁻¹ in the center), with an inverse e-folding 231 time of 0.5 s⁻¹, and nudging decreasing to zero over 20 min. For each case, a control

- time of 0.5 s^{-1} , and nudging decreasing to zero over 20 min. For each case, a control configuration was run along with sensitivity tests related to prediction of liquid fraction and the
- number of ice-phase categories. All simulations examined in this study are listed in Table 1.

The soundings used to initiate each case, shown in Fig. 2, were taken from operational NWP 235 models. The OK sounding was extracted from the 0100 UTC 1 June 2008 Rapid Update Cycle 236 (RUC) analysis near the region of the initiation of the observed storm (see Milbrandt et al., 2021 237 and references therein). The AB case was initialized from a 6-h model forecast sounding from 238 ECCC's Regional Deterministic Prediction System (RDPS), valid at 0000 UTC 14 June 2020, 239 near the city of Calgary, near the initiation region of the storm. The temperature and humidity 240 profiles were modified slightly to prevent initial instabilities. Also, the mean 0-6 km wind (the 241 approximate storm translation speed) was subtracted from the sounding winds such that the 242 model storms remained approximately in the domain center throughout the simulations. While a 243 detailed examination of the simulations is provided in the following section, an illustration of the 244 model storms for the control (CTR) runs for each case is shown in Fig. 3, with qualitative 245 comparisons to radar observations. This is not intended to serve as a verification per se, but 246 simply as an illustration of the overall realism of the simulated hailstorms. For the OK case, the 247 combination of $Z_H > 35$ dBZ with $Z_{DR} < 0.5$ dB in the observed storm (Fig. 3, top right panels) is 248 a dual-polarization radar signature for the presence of hail (e.g., Kumjian et al., 2010). The 249 model storm (OK-CTR) has a similar reflectivity structure with the presence of hail (high-250 density ice) along the right flank. For the AB case, the reflectivity of the observed storm (Fig. 3, 251 bottom right panel) had high values (> 60 dBZ) along the right flank near the surface (0.4° plan 252

253 position indicator [PPI]), indicative of hail at the surface. The model storm (AB-CTR; Fig. 3,

bottom-left panel) has a reasonably realistic reflectivity structure with a hail along the right edge

- of the reflectivity core. Thus, the model simulations for the two cases appear to be sufficiently
- realistic in terms of reflectivity structure and their production of hail at the surface that we can
- confidently use this model framework to examine the impacts of details in the microphysics
- scheme for the simulation of hail through model sensitivity tests.
- 259



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Figure 2. Initial soundings and hodographs for a) OK case, valid at 0100 UTC 1 June 2008, and
b) AB case, valid at 0100 UTC 14 June 2020. See main text for additional details. Sounding
plots were created using MetPy. Winds are in knots with conventional meaning for the barbs.

RADAR OBSERVATIONS



MODEL

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Figure 3. a) Low-level (800 m) Z_e (shading) and $Q_{i,tot}$ (black contours) from OK-CTR (50 min). b) Horizontal (Z_H) and differential (Z_{DR}) reflectivity from operational radar (see Milbrandt et al. 2021 and references therein for details). c) $Z_{e,c}$ (shading) and lowest-level $Q_{i,tot}$ (black contours) from AB-CTR (80 min). d) Z_H from operational ECCC radar (Strathmore, AB), 0.4 deg PPI. $Q_{i,tot}$ contours are 10⁻⁶, 0.001, 0.1, ... g kg⁻¹ (intended for illustration only).

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272 **3 Results of control simulations**

273 3.1 Choice of analysis times

In order to reduce the quantity of analysis presented, specific times are chosen for each case for

- which the microphysical fields are examined. The times selected are during the mature, quasi-
- steady stages of the model storms and are representative of the hail growth at other times.
- 277 Periods of the modeled storm evolution for the two cases are given in Fig. 4, which shows

- snapshots at various times for the column-maximum model equivalent reflectivity ($Z_{e,c}$) and ice mixing ratios ($Q_{i,tot}$) at the lowest model level, as well as the domain-maximum vertical motion.
- 280 The simulation times of interest chosen are 60 and 80 min for the OK and AB cases,
- respectively. At these times, both storms are well developed and produce hail at the surface. In
- the figures discussed below, vertical cross sections along the dashed lines in Figs. 5c,6c are
- shown. The cross-section lines are chosen subjectively (but consistently for each run) by the
- following criteria: the lines cross through the point of maximum $Q_{i,tot}$ at the lowest model level
- (or the point of maximum $Z_{e,c}$ if the near-surface ice field is zero) and at prescribed
- meteorological angles of 335° for OK case and 115° for AB case, from the rear to the front of the
- storms. For the remainder of the paper, microphysical fields are examined at these times and
- locations. However, the microphysical sensitivities discussed below are general and occur at
 other times (with occasional minor differences).



CTR Reflectivity (column-maximum) + $Q_{i(tot)}$ (surface)

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Figure 4. Column-maximum reflectivity ($Z_{e,c}$, shaded) and near-surface (lowest model level) ice mass mixing ratio ($Q_{i,tot}$, contours of 10⁻⁶, 0.001, 0.1, ... g kg⁻¹) at 40, 50, and 60 min (OK-CTR, top) and at 60, 70, 80 min (AB-CTR, bottom). Domain-maximum vertical motion (max. w) is indicated numerically in each panel. (Note, the $Q_{i,tot}$ contours are intended only to illustrate the location of hail near the surface.)

297 3.2 Case 1: OK 2008

Results for the OK-CTR run at 60 min are summarized in Fig. 5. The left column shows 298 299 vertical cross sections (see location in Fig. 5c) of the total ice, cloud water, and rain mass contents (Fig. 5a) and Z_e (Fig. 5b), the near-surface (first model level) Z_e and ice content (Fig. 300 5c) and the total and solid precipitation rates (Fig. 5d). The panels in the right column shows 301 various fields related to ice: the total ice mass content (Q_i) (which includes the liquid portion, 302 when relevant), number concentration (N_i), rime mass fraction (F_{rim}), liquid fraction (F_{liq} ; not 303 relevant for the CTR but plotted for consistency with subsequent figures), mass-weighed mean 304 density (ρ_1) , mass-weighted mean fall speed (V_m) , mass-weighted mean diameter (D_m) , and 305 maximum hail size $(D_{h,max})$. Note, the mass and number fields are converted from mixing ratios 306 to concentrations for the vertical cross-section plots. 307

308 Despite this run having only a single ice-phase category, overall distributions of the ice

- 309 physical properties are consistent with what one would expect in a strong deep convective storm.
- Most of the ice is heavily rimed ($F_{rim} > 0.7$; Fig. 5g), even the ice falling out of the anvil, owing to it originating within the strong convective updraft, with copious amount of liquid water
- available for riming (Fig. 5a), before being lofted and transported horizontally. In the convective
- core the ice has high density (Fig. 5i), large sizes (Figs. 5k), and fast fall speeds (Fig. 5j). At high
- altitudes (e.g. z > 10 km) in the anvil, the ice is small (Fig. 5k) and dense (Fig. 5i), with evidence
- of gravitational size sorting in forward part of the anvil, and larger mean ice sizes and fall speeds
- at lower elevations (Figs. 5k,j). Note that frozen drops are initialized as rimed ice, in order to
- 317 prescribe an initial bulk density as that of solid ice upon initiation. Technically this is not rime,
- but it allows the model to properly initiate and track the properties (density, shape). The
- maximum hail size, $D_{h,max}$, appears as the shaded regions in Fig. 51. The largest sizes are
- 320 constrained to a narrow shaft in the convective core, reaching the surface along the right flank
- 321 (Figs. 5c,d), while smaller hail is lofted and ejected into the anvil, melting before reaching the
- surface. With the liquid-fraction shut off for the control run, the F_{liq} field (Fig. 5h) is not
- 323 applicable (or could be considered zero by design).



Figure 5. OK-CTR simulation at 60 min. a) Vertical cross-sections of Q_i (shading), Q_c (black contours) and Q_r (red contours), with shading boundaries and contours of 0.1, 1, 3, 5, and 10 g m⁻³). b) Near-surface (lowest model level) Z_e (shading) and Q_i (contours; 10⁻⁶, 0.1, and 1 g m⁻³). c) Total (shaded) and solid (contours) surface precipitation rates (same shading boundaries/contours). Domain maximum and mean for each are indicated numerically. The right column has vertical cross sections of e) Q_i , f) N_i , g) F_{rim} , h) F_{liq} , i) ρ_i , j) V_m , k) D_m , and l) $D_{h,max}$. The line of the cross-sections is indicated in b). Note, all mass and number mixing ratios

332 (quantity kg⁻¹) are converted to concentrations (quantity m⁻³) for plotting. The dotted red

contours in b) and c) are the 30 dBZ $Z_{e,c}$ isopleths. The dotted line in l) denotes the 10^{-12} g m⁻³ Q_i isopleth.

336 3.3 Case 2: AB 2022

- 337 The storm structure for the AB-CTR simulation (Figs. 4d-f, 6a,b) is notably different from the
- 338 OK case (Figs. 4a-c, 5a,b), but the overall distributions of the ice physical properties are similar
- (Figs. 6e-l). There are some quantitative differences, such as lower values of F_{rim} (Fig. 6g) and ρ_i
- 340 (Fig. 6i) further downstream in the anvil, probably due to weaker updraft strengths in the AB
- case (Fig. 4) and thus less dominance of ice from frozen drops transported from the convective
- 342 core. However, the overall similarity of ice property distributions despite the different storm
- 343 structures lends support to the generality of the sensitivity test results presented below.







- 347 4 Microphysics sensitivity tests
- 348 4.1 Impacts of liquid fraction

The impacts of the prognostic liquid fraction are examined here. The ice fields are summarized 349 in Fig. 7 for OK-LF at 60 min in the left column (corresponding the right column of Fig. 5 for 350 OK-CTR) and for AB-LF at 80 min in the right column (corresponding to the right column of 351 Fig. 6 for AB-CTR). Most of the ice fields are quite similar to those of the corresponding CTR 352 353 runs, but with some notable and important differences. The F_{liq} field is now defined and while it is zero for most locations with ice present, it increases to 1 with decreasing height as the ice 354 melts (Figs. 7d,l). Although it is not apparent in Fig. 7, Fliq can also be non-zero in the hail 355 growth zone if the ice is undergoing wet growth. Also, with the predicted liquid fraction the 356 model reflectivity is more realistic in melting regions as a result of the bright band (not shown) 357 being accounted for (Cholette et al., 2023). The important impact of the inclusion of liquid 358 fraction pertaining to this study is that the quantity and size of ice/hail reaching the surface is 359 notably reduced in both cases (Figs. 7a,g,h,i,o,p). This is consistent with reduced domain-360 maximum and domain-mean solid precipitation rates for OK-LF and AB-LF (Table 2). 361

This significant reduction of hail reaching the surface is due to differences in the way melted 362 ice mass is treated with liquid fraction on and the closure assumptions pertaining to the ice 363 364 number tendency during melding and shedding, all of which we believe increase the realism of these parameterized processes in P3. With liquid fraction off, melting in P3 is treated as follows: 365 The amount of total ice mass that melts in one time step is computed, following the heat balance 366 equation (see Morrison & Milbrandt, 2015 for details), and is assumed to be immediately and 367 completely shed to rain. The $N_{i,tot}$ -tendency due to melting is parameterized using the closure 368 assumption of a constant mean-mass diameter D_{mm} , defined by 369

370
$$D_{mm} = \left(\frac{6}{\pi\rho_i} \cdot \frac{Q}{N}\right)^{1/3},\tag{2}$$

which is commonly used in multi-moment bulk schemes (e.g. Ziegler, 1985; Ferrier, 1994; Milbrandt & Yau, 2005b; Morrison et al., 2005; Mansell et al., 2010). In (2) and the equations below, the "*i*,*tot*" subscripts are excluded from $Q_{i,tot}$ and $N_{i,tot}$ for conciseness. Note that for a gamma size distribution, this is equivalent to assuming a constant slope (λ) and shape parameter (μ) for this process. With this assumption, the ratio $Q_{i,tot} / N_{i,tot}$ remains constant so $N_{i,tot}$ decreases proportionally to $Q_{i,tot}$ during melting, following

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$$\left(\frac{dN}{dt}\right)_{MELT} = \frac{N}{Q} \cdot \left(\frac{dQ}{dt}\right)_{MELT}.$$
 (3)

where $(dQ/dt)_{MELT}$ is the melting rate of $Q_{i,tot}$. With liquid fraction on, the treatment of the melted ice mass in P3 is physically more realistic (see Cholette et al., 2019 for details). In a given time step during melting, a portion of the solid mass, which is $Q_{i,tot} - Q_{i,liq}$ (i.e. deposition plus rime mass), melts to liquid. Small ice particles are assumed to melt completely in the time step and thus the mass goes directly to rain (Q_r) , with $N_{i,tot}$ decreasing as per (3) (for this portion of the melting only). The rest of the melted ice mass, however, is converted from solid to liquid but remains within the mixed-phase particles $(Q_{i,rim}$ decreases, $Q_{i,liq}$ increases, and $Q_{i,tot}$ remains the

- same), increasing the liquid fraction locally and with no change to $N_{i,tot}$. Shedding of liquid on
- mixed-phase particles is then calculated explicitly (see Cholette et al., 2019, 2023) and depends
- 387 on the rime mass fraction, where at the extremes unrimed ice does not shed whereas fully-rimed
- 388 ice sheds at the maximum rate. During shedding, $N_{i,tot}$ does not change while the rain mass and
- number increase. As a result, with liquid fraction on the melting of heavily rimed ice combined
- 390 with shedding tends to result in a decrease in the mean ice size, as per (2).

391 For unrimed or lightly-rimed ice, the differences in mass changes during melting and the

- impacts of this are significant since with liquid fraction on the melted mass remains in mixed-
- 393 phase particles, increasing their fall speed towards that of rain until the ice melts completely. For
- heavily-rimed ice, although there is a temporary transfer of most of the melted mass to liquid
- 395 within mixed-phase particles, most of this mass is quickly shed; thus, the mass transfer from 396 solid ice to rain is similar to that with liquid fraction off. However, the difference in the
- solid ice to rain is similar to that with liquid fraction off. However, the difference in the treatment of $N_{i,tot}$ during melting/shedding results in a much different change in D_{mm} , with the
- size decreasing much faster with liquid fraction on. This results in slower fall speeds, greater
- total surface area (since a given mass is distributed over more particles), and thus a faster mass
- 400 melting rate and ultimately melting hail is more likely to completely melt before reaching the
- surface. Therefore, with the exception of the change in $N_{i,tot}$ that can occur for the small melted
- fraction that goes directly to rain, for the melting that is first retained in the liquid portion of the
- 403 mixed-phase particles and then shed, $N_{i,tot}$ remains constant.



Figure 7. Bulk ice fields/properties for OK-LF (at 60 min, left) and AB-LF (80 min, right). The panels in each column correspond to those in the right column in Fig. 5.

Table 2. Total and solid surface precipitation rates at 60 min (OK case) and 80 min (AB case).

409 Units are in mm h^{-1} for domain-maximum and 0.001 mm h^{-1} for domain-mean values.

Run name	Total (max)	Total (mean)	Solid (max)	Solid (mean)
OK-CTR	102.51	59.085	1.28	0.056
OK-LF	76.52	62.082	0.00	0.000
OK-CTR-MOD	94.04	100.528	0.00	0.000
OK-LF-MOD	134.37	67.362	2.04	0.087
OK-LF-2CAT	103.44	95.499	0.01	0.000
OK-LF-3CAT	128.85	58.073	2.20	0.055
OK-LF-4CAT	53.94	62.703	0.23	0.005
AB-CTR	279.30	230.585	44.70	4.331
AB-LF	242.51	241.034	18.84	1.310
AB-LF-2CAT	313.78	297.526	139.32	7.814
AB-LF-3CAT	268.53	291.970	155.61	19.016
AB-LF-4CAT	234.70	302.090	84.38	6.181

410

411

To illustrate that the differences described above are indeed responsible for the reduced hail at 412 the surface in the OK-LF and AB-LF simulations with liquid fraction on, two sensitivity tests 413 were run (for the OK case only). For the first test (OK-CTR-MOD), the code in the OK-CTR 414 configuration was modified such that $(dN/dt)_{MELT}$ is set to zero, similar to the overall effect with 415 liquid fraction on in OK-LF (except for the portion of small ice melting directly to rain). In the 416 second test (OK-LF-MOD), the OK-LF configuration was modified such that $(dN/dt)_{MELT}$ is 417 computed by (3) following the closure assumption for melting in OK-CTR, with $(dN/dt)_{SHED}$ set 418 to zero since it is implicitly included in melting. The impacts on ice mass and mean sizes near 419 the surface are shown in Fig. 8 (with fields from the unmodified OK-CTR and OK-LF also

the surface are shown in Fig. 8 (with fields from the unmodified OK-CTR and OK-LF also
shown in Figs. 5 and 7, repeated to facilitate comparison). The OK-CTR-MOD run (Fig. 8d,e,f)

422 is now similar to the OK-LF run (Fig. 8g,h,i), with no ice mass reaching the surface. Both D_m

423 and $D_{h,max}$ are reduced, and the solid precipitation reaching the surface is now zero (Table 2).

424 Conversely, OK-LF-MOD (Fig. 8j,k,l) is similar to OK-CTR (Fig. 8a,b,c), with ice/hail reaching

the surface, increased particle sizes, and similar solid precipitation rates. Clearly, therefore, the

differences in the closure assumptions for the changes in $N_{i,tot}$ during melting/shedding are

427 largely responsible for the notable reduction of hail at the surface with the liquid fraction on

428 configuration. The results for the same set of tests are qualitatively similar for the AB case (not

429 shown).



Figure 8. Vertical cross-sections of Q_i , D_m , and $D_{h,max}$ for OK case (at 60 min) for OK-CTR [top left; a), b), and c)], OK-CTR-MOD [top right; d), e), and f)], OK-LF [bottom left; g), h), and i)], and OK-LF-MOD [bottom right; j), k), and l)].



- related to melting/shedding for OK-LF are shown in Fig. 9. Here we partition melting into the
- portion of frozen ice mass that melts directly to rain (MELT1) and the portion that transfers
- frozen mass to liquid mass in the mixed-phase particle (MELT2). Figure 9a,b shows $(dQ/dt)_{MELT1}$
- and $(dN/dt)_{MELT1}$, respectively. The mean particle size due this sub-process remains constant.
- 440 Figure 9c shows $(dQ/dt)_{MELT2}$, which does not result in any change in $Q_{i,tot}$ (only a transfer from
- 441 ice to liquid that remains on the particle), with the mass loss rate due to shedding given by
- 442 $(dQ/dt)_{SHED}$ (Fig. 9d). The resulting rate of change of D_{mm} due to the combined melting and
- 443 shedding, $(dD/dt)_{MELT+SHED}$, is given by

444
$$\left(\frac{dD}{dt}\right)_{MELT+SHED} = \frac{1}{3} \left(\frac{\pi}{6} \rho_i\right)^{-\frac{2}{3}} \cdot \left[Q^{-\frac{2}{3}} N^{-\frac{1}{3}} \left(\left(\frac{dQ}{dt}\right)_{MELT1} + \left(\frac{dQ}{dt}\right)_{SHED}\right) - Q^{-\frac{1}{3}} N^{-\frac{4}{3}} \left(\frac{dN}{dt}\right)_{MELT1}\right], \quad (4)$$

- and is shown in Fig. 9e. Clearly the mean size of hail that melts and sheds in the convective
- 446 cores ($x \sim 25$ km) decreases with the liquid fraction configuration. Note, in computing (4)
- (which is only diagnostic, for Fig. 9e) ρ_i is held constant for simplicity, so in fact (4)
- underestimates the rate of decrease in mean particle size. This is because for MELT2, although
- there is no change in total mass or number, frozen mass is transferred to liquid $(Q_{i,lia})$ which
- 450 increases the mean particle density, thereby decreasing the mean size as per (2).



Figure 9. Process rates related to melting and shedding for OK-LF (at 60 min): a) and b) $Q_{i,tot}$ and $N_{i,tot}$ tendencies, respectively, due to complete melting (to rain) of small particles (MELT1); c) Tendency for mass transfer from solid to liquid within mixed-phase particles due to melting (MELT2); d) $Q_{i,tot}$ tendency due to shedding; e) D_{mm} tendency due to combination of melting to rain and shedding calculated from (4). See main text for details. Positive values denote decreases.

- If we believe that the LF configuration indeed allows for a more realistic representation of
- melting and shedding, and also for representing complex mixed-phase winter precipitation
- 461 (Cholette et al., 2019, 2024), a way to improve this in the liquid fraction-off configuration may
- 462 simply be to replace the constant D_{mm} closure assumption for melting with the one tested in OK-
- 463 CTR-MOD, at least for large values of F_{rim} . This may be considered for future versions of P3 464 since there is some computational cost associated with LF configuration (due to the additional
- 465 prognostic variable, $Q_{i,liq}$). Similarly, the $(dN/dt)_{MELT} = 0$ approach may be a simple improvement
- 466 in traditional bulk schemes for the graupel and hail categories that do not include prognostic
- 467 liquid fraction. Note that an alternative approach to mitigating the assumption of (3) was
- explored by Mansell et al. (2020), guided by detailed bin scheme calculations of hail melting. It
 should also be noted that Loftus et al. (2014) predicted the liquid fraction (via prognostic heat
- 470 content) for hail.

Shedding also happens during wet growth which can, in principle, be modeled more realistically with the predicted liquid fraction. With liquid fraction off, the shedding rate (mass) is computed as the dry growth rate (i.e. the total accretion rate of liquid water) minus the wet growth rate, computed from a heat balance equation, based on the Shuman-Ludlam limit (Young, 1993). With liquid fraction on, this difference in unfrozen collected mass remains as liquid on the particles (F_{liq} increases); shedding of a portion of this liquid is then computed separately. This is depicted in Fig. 1. Thus, wet hail can be represented and the liquid remaining can re-

freeze onto the existing ice once wet growth stops, so in principle hail can acquire larger mass

479 contents and sizes. This is a potentially interesting (and aesthetically curious) aspect of the

liquid-fraction configuration of P3 and it will be examined in a future study. However, the

capacity to model wet hail growth is probably much less important than the improved capacity to

model the melting/shedding of ice in general, including for the simulation of hail at the surface.

483

484

4.2 Impacts of the number of ice categories

As illustrated in section 3.1, even with a single ice category P3 can simulate a wide and 485 continuous range of ice particle physical properties, and hence a wide range of frozen 486 hydrometeor types. With the liquid fraction configuration, mixed-phase particles can also be 487 represented and the associated microphysical processes better modeled. The limitation, however, 488 is that only a single set of properties – and hence one dominant particle type – can be present at a 489 given point in time and space. The multi-category configuration of P3 removes this limitation 490 and allows for multiple sets of properties, and thus multiple modes, to coexist and to evolve 491 492 independently. The details of ice initiation into a given category and the merging of categories 493 with similar properties are explained in Milbrandt & Morrison (2016).

To examine the impact of multiple categories on the simulation of hail, a second set of sensitivity runs for each case was conducted, increasing the number of categories (nCat) from 1 to 4 (incrementally). All of these runs were with liquid fraction on, thus the control runs for this

- 497 analysis become OK-LF and AB-LF. The fields for each of the ice categories in OK-LF-2CAT
- are shown in Fig. 10. At any given location, the physical properties are quite often different
- between the two categories, and are also different from the single-category run, OK-LF (Fig. 7).
- 500 With the 3-category run (OK-LF-3CAT, Fig. 11), not only is the ice in category 3 (Fig. 11, right
- column) different from the other two, but the ice in categories 1 and 2 of OK-LF-3CAT (Fig. 11,
- ⁵⁰² left and middle columns) are different from those of OK-LF-2CAT (Fig. 10). For example, the
- mean particle sizes are much larger (> 10 mm) in category 2 for the ice at lower levels in the anvil (Fig. 1110) than those of category 2 in OK-LF-3CAT (Fig. 100), with D_m values < 4 mm.
- anvil (Fig. 1110) than those of category 2 in OK-LF-3CAT (Fig. 100), with D_m values < 4 mm. These differences emphasize that a given ice category in the multi-category configuration is not
- predisposed to represent a particular mode/type of ice; each category is equally continuous and
- 507 variable. Also, a given category is not predisposed to a particular set of dominant properties,
- though for both OK-LF-2CAT and OK-LF-3CAT most of the ice mass resides in category 1 (top
- rows of Figs. 10, 11). The ice fields for each category of the OK-LF-4CAT run (not shown)
- support this further. These results are consistent with the simulations for the AB cases, discussed
- 511 below.



Figure 10. As in the right column of Fig. 5 but for ice category 1 (left) and category 2 (right) for OK-LF-2CAT (60 min).







Figure 12 summarizes the "bulk" ice fields for all categories for the OK-LF-2CAT, OK-LF-519

- 3CAT, and OK-LF-4CAT simulations. For the total mass and number this is the sum of $Q_{i,tot}(i)$ 520
- and $N_{i,tot}(i)$ over all i in 1 to nCat (converted to mass and number concentrations, Q_i and N_i); the 521
- "total" F_{rim} and F_{liq} are computed from the appropriate sums of the ice fields; ρ_i , V_m , and D_m are 522
- mass-weighted averages of each category; and $D_{h max}$ is the maximum value amongst the 523
- 524 categories. These bulk fields can be compared directly to the 1-category run, OK-LF (Fig. 7). For

the AB case, the corresponding results for the multi-category simulations are shown in Figs. 13-15.

527 For both cases, despite the internal variability within the individual categories exhibited in Figs. 8, 9, 13, 14 (and also for the 4-category runs, not shown), the bulk fields are broadly similar 528 for all of the simulations, as well as to those of the 1-category runs (Fig. 7). However, there are 529 some important differences with respect to the simulation of hail with variation in the number of 530 ice categories. In general, the hail quantity and size increase as the number of ice categories is 531 increased. This is evident from the hail mass reaching the surface around the convective core ($x \sim$ 532 25 km, top rows of Figs. 7, 12, 15), the mean particle sizes D_m (second last rows), the maximum 533 hail sizes $D_{h,max}$ (last rows), as well as the domain-mean and domain-maximum solid 534 precipitation rates at those times (Table 2). For the 4-category runs the solid precipitation rates 535 are, on the other hand, lower (than the 3-category runs) at those particular times; however, there 536 is still abundant large hail reaching the surface (e.g. Figs. 12q,x, 15q,x), notably more than the 1-537 and 2-category runs (and the 3-category run for the AB case). Note, although periods of hail can 538 be intermittent and the results shown above are for individual cross-sections for snapshots in 539 time, these results were similar at other times during the simulations (not shown), and are similar 540 for both cases. Thus, this impact on hail with multiple ice categories in P3 can be considered 541

542 general.



544 Figure 12. Bulk ice properties from OK-LF-2CAT (left), OK-LF-3CAT (middle), and OK-LF-

545 4CAT (right) (60 min). The panels in each column are similar to those in the right column of Fig. 546 5, but are the sum (for Q_i and N_i) across all categories, the values computed from the appropriate

sums (for F_{rim} and F_{liq}), or the mass-weighted values (for ρ_i , V_m , D_m , and $D_{h,max}$) considering each

⁵⁴⁸ ice category.



Figure 13. As in Fig. 10 but for AB-LF-2CAT (80 min).



554 Figure 14. As in Fig. 11 but for AB-LF-3CAT (80 min).



Figure 15. As in Fig. 12 but for AB-LF-2CAT (left), AB-LF-3CAT (middle), and AB-LF-4CAT (right) (at 80 min).

The use of multiple ice categories increases the hail amount and sizes, which presumably is an 560 increase in the realism of the simulations because with the capacity to represent two or more sets 561 of physical properties in the same location the problem of property dilution is reduced. Property 562 dilution occurs when, for example two modes (i.e. sets of properties) that would otherwise exist 563 independently are represented with a single distribution; the result is a kind of averaging of the 564 properties, hence "dilution". For hail, this dilution can be detrimental to subsequent growth since 565 the particle properties such as fall speed and cross-sectional area are important in determining the 566 collection rate of liquid water. This is illustrated in Fig. 16 which is a zoomed-in view of some 567

- fields of bulk ice properties that impact hail growth rates for the 1-category (AB-LF) and 2-
- category (AB-LF-2CAT) simulations. Note the properties in the hail core region, around 5 km
- AGL and $x \sim 30$ km: for ice category 1 in AB-LF-2CAT, V_m is greater than 20 m s⁻¹ (Fig. 16d) and D_m is larger than 20 mm (Fig. 16e), whereas for category 2 in the same location V_m is 5-10 m
- and D_m is larger than 20 mm (Fig. 16e), whereas for category 2 in the same location V_m is 5-10 m s⁻¹ (Fig. 16g) and D_m is smaller than 3 mm (Fig. 16h). With a peak updraft speed of around 35 m
- s^{-1} (assuming a similar speed as AB-CTR at that time; Fig. 4f) this means that the particles in
- 574 category 1 can reside longer in the hail growth zone and grow to larger sizes, which is evident
- with the much larger values of $D_{h,max}$ (Fig. 16f). For the 1-category run (AB-LF), the property
- values in that region are in between those of the two categories in AB-LF-2CAT and the
- 577 maximum hail sizes at the surface are indeed smaller in the hail shaft region (Fig. 16c). Note, the
- 578 properties in this region in AB-LF cannot be interpreted as the literal average of the properties in
- categories 1 and 2 of AB-LF-2CAT since they are different simulations. However, the
- comparison in Fig. 16 is useful to illustrate how multiple ice categories in P3 reduce property
- dilution and allow for more realistic growth of larger hail, and ultimately to more hailfall at the
- surface and with larger sizes.







Although the simulations presented are quasi-idealized and without a rigorous "verification" 588 against observations, and evaluation against a numerical "truth" simulation is impossible since 589 no perfect microphysics scheme exists, it is reasonable to believe that the aspects of P3 explored 590 above improve the overall realism in representing ice-phase and mixed-phase microphysics in 591 592 general, including the modeling of hail. It may appear initially that liquid fraction is detrimental to simulating hail, given that, for example, OK-LF has no hail but OK-CTR does, as did the 593 observed storm. However, one must remember that the results from any numerical simulation 594 come from the sum of all components of the model and this can include compensating errors. For 595 melting of ice, the physics is better represented by a scheme that can model mixed-phase 596 particles and the gradual transfer of ice to liquid within the particles followed by shedding. So, 597 while the predicted liquid fraction appears to worsen the simulation of hail, at least for the OK 598 case, the simulation of the specific processes of melting and shedding most likely improved. In 599 the single category CTR configuration, the compensating error (or limitation) is the 600 601 representation of all ice in the updraft with a single set of physical properties at a given point in time and space (i.e., in a grid cell), including fall speed, which has the effect of limiting hail 602 growth to large sizes. Since all ice categories in multicategory configurations in P3 are subject to 603 the identical parameterized processes and since additional categories reduce property dilution 604 and hence improve the representation of the overall total ice, simulations should - in principle -605 always improve with an increased number of categories. 606

607 The multi-category P3 configuration could be optimized, or at least improved, such that there is a higher degree of "spread" of the properties amongst the various categories and thus a greater 608 mitigation of property dilution. In the multi-category configuration, newly initiated ice (by 609 primary nucleation, drop/droplet freezing, or secondary ice production) and ice in existing 610 categories are compared in terms of overall similarity of bulk properties. New ice is added to the 611 612 category that is most similar in terms of particle properties, or to a category containing no ice if one is available. At the end of the time step, ice categories that are evaluated as being similar are 613 merged into a single category in order to free up the category for new ice. In the current 614 configuration, D_m is used as the proxy to evaluate overall similarity, where two populations of 615 616 ice (two categories or new ice and a given category) are deemed to be similar if their difference in D_m is below a certain threshold (which is a prescribed parameter but is a decreasing function 617 of the number of categories; see Milbrandt & Morrison, 2016). The optimal similarity condition 618 depends on the number of ice categories used and on the type of weather being simulated, since 619 the ultimately purpose of multiple categories is to maximize the reduction of property dilution. In 620 order to simulate large hail optimally with multiple categories, one needs to be able to 621 distinguish ice that represents small graupel from ice that represents large hail. In this regard, the 622 use of D_m as a proxy for similarity is reasonable (as per the discussion above pertaining to Fig. 623 16), though it could likely be improved. In contrast, for a large-scale baroclinic system with 624 625 relatively little riming, the ability to distinguish graupel from hail is unnecessary so optimization likely means maximizing the ability to separate unrimed ice of different size ranges and/or 626 unrimed ice from rimed ice of similar mean sizes. The proxy for overall property similarity based 627

on D_m means that a population of high-density, heavily-rimed ice could be classified (by the

- current algorithm) as being similar to a population of low-density, unrimed ice with a similar
- 630 mean size and hence could be merged into a single category, thereby violating the principle of
- 631 minimizing property dilution. In a future study, we will explore and attempt to design an
- 632 improved multi-ice-category configuration of P3, optimized for a wide range of category
- 633 numbers and types of weather. This will likely use V_m as a similarity proxy and with three
- 634 categories to ensure the separation of unrimed ice, graupel, and hail.

Despite potential weaknesses in the current configuration, it is important to recognize that a 635 suboptimal multi-ice-category configuration of P3 is still a conceptual and effective 636 improvement compared to the 1-category configuration (though it could, in principle, lead to a 637 worse solution due to compensating model errors), but one with less improvement than is 638 639 possible. This is simply a logical deduction from the fact that all ice categories are treated with identical parameterized process and the premise that the separation of ice into "free" categories 640 in P3 reduces property dilution and improves representation of ice hydrometeors. There are two 641 extremes in which a multi-category configuration would be least optimal. In the first, if the 642 similarity condition is such that all newly-formed ice goes into the first available category such 643 that there is never any ice in any other category, then the solution will be identical to 1CAT. In 644 the second, all newly-formed ice gets nearly evenly distributed amongst all categories resulting 645 in virtually identical sets of properties – and thus subsequent growth rates – in each category, 646 647 therefore the solution would also be very similar to 1CAT (with tiny difference arising due to changes in order-of-operations calculations, etc.). Thus, any multi-category solution in P3 that is 648 different from the 1-category solution should, in principle, be more physically realistic since it 649 the differences result from being affected by multiple (and different) ice modes and modeling 650 their evolution independently. 651

Although in this study we extol the benefits of multiple ice-phase categories, this should not be 652 interpreted as a proposal to return to traditional pre-defined category-based schemes. In P3, the 653 categories are not in any way predefined; they all are subject to the identical parameterized 654 process rates and can each represent any type of ice-phase or mixed-phase particle depending on 655 the history of conditions at different locations and times. The merging of two P3 ice categories 656 into one is not comparable to, for example, the conversion from snow to graupel in a traditional 657 scheme. Despite the use of fixed parameters as a proxy for similarity, merging is not conversion 658 since it is done between categories that are deemed to be similar, rather than being done to 659 produce a hydrometeor type that is different, as in traditional schemes. A suboptimal P3 660 configuration, with a poorly chosen similarity criterion, is bound to be less harmful (i.e. result in 661 less sensitivity) than traditional conversion processes based on arbitrary and unconstrained 662 thresholds as was shown, for example, in Morrison & Milbrandt (2011) where there was a large 663 sensitivity of supercell simulations to whether the traditional BMS favored graupel or hail. 664

665 Perhaps somewhat ironically, in addition to illustrating the benefits of multi-category P3 for 666 the simulation of hail, the results presented in section 4.2 also strongly support the conclusions originally made in Morrison & Milbrandt (2015) and Morrison et al. (2015) regarding the

versatility of using a single free ice-phase category in a BMS to represent a wide range of

669 hydrometeor types and a majority of the important microphysical processes. This is evident from

the results since, except for hail in the convective core and near the surface, the overall ice

671 properties in the 1-category simulations (Fig. 7) are similar to those in the multi-category runs 672 (Figs. 12,15).

673

674 6 Conclusions

This study examined the impacts of predicting liquid fraction and multiple free ice-phase 675 categories in the P3 microphysics scheme in the context of cloud-resolving, quasi-idealized 676 hailstorm simulations. An important effect of predicting the liquid fraction is to improve the 677 parameterization of melting of ice, in which a portion of the melted mass is temporarily retained 678 in the mixed-phase particles and then gradually shed, depending on the degree of riming. This 679 increases the rate at which ice mass is transferred to rain for heavily-rimed ice for this set of 680 processes and ultimately reduces the amount of hail reaching the surface. In contrast, the impacts 681 of adding ice-phase categories tends to increase the amount of hail reaching the surface, and also 682 the hail sizes. This is due to reduced property dilution, which allows ice to be represented in at 683 least one category as large hail which can reside in the hail growth zone for longer times and thus 684 grow even larger. With multiple categories the dilution of properties is reduced; multiple modes 685 can coexist without loss to either of their sets of properties (with the exception of changes due to 686 category interactions via aggregation) and each population of ice can continue to evolve 687 accordingly. Hailstorm cases from two very different pre-storm environments were used which 688 strengthens the generality of the conclusions regarding the systematic impacts. 689

Since its inception, the P3 scheme has advanced in terms of its capacity to simulate hail. This 690 includes the implementation of triple-moment ice which controls excessive size sorting, the 691 692 predicted liquid faction which improves the representation of wet growth, melting, and shedding, and the use of multiple free ice categories which allows hail to grow to large sizes without 693 dilution from smaller particles. Future improvements pertaining to hail will include optimizing 694 the initiation and merging of ice in the multicategory configuration. We also plan to extend the 695 triple-moment treatment of ice to include the formal treatment of all microphysical processes, 696 thereby improving all process rates that impact the dispersion of the size spectra; this will be 697 reported in an upcoming study. On-going improvements to the representation of primary ice 698 nucleation, secondary ice production, and the representation of aerosols is on-going. We believe 699 700 that the P3 scheme is nearing the point that it can be used as a tool to conduct detailed process 701 studies on hailstorms.

In addition to using P3 as a research tool, all of the results and conclusions on the impacts on simulating hail in this study are valid for km-scale numerical weather prediction (NWP). While all of the simulations presented were done with a 200-m grid spacing to minimize interpretation

challenges associated with unresolved deep convection, all of the simulations discussed were 705 also done with a 1-km horizontal grid spacing km (not shown). Each of the sensitivities exhibited 706 at 200 m were similar at 1 km. This is at the scale of some current real-time experimental NWP 707 systems and is at the scale that operational systems are moving towards, even over large areas 708 709 such as the CONUS. While the configuration of P3 with triple-moment ice, predicted liquid fraction, and two ice categories requires that 18 hydrometeor tracers must be advected and 710 diffused, which would typically be considered computationally prohibitive for operational NWP, 711 microphysics schemes like P3 which have several variables per category lend themselves very 712 well to advection techniques such as the scaled flux vector transport method (SFVT; Morrison et 713 al., 2016). For this specific configuration of P3, 18 microphysics tracers could be advected for 714 the computational cost of advecting 4 primary tracers (one per hydrometeor category) with the 715 standard advection algorithm, plus a relatively small additional cost to compute the advective 716 tendencies of the 14 secondary tracers. Also, due to its extensive use of pre-computed look-up 717 718 tables, the P3 code itself is quite fast compared to other BMSs (see Morrison et al., 2015). We close in commenting, therefore, that the predictive detail in the LF-2CAT (or even LF-3CAT) 719 configuration could be easily be affordable for a km-scale operational NWP system, even with 720 current computational constraints, using an efficient advection algorithm such as SFVT or 721 artificial-intelligence based advection. 722

723

724 Acknowledgments

We thank George Bryan (NSF NCAR) for developing and maintaining the CM1 model.

726

727 **Open Research**

The code for the P3 scheme, as well as necessary files to interface the latest version with CM1, is

available at <u>https://github.com/P3-microphysics/P3-microphysics</u>. The code for the CM1 model is

available at <u>https://github.com/NCAR/CM1</u>. The model soundings and namelist files used to

731 generate the simulations are available upon request.

732

734 Appendix A

735 (see Table A1)

736 **Table A1.** List of symbols

abit AI. List of syn

737

Symbol	Description	Units
$B_{i,rim}$	rime ice volume mixing ratio (for a given category)	$m^3 kg^{-1}$
D	equivalent diameter	m
$D_{h,max}$	maximum diagnosed hail diameter	m
D_m	mass-weighted mean ice diameter	m
D_{mm}	mean-mass diameter	m
F_{liq}	liquid fraction (for a given ice category)	
Frim	rime ice mass fraction (for a given category)	
N(D)	number density function (particle size distribution, PSD)	$\# m^{-1} kg^{-1}$
N_0	intercept parameter (of gamma PSD)	$m^{-(1+\mu)} kg^{-1}$
nCat	number of ice categories	
N_i	total ice number concentration (for a given category)	# m ⁻³
Ni,tot	total ice number mixing ratio (for a given category)	# kg ⁻¹
Q_c	mass content/concentration of cloud (droplets)	kg m ⁻³
Q_i	total ice mass concentration/content (for a given category)	kg m ⁻³
$Q_{i,liq}$	liquid (on ice) mass mixing ratio (for a given category)	kg kg ⁻¹
$Q_{i,rim}$	rime mass mixing ratio	kg kg ⁻¹
$Q_{i,tot}$	total ice mass mixing ratio (for a given category)	kg kg ⁻¹
Q_r	mass content/concentration of rain	kg m ⁻³
V_m	mass-weighted fall speed for ice	m s ⁻¹
Wmax	peak updraft speed	m s ⁻¹
Z_{DR}	differential reflectivity (from dual-polarization radar)	dB
Ze	equivalent reflectivity (from model)	dBZ
Ze,c	equivalent reflectivity, column-maximum	dBZ
Z_H	horizontal reflectivity (from radar)	dBZ
$Z_{i,tot}$	reflectivity factor (6 th moment) mixing ratio (for a given	$m^6 kg^{-1}$
	category)	
$ ho_a$	air density	kg m ⁻³
$ ho_{\rm i}$	bulk ice density	kg m ⁻³
λ	slope parameter (of gamma PSD)	m ⁻¹
μ	shape parameter (of gamma PSD)	

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739 **References**

740 Balsara, D. S., & Shu, C. W. (2000). Monotonicity preserving weighted essentially non-

oscillatory schemes with increasingly high order of accuracy. *Journal of Computational*

742 Physics, 160(2), 405-452. https://doi.org/10.1006/jcph.2000.6443

743	Bryan, G. H., & Fritsch, J. M. (2002). A benchmark simulation for moist nonhydrostatic
744	numerical models. <i>Monthly Weather Review</i> , 130(12), 2917-2928.
745	https://doi.org/10.1175/1520-0493(2002)130<2917:ABSFMN>2.0.CO;2
746 747 748	Chen, J. P., & Tsai, T. C. (2016). Triple-moment modal parameterization for the adaptive growth habit of pristine ice crystals. <i>Journal of the Atmospheric Sciences</i> , 73(5), 2105-2122. https://doi.org/10.1175/JAS-D-15-0220.1
749	Cholette, M., Morrison, H., Milbrandt, J. A., & Thériault, J. M. (2019). Parameterization of the
750	bulk liquid fraction on mixed-phase particles in the predicted particle properties (P3) scheme:
751	Description and idealized simulations. <i>Journal of the Atmospheric Sciences</i> , 76(2), 561-582.
752	https://doi.org/10.1175/JAS-D-18-0278.1
753 754 755 756	 Cholette, M., Milbrandt, J. A., Morrison, H., Paquin-Ricard, D., & Jacques, D. (2023). Combining Triple-Moment Ice With Prognostic Liquid Fraction in the P3 Microphysics Scheme: Impacts on a Simulated Squall Line. <i>Journal of Advances in Modeling Earth Systems</i>, 15(4), e2022MS003328. https://doi.org/10.1029/2022MS00332
757	Cholette, M., Milbrandt, J. A., Morrison, H., Kirk, S., & Lalonde, L.É. (2024). Secondary Ice
758	Production Improves Simulations of Freezing Rain. <i>Geophysical Research Letters, in press</i> .
759	Dawson, D. T., Mansell, E. R., Jung, Y., Wicker, L. J., Kumjian, M. R., & Xue, M. (2014). Low-
760	level Z DR signatures in supercell forward flanks: The role of size sorting and melting of hail.
761	<i>Journal of the Atmospheric Sciences</i> , 71(1), 276-299. https://doi.org/10.1175/JAS-D-13-
762	0118.1
763 764	Deardorff, J. W. (1980). Stratocumulus-capped mixed layers derived from a three-dimensional model. <i>Boundary-layer meteorology</i> , <i>18</i> , 495-527. https://doi.org/10.1007/BF00119502
765	Ferrier, B. S. (1994). A double-moment multiple-phase four-class bulk ice scheme. Part I:
766	Description. <i>Journal of Atmospheric Sciences</i> , 51(2), 249-280. https://doi.org/10.1175/1520-
767	0469(1994)051<0249:ADMMPF>2.0.CO;2
768	Hashino, T., & Tripoli, G. J. (2007). The Spectral Ice Habit Prediction System (SHIPS). Part I:
769	Model description and simulation of the vapor deposition process. <i>Journal of the Atmospheric</i>
770	<i>Sciences</i> , <i>64</i> (7), 2210-2237. https://doi.org/10.1175/JAS3963.1
771 772	Jensen, A. A., Harrington, J. Y., Morrison, H., & Milbrandt, J. A. (2017). Predicting ice shape evolution in a bulk microphysics model. <i>Journal of the Atmospheric Sciences</i> , 74(6), 2081-

2104. https://doi.org/10.1175/JAS-D-16-0350.1

774	Jensen, A. A., Thompson, G., Ikeda, K., & Tessendorf, S. A. (2023). Improving the
775	representation of hail in the Thompson microphysics scheme. <i>Monthly Weather Review</i> ,
776	151(9), 2307-2332. https://doi.org/10.1175/MWR-D-21-0319.1
777 778 779	Johnson, M., Jung, Y., Milbrandt, J. A., Morrison, H., & Xue, M. (2019). Effects of the representation of rimed ice in bulk microphysics schemes on polarimetric signatures. <i>Monthly Weather Review</i> , <i>147</i> (10), 3785-3810. https://doi.org/10.1175/MWR-D-18-0398.1
780	Jouan, C., Milbrandt, J. A., Vaillancourt, P. A., Chosson, F., & Morrison, H. (2020). Adaptation
781	of the Predicted Particles Properties (P3) microphysics scheme for large-scale numerical
782	weather prediction. <i>Weather and Forecasting</i> , 35(6), 2541-2565.
783	https://doi.org/10.1175/WAF-D-20-0111.1
784	Kumjian, M. R., Ryzhkov, A. V., Melnikov, V. M., & Schuur, T. J. (2010). Rapid-scan super-
785	resolution observations of a cyclic supercell with a dual-polarization WSR-88D. <i>Monthly</i>
786	<i>Weather Review</i> , 138(10), 3762-3786. https://doi.org/10.1175/2010MWR3322.1
787	Lin, Y. L., Farley, R. D., & Orville, H. D. (1983). Bulk parameterization of the snow field in a
788	cloud model. <i>Journal of Applied Meteorology and Climatology</i> , 22(6), 1065-1092.
789	https://doi.org/10.1175/1520-0450(1983)022<1065:BPOTSF>2.0.CO;2
790 791 792	Loftus, A. M., Cotton, W. R., & Carrió, G. G. (2014). A triple-moment hail bulk microphysics scheme. Part I: Description and initial evaluation. <i>Atmospheric Research</i> , <i>149</i> , 35-57. https://doi.org/10.1016/j.atmosres.2014.05.013
793	Mansell, E. R., Ziegler, C. L., & Bruning, E. C. (2010). Simulated electrification of a small
794	thunderstorm with two-moment bulk microphysics. <i>Journal of the Atmospheric Sciences</i> ,
795	67(1), 171-194. https://doi.org/10.1175/2009JAS2965.1
796	Meyers, M. P., Walko, R. L., Harrington, J. Y., & Cotton, W. R. (1997). New RAMS cloud
797	microphysics parameterization. Part II: The two-moment scheme. <i>Atmospheric Research</i> ,
798	45(1), 3-39. https://doi.org/10.1016/S0169-8095(97)00018-5
799 800 801	Milbrandt, J. A., & Yau, M. K. (2005a). A multimoment bulk microphysics parameterization. Part I: Analysis of the role of the spectral shape parameter. <i>Journal of the Atmospheric Sciences</i> , <i>62</i> (9), 3051-3064. https://doi.org/10.1175/JAS3534.1
802 803 804	Milbrandt, J. A., & Yau, M. K. (2005b). A multimoment bulk microphysics parameterization. Part II: A proposed three-moment closure and scheme description. <i>Journal of the Atmospheric Sciences</i> , 62(9), 3065-3081. https://doi.org/10.1175/JAS3535.1

805 806 807	Milbrandt, J. A., & Morrison, H. (2013). Prediction of graupel density in a bulk microphysics scheme. <i>Journal of the Atmospheric Sciences</i> , 70(2), 410-429. https://doi.org/10.1175/JAS-D-12-0204.1
808 809	Milbrandt, J. A., Bélair, S., Faucher, M., Vallée, M., Carrera, M. L., & Glazer, A. (2016). The pan-Canadian high resolution (2.5 km) deterministic prediction system. <i>Weather and</i>
810	Forecasting, 31(6), 1791-1816. https://doi.org/10.1175/WAF-D-16-0035.1
811	Milbrandt, J. A., & Morrison, H. (2016). Parameterization of cloud microphysics based on the
812	prediction of bulk ice particle properties. Part III: Introduction of multiple free categories.
813	Journal of the Atmospheric Sciences, 73(3), 975-995. https://doi.org/10.1175/JAS-D-15-
814	0204.1
815	Milbrandt, J. A., Leroyer, S., Paquin-Ricard, D., Faucher, M., Zhang, S., & Jouan, C. (2018).
816	High resolution deterministic prediction system HRDPS. Update from version 4.4.0 to version
817	5.0.0 (p. 57). Technical Note, Canadian Meteorological Centre.
818	Milbrandt, J. A., Morrison, H., Dawson II, D. T., & Paukert, M. (2021). A triple-moment
819	representation of ice in the Predicted Particle Properties (P3) microphysics scheme. Journal of
820	the Atmospheric Sciences, 78(2), 439-458. https://doi.org/10.1175/JAS-D-20-0084.1
821	Morrison, H. C. J. A., Curry, J. A., & Khvorostyanov, V. I. (2005). A new double-moment
822	microphysics parameterization for application in cloud and climate models. Part I:
823	Description. Journal of the Atmospheric Sciences, 62(6), 1665-1677.
824	https://doi.org/10.1175/JAS3446.1
825	Morrison, H., Thompson, G., & Tatarskii, V. (2009). Impact of cloud microphysics on the
826	development of trailing stratiform precipitation in a simulated squall line: Comparison of one-
827	and two-moment schemes. Monthly Weather Review, 137(3), 991-1007.
828	https://doi.org/10.1175/2008MWR2556.1
829	Morrison, H., & Milbrandt, J. (2011). Comparison of two-moment bulk microphysics schemes in
830	idealized supercell thunderstorm simulations. Monthly Weather Review, 139(4), 1103-1130.
831	https://doi.org/10.1175/2010MWR3433.1
832	Morrison, H., & Milbrandt, J. A. (2015). Parameterization of cloud microphysics based on the
833	prediction of bulk ice particle properties. Part I: Scheme description and idealized tests.
834	Journal of the Atmospheric Sciences, 72(1), 287-311. https://doi.org/10.1175/JAS-D-14-
835	0065.1
836	Morrison, H., Milbrandt, J. A., Bryan, G. H., Ikeda, K., Tessendorf, S. A., & Thompson, G.
837	(2015). Parameterization of cloud microphysics based on the prediction of bulk ice particle

838 839	properties. Part II: Case study comparisons with observations and other schemes. <i>Journal of the Atmospheric Sciences</i> , 72(1), 312-339. https://doi.org/10.1175/JAS-D-14-0066.1
840 841 842	Morrison, H., Jensen, A. A., Harrington, J. Y., & Milbrandt, J. A. (2016). Advection of coupled hydrometeor quantities in bulk cloud microphysics schemes. <i>Monthly Weather Review</i> , <i>144</i> (8), 2809-2829. https://doi.org/10.1175/MWR-D-15-0368.1
843 844 845 846	Morrison, H., van Lier-Walqui, M., Fridlind, A. M., Grabowski, W. W., Harrington, J. Y., Hoose, C., & Xue, L. (2020). Confronting the challenge of modeling cloud and precipitation microphysics. <i>Journal of Advances in Modeling Earth Systems</i> , <i>12</i> (8), e2019MS001689. https://doi.org/10.1029/2019MS00168
847 848 849	Murakami, M. (1990). Numerical modeling of dynamical and microphysical evolution of an isolated convective cloud The 19 July 1981 CCOPE cloud. <i>Journal of the Meteorological Society of Japan. Ser. II</i> , 68(2), 107-128. https://doi.org/10.2151/jmsj1965.68.2_107
850 851 852	Naylor, J., & Gilmore, M. S. (2012). Convective initiation in an idealized cloud model using an updraft nudging technique. <i>Monthly Weather Review</i> , <i>140</i> (11), 3699-3705. https://doi.org/10.1175/MWR-D-12-00163.1
853 854 855 856 857	Park, S. Y., Lim, K. S. S., Kim, K., Lee, G., & Milbrandt, J. A. (2024). Introduction of Prognostic Graupel Density in Weather Research and Forecasting (WRF) Double-Moment 6- Class (WDM6) Microphysics and Evaluation of the Modified Scheme During the ICE-POP Field Campaign. <i>Geoscientific Model Development Discussions</i> , 2024, 1-29. https://doi.org/10.5194/gmd-2023-241
858 859 860	Paukert, M., Fan, J., Rasch, P. J., Morrison, H., Milbrandt, J. A., Shpund, J., & Khain, A. (2019). Three-moment representation of rain in a bulk microphysics model. <i>Journal of Advances in</i> <i>Modeling Earth Systems</i> , 11(1), 257-277. https://doi.org/10.1029/2018MS001512
861 862 863 864	Qu, Z., Korolev, A., Milbrandt, J. A., Heckman, I., Huang, Y., McFarquhar, G. M., Morrison, H., Wolde, M. & Nguyen, C. (2022). The impacts of secondary ice production on microphysics and dynamics in tropical convection. <i>Atmospheric Chemistry and Physics</i> , <i>22</i> (18), 12287-12310. https://doi.org/10.5194/acp-22-12287-2022
865 866 867	Reisner, J., Rasmussen, R. M., & Bruintjes, R. T. (1998). Explicit forecasting of supercooled liquid water in winter storms using the MM5 mesoscale model. <i>Quarterly Journal of the Royal Meteorological Society</i> , <i>124</i> (548), 1071-1107. https://doi.org/10.1002/qj.49712454804
868 869 870 871	Rutledge, S. A., & Hobbs, P. (1983). The mesoscale and microscale structure and organization of clouds and precipitation in midlatitude cyclones. VIII: A model for the "seeder-feeder" process in warm-frontal rainbands. <i>Journal of the Atmospheric Sciences</i> , <i>40</i> (5), 1185-1206. https://doi.org/10.1175/1520-0469(1983)040<1185:TMAMSA>2.0.CO;2

- 872 Seifert, A., & Beheng, K. D. (2006). A two-moment cloud microphysics parameterization for
- mixed-phase clouds. Part 1: Model description. *Meteorology and Atmospheric Physics*, 92(1),
- 45-66. https://doi.org/10.1007/s00703-005-0112-4
- Skamarock, W. C., Klemp, J. B., Dudhia, J., Gill, D. O., Barker, D. M., Duda, M. G., ... &
 Powers, J. G. (2008). A description of the advanced research WRF version 3. *NCAR technical note*, 475, 113.
- Thompson, G., & Eidhammer, T. (2014). A study of aerosol impacts on clouds and precipitation
 development in a large winter cyclone. *Journal of the Atmospheric Sciences*, *71*(10), 36363658. https://doi.org/10.1175/JAS-D-13-0305.1

Tsai, T. C., & Chen, J. P. (2020). Multimoment ice bulk microphysics scheme with consideration
for particle shape and apparent density. Part I: Methodology and idealized simulation. *Journal of the Atmospheric Sciences*, 77(5), 1821-1850. https://doi.org/10.1175/JAS-D-19-0125.1

Wang, J., Fan, J., Feng, Z., Zhang, K., Roesler, E., Hillman, B., ... & Xie, S. (2021). Impact of a
new cloud microphysics parameterization on the simulations of mesoscale convective systems
in E3SM. *Journal of Advances in Modeling Earth Systems*, *13*(11), e2021MS002628.
https://doi.org/10.1029/2021MS002628

Xue, L., Fan, J., Lebo, Z. J., Wu, W., Morrison, H., Grabowski, W. W., ... & Rasmussen, R. M.

- (2017). Idealized simulations of a squall line from the MC3E field campaign applying three
- 890 bin microphysics schemes: Dynamic and thermodynamic structure. *Monthly Weather*
- 891 *Review*, 145(12), 4789-4812. https://doi.org/10.1175/MWR-D-16-0385.1
- Yang, J., & Yau, M. K. (2008). A new triple-moment blowing snow model. *Boundary-layer meteorology*, *126*, 137-155. https://doi.org/10.1007/s10546-007-9215-4

Young, K. C., 1993: *Microphysical Processes in Clouds*, Oxford University Press, Inc. 427 pp.

- ⁸⁹⁵ Ziegler, C. L. (1985). Retrieval of thermal and microphysical variables in observed convective
- storms. Part 1: Model development and preliminary testing. *Journal of the Atmospheric*
- *Sciences*, *42*(14), 1487-1509. https://doi.org/10.1175/1520-
- 898 0469(1985)042<1487:ROTAMV>2.0.CO;2