The operational GDPS-YY 25Km Abdessamad Qaddouri &Vivian Lee

Collaborators

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Outline

- Why do we have to change the grid?
- Domain decomposition method used for GEM model on Yin-Yang grid.
- Blended variables in the overlap zone
- Some Results
- List of differences (GU25 vs GY25)

Why do we have to change the grid?

GU25 /GY25

Lat-Lon grid GU25

- 1024x800 grid-points
- 2 singular points
- High resolution near poles: 39km/0.05km
- Reached the limits of scalability for GEM model
- Needs special treatment near poles

Yin-Yang Grid GY25

- 1287x417x2 grid-points
- No singular points
- Grille spacing quasiuniform: 25km/17.2km
- Scales well for GEM model
- Needs special treatment in the overlap regions.

Timings

GU 25km – v4.7.0-rc5

GY 25km – v4.7.0-rc5

GY25 for global Forecast

The global forecast is based on the two-way nesting method between 2-limited area models; $\Omega = \{45^0 - 3\delta \le \lambda \le 315^o + 3\delta; -45^0 - \delta \le \theta \le 45^o + \delta\}; \delta = 2^0$
The global forecast is based on the two-way nesting method
between 2-limited area models;
Qaddouri and Lee 2011 Q.J.R.Meteorol.Soc.137:1913-1926

Domain decomposition method

- On each panel (Yin/Yang)
	- A system of forced primitive equations is solved with a local solver based on Implicit semi-Lagrangian time discretisation.
	- Boundary conditions are passed by cubic-Lagrange interpolation (non-matching grids)
	- Implicit discretisation: 3D-elliptic problem is solved by the iterative Schwarz method

Forced primitive Equations Spatial discretization

Girard et al. 2014 Mon.Wea.Rev..,142,3,1183-1196

Time Iterative Solver

$$
\frac{dF_i}{dt} + G_i = 0
$$
\n
$$
\frac{F_i^A}{\tau} + G_i^A = \frac{F_i^D}{\tau} - \beta G_i^D \equiv R_i; \quad \tau = \Delta t / 2
$$

Linearisation

$$
L_i = \left(\frac{F_i^A}{\tau} + G_i^A\right)_{lin}; \qquad N_i = \frac{F_i^A}{\tau} + G_i^A - \left(\frac{F_i^A}{\tau} + G_i^A\right)
$$

Do jter=1,2 (Crank Nicholson) Do iter=1,2 (Non-linear)

$$
(L_i)^{iter, iter} = (R_i)^{iter} - (N_i)^{iter-1, iter}; \qquad (N_i)^{0,1} = N_i(\mathbf{r}, t - \Delta t)
$$

end do $i = 1,..., Neg$

end do Côté et al. 1998 Mon.wea.Rev., 126, 1373-1395

Elliptic problem $P = \phi'$

$$
\nabla_{\zeta}^{2} P + \frac{\gamma}{\kappa \tau^{2} RT_{*}} \left(\delta_{\zeta}^{2} P + \overline{\delta_{\zeta} P}^{\zeta} - \varepsilon (1 - \kappa) \overline{P}^{\zeta \zeta} \right) = R
$$

 $\left|\delta_{\zeta}P-\varepsilon P^{\degree}\right|\right| = -\left(L^{\prime\prime}_{\theta}\right)_{T}$ *T* $RT_* \overset{C_{\zeta^1}}{\sim} \overset{C_{\zeta^1}}{\sim} \left| \right|_T = \overset{C_{\zeta^1}}{\sim} \theta$ ζ $\delta_{\zeta}P-\varepsilon$ $K\!\mathcal{T}$ γ יי
י * $\frac{1}{2} \frac{1}{D T} \left[\delta \frac{1}{2} P - \varepsilon P^2 \right]$ = - \rfloor $\vert \vert$ \mathbf{r} L $\overline{}$ $\left| -\varepsilon P^{\varepsilon} \right| = -\left(L''_{\theta} \right)_{T} \qquad \qquad \left| \frac{1}{\varepsilon \varepsilon^{2} P T} \left[\delta_{\zeta} P + \kappa P^{\varepsilon} \right] \right| = -\left(L''_{\theta} \right)_{S} + \frac{\gamma_{S}}{\varepsilon^{2} P T}$ $*$ $*$ $\frac{1}{2pT}\left|\delta_{\zeta}P+\kappa P^*\right|\right| = -(L^{\prime\prime}_{\theta})_S + \frac{\gamma_S}{\tau^2PT}$ *RT* $P + \kappa P^2$ $|| = -(L_{\theta}^{\nu})_S + \frac{\gamma_S}{2 \Delta T}$ RT_* $\left| \begin{matrix} 5 & 7 \end{matrix} \right|$ $\left| \begin{matrix} 7 & 7 \end{matrix} \right|$ *S* $S \left(\frac{1}{2} D T \right)$ $\tau K I_*$ $\phi_{\rm s}$ $|\delta_z P + \kappa P^{\dagger}|$ = $-(L''_{\alpha})_{\alpha} + \frac{\gamma}{2}$ KT^rKl_* γ $\left| \begin{array}{c} \Sigma_{D} & -\zeta \\ \end{array} \right|$ θ /S \pm 2 pm $\left|\sum_{\zeta} P + \kappa \overline{P}^{\zeta}\right| = -\left(L''_{\theta}\right)_{S} + \frac{\varphi_{S}}{\tau^{2}PT}$ \Box_S $\begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}$ $\frac{1}{\kappa^2 D T} \varphi_\zeta P +$ $\lfloor K \tau K I_* \rfloor$ γ α $+ \kappa P^{\text{2}}$ || = $-(L_{\theta})_{\text{s}}$ + -Vertical boundary conditions: Mixed type **Elliptic problem** $P = \phi^t + RT_*(Bs+q)$
 $\nabla^2_{\zeta}P + \frac{\gamma}{\kappa \tau^2 RT_*} \left(\delta^2_{\zeta}P + \overline{\delta_{\zeta}P}^{\zeta} - \varepsilon(1-\kappa)\overline{P}^{\zeta\zeta} \right) = R$

Vertical boundary conditions: Mixed type
 $\left[\frac{\gamma}{\kappa \tau^2 RT_*} \left(\delta_{\zeta}P - \varepsilon \overline{P}^{\zeta} \right) \right$

Horizontal boundary conditions: Dirichlet type

The others variables are calculated by back-substitution from P.

Semi-Lagrangian on GY grid

- 1-Extend each panel (Yin, Yang) by a halo (size depends on CFL_max),
- 2-Interpolate from other panel to the halos the fields and (u,v, ζ) from previous timestep,
- 3-Do Semi-Lagrangian time integration as usual in each panel. Goto 2

Qaddouri et al. 2012 Q.J.R.Meteorol.Soc.138:989-1003

Elliptic problem on GY grid with Schwarz method

- Global solution is obtained by solving iteratively 2 elliptic sub-problems (Yin/Yang)
	- 1) receive Boundary conditions (BCs) from the other panel; solve local elliptic problem.
	- 2) if boundary conditions converge, stop; else send BCs to other panel ; goto 1

 Note : we use 2 degrees as overlap to increase convergence. Qaddouri et al. 2008 Appl.Numerical.Math.,58,4,459-471

Iterative Schwarz method : GY grid

GDPS_YY 25Km : only 4 iterations are needed for convergence with 2 degrees overlap

Why are there differences in the overlap?

- At each time step, the value of all the dynamical fields are prescribed by the other panel in its piloting region.
- The local solution of each panel includes the overlap region needed for the convergence of the elliptic problem.
- The two LAM solutions in the overlap can evolve independently (even though we assure a global convergence in the elliptic solver).
- Small and sharp differences may arise between the two panel point values in the overlap region (due to some schemes that have threshold parameters).

Solution: Flow relaxation scheme (blending)

• To eliminate the sharp differences, the point values in the overlap region are relaxed toward the value of the other panel at the end of dynamical time step (before physics).

$$
\frac{\partial F^l(x,t)}{\partial t} = k(x) \left\{ F^l(x,t) - F^{3-l}(x,t) \right\},
$$
 = 1,2

• No change is made when the two panel solutions are in agreement

H C Davies 1976 Q J Roy Met Soc 102 405-418

Solution: Flow relaxation scheme (blending)

 \bullet k(x) constant

$$
F_r^l(x,t) = 0.5 * \{F^l(x,t) + F^{3-l}(x,t)\}, \ l = 1,2
$$

• Several tests have been conducted ; the solution of relaxing only the winds (u,v) and generalized vertical velocity ζ in the overlap region has been proven the best.

Flow of GEM GY grid

Overlap zone

Differences between GU and GY

